

# **Galaxy Systems in the Optical and Infrared**

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# Plan of the lectures:

I. Identification, global properties, and scaling relations

**II. Structure and dynamics**

III. Properties of the galaxy populations

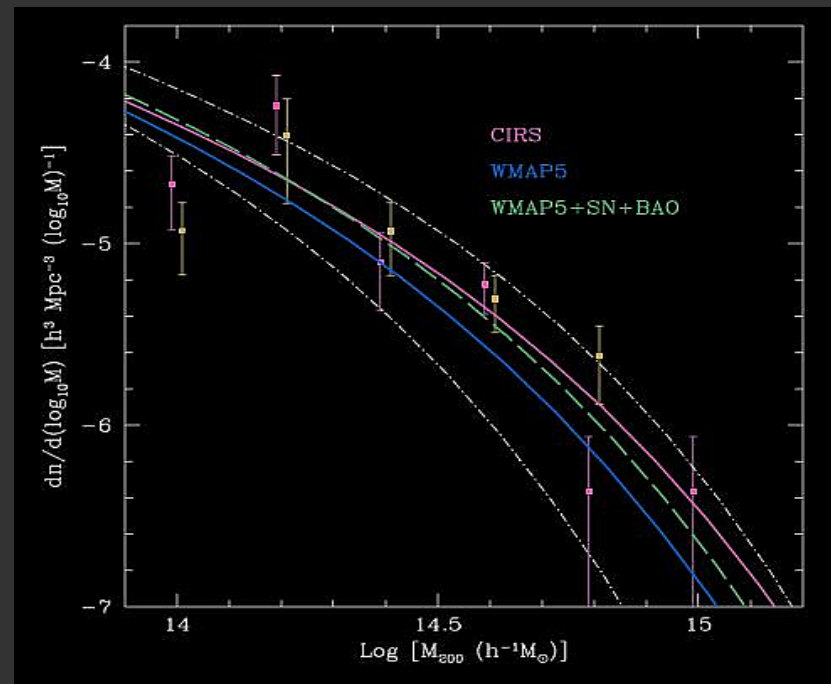
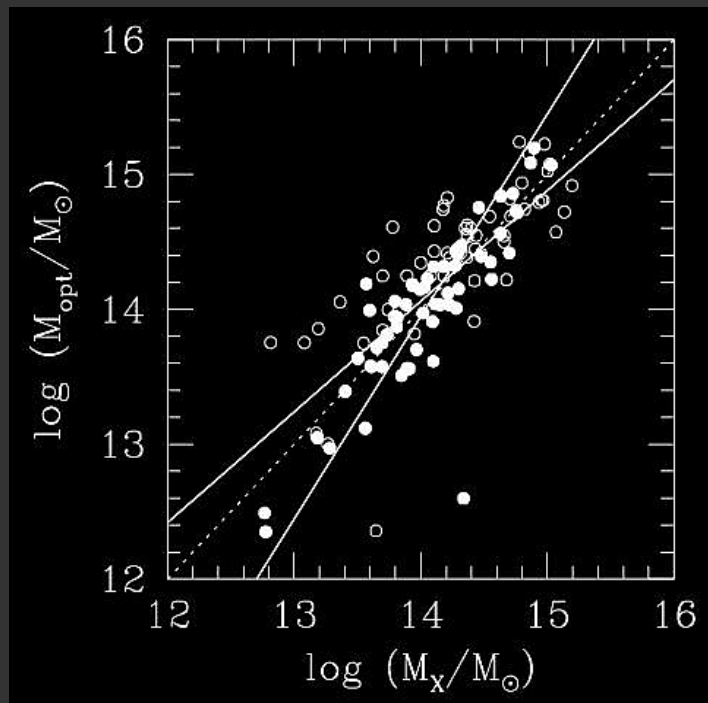
# Introduction

Early cluster mass determinations based  
on the *light traces mass* hypothesis



# Early cluster mass determinations based on the *light traces mass* hypothesis

Indirect evidence supports this hypothesis



Early cluster mass determinations based on the *light traces mass* hypothesis

Indirect evidence supports this hypothesis

Must **prove** it by direct comparison of the TRACER and MASS distributions

$M(r)$  determination  $\Rightarrow$  clues on:

- nature of DM
- formation and evolution of galaxy clusters

## Cold DM:

halo density profiles have central cusp

$$\rho_{NFW} = \frac{\rho_0}{(cr/r_{200})(1 + cr/r_{200})^2}$$

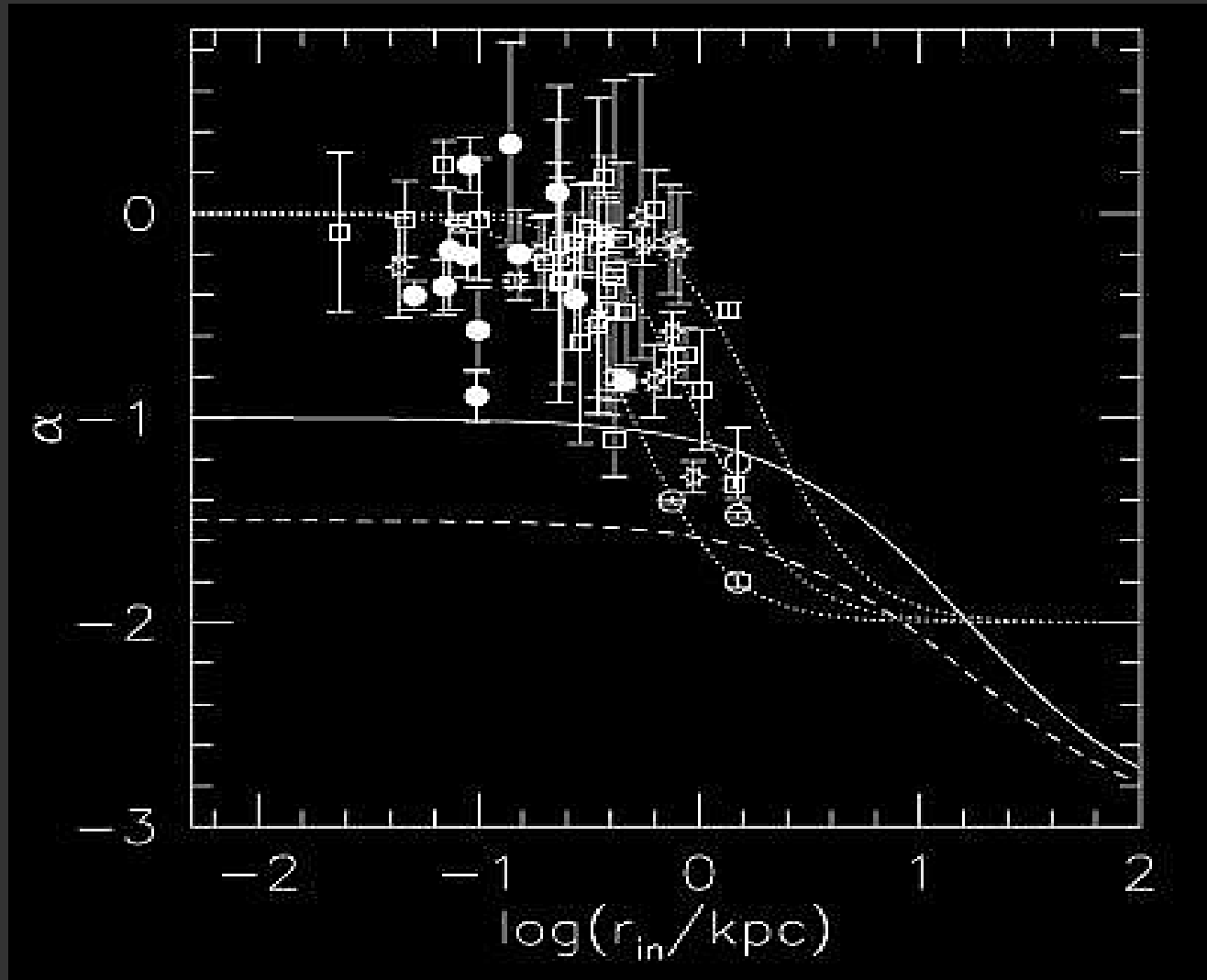
from cosmological numerical simulations

$$\rho_{Hernquist} = \frac{\rho_0}{r(r + r_H)^3}$$

used in theoretical modelling; note steeper slope

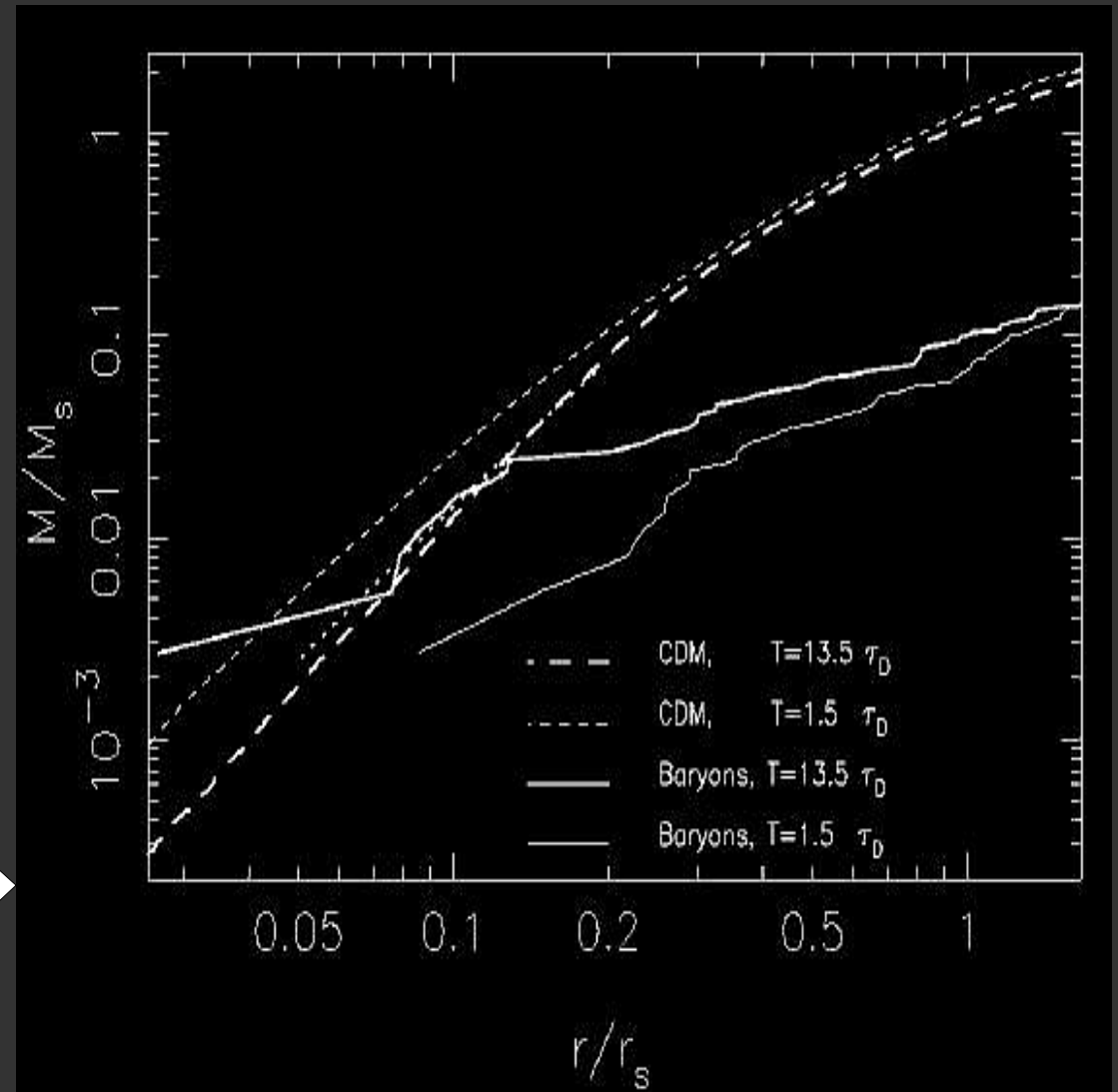
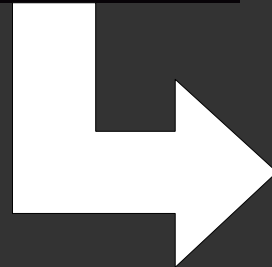
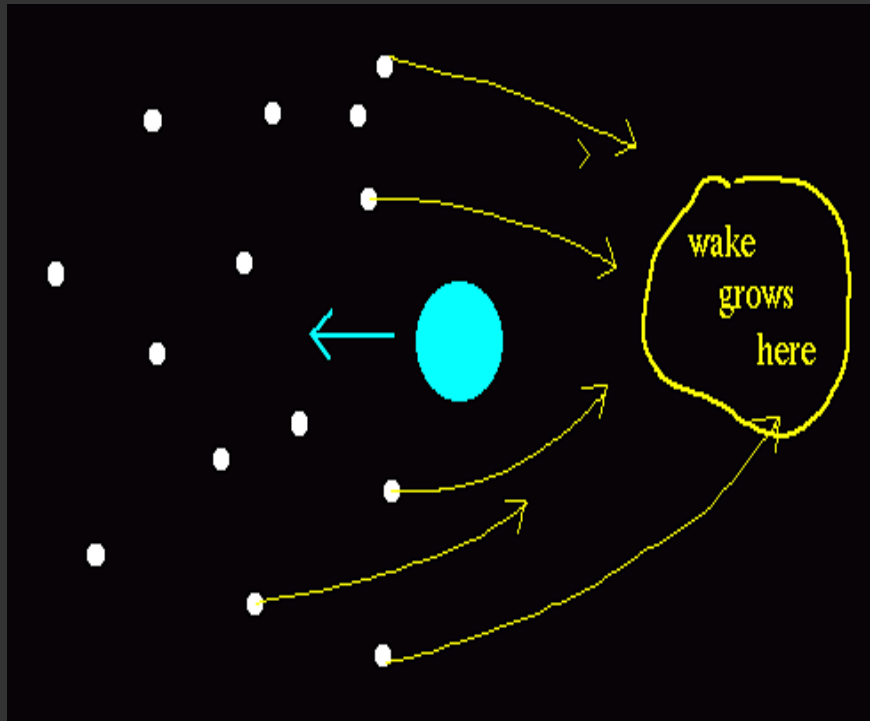


# Galaxy rotation curves: **no central cusp?**



(de Blok & Bosma 02)

# Central cusp erased by dynamical friction?



(El Zant+04)

# Halo density profiles with central core

$$\rho_{Burkert} = \frac{\rho_0}{(1 + r/r_c)[1 + (r/r_c)^2]}$$

Note: same asymptotic slope as NFW

$$\rho_{SIS}(r) = \frac{\rho_0}{1 + (r/r_c)^2}$$

Note: shallower asymptotic slope

# Dynamical analysis: methods

# The Jeans equation

$$M(< r) = -\frac{r\sigma_r^2}{G} \left( \frac{d \ln \nu}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right)$$



$$\beta(r) \equiv 1 - \frac{\langle v_t^2 \rangle(r)}{\langle v_r^2 \rangle(r)}$$

# The Jeans equation

$$\frac{d(\nu\sigma_r^2)}{dr} + 2\beta\frac{\nu\sigma_r^2}{r} = -\nu\frac{d\phi}{dr}$$



$$\beta(r) \equiv 1 - \frac{\langle v_t^2 \rangle(r)}{\langle v_r^2 \rangle(r)}$$

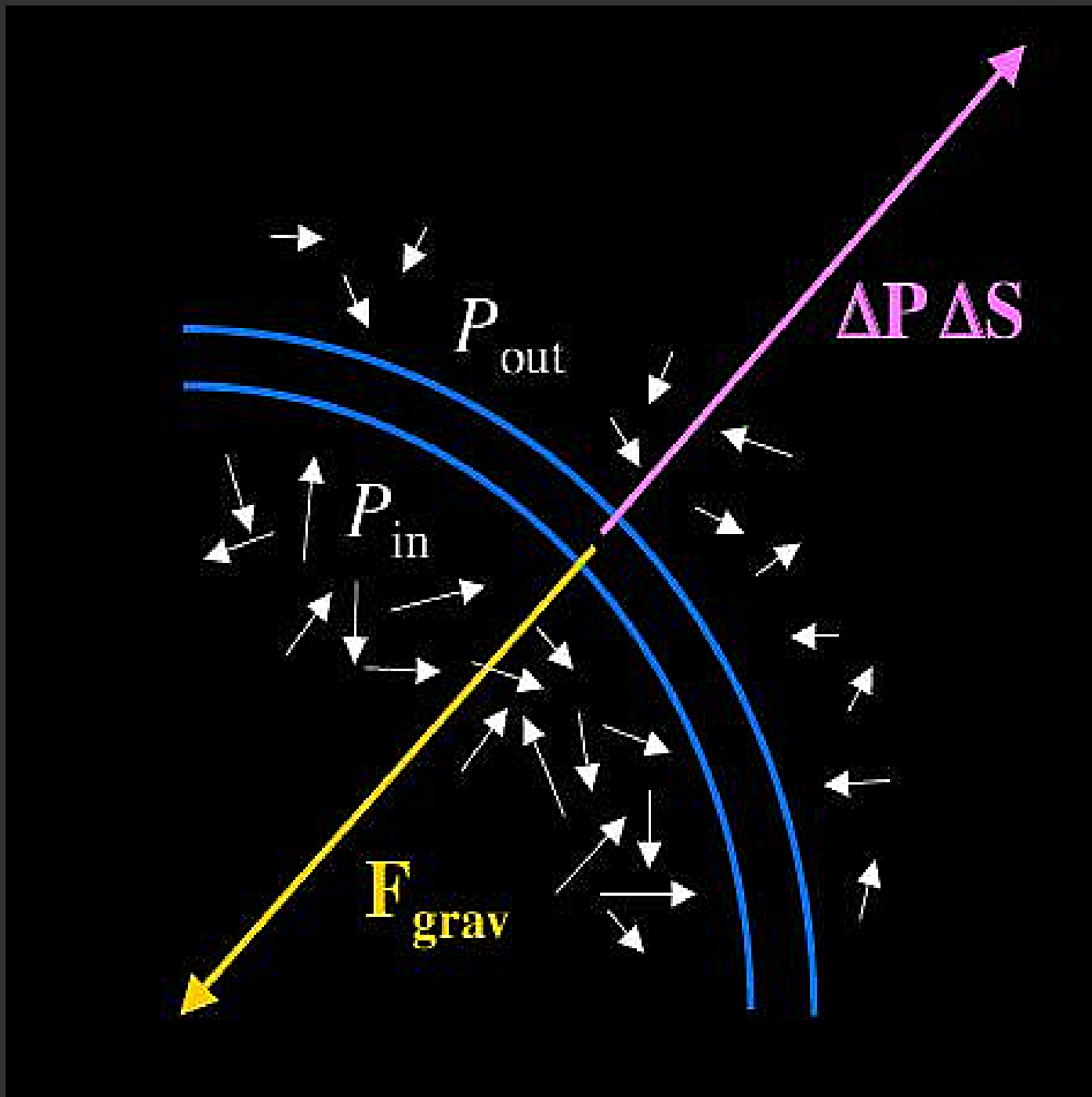
# The Jeans equation

$$\frac{d(\nu\sigma_r^2)}{dr} + 2\beta\frac{\nu\sigma_r^2}{r} = -\nu\frac{d\phi}{dr}$$



Dynamical pressure gradient

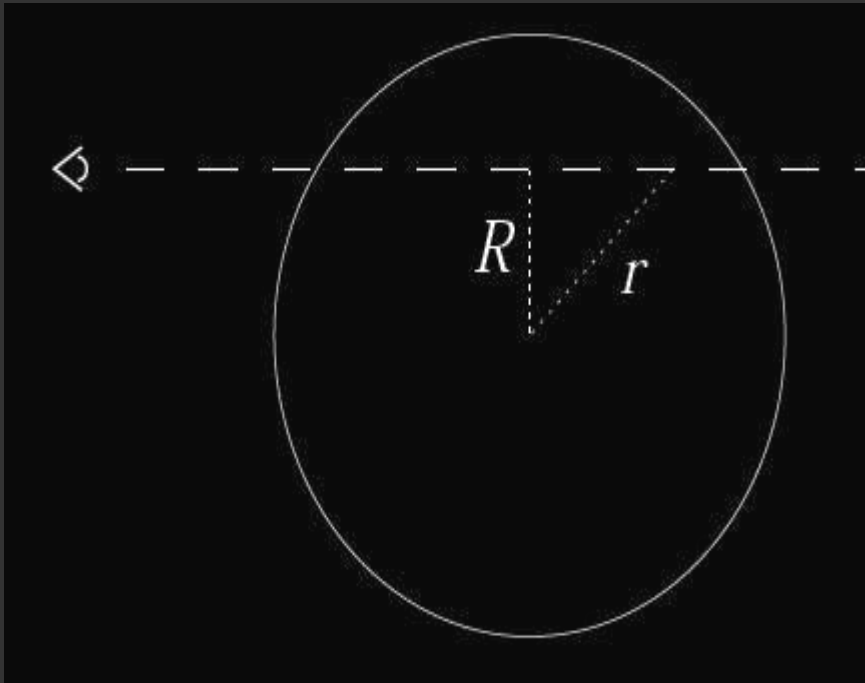
Gravitational potential gradient



(from Gary Mamon's University lectures)



3-d profiles enter the Jeans equation  
but only projected profiles are observable



(from G. Mamon's lectures)

$$\nu(r) = -\frac{1}{\pi} \int_r^{\infty} \frac{dN}{dR} \frac{dR}{\sqrt{R^2 - r^2}}$$



$$N(R) = 2 \int_R^{\infty} \frac{\nu r dr}{\sqrt{r^2 - R^2}}$$

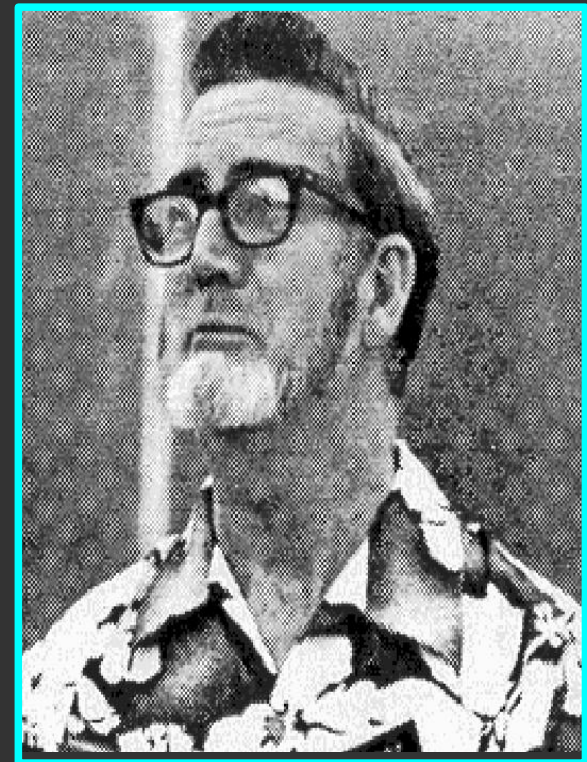
Spherical symmetry:  
direct Abel inversion of density profile

Note:

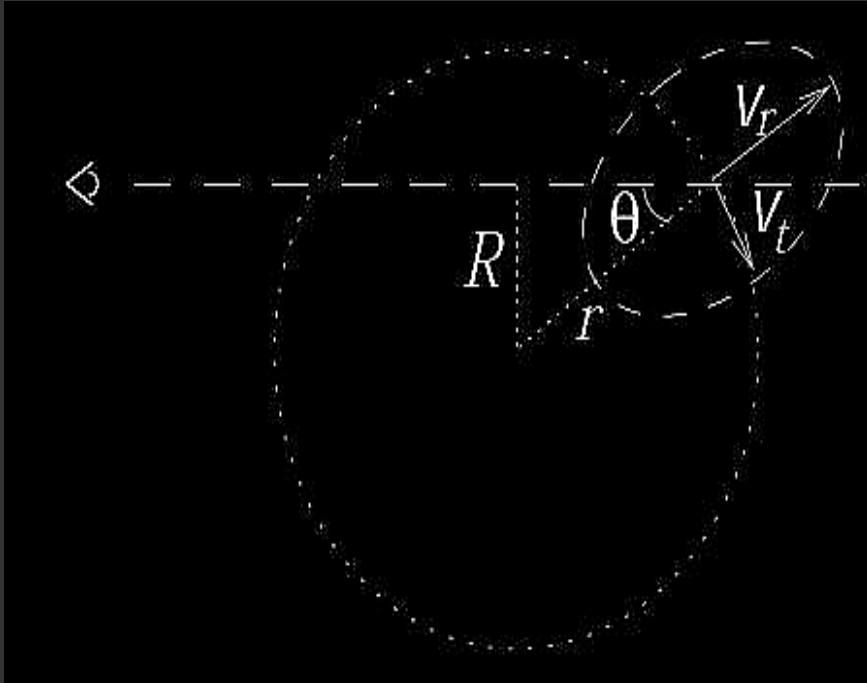
Niels Henrik Abel (\*1802 †1829)

*is not*

George Ogden Abell (\*1927 †1983)



3-d profiles enter the Jeans equation  
but only projected profiles are observable



(from G. Mamon's lectures)

$$\sigma_r^2 = -\frac{1}{\pi\nu(r)} \int_r^\infty \frac{d[N \times \sigma_p^2]}{dR} \frac{dR}{\sqrt{R^2 - r^2}}$$



$$N(R)\sigma_p^2(R) = 2 \int_R^\infty \left(1 - \beta \frac{R^2}{r^2}\right) \frac{\nu \sigma_r^2(r) r dr}{\sqrt{r^2 - R^2}}$$

$\beta$  needed to invert the velocity dispersion profile;  
not a simple Abel inversion (Mamon & Boué 08)

# Playing the Jeans game:

Observables  
 $N(R), \sigma_p(R)$

$+\beta(r)$



$M(r)$

Mamon &  
 Boué 08

Observables  
 $N(R), \sigma_p(R)$

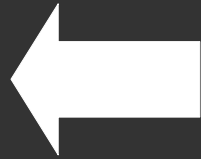
$+M(r)$



$\beta(r)$

Binney &  
 Mamon 82

Observables  
 $N(R), \sigma_p(R)$



$M(r)+\beta(r)$

Bacon+83

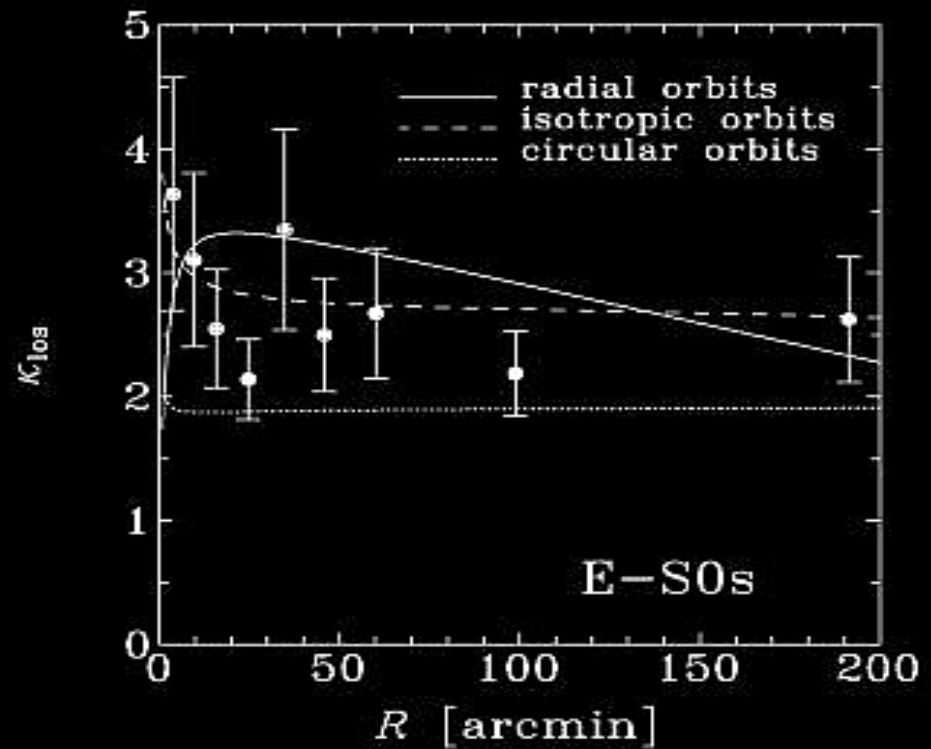
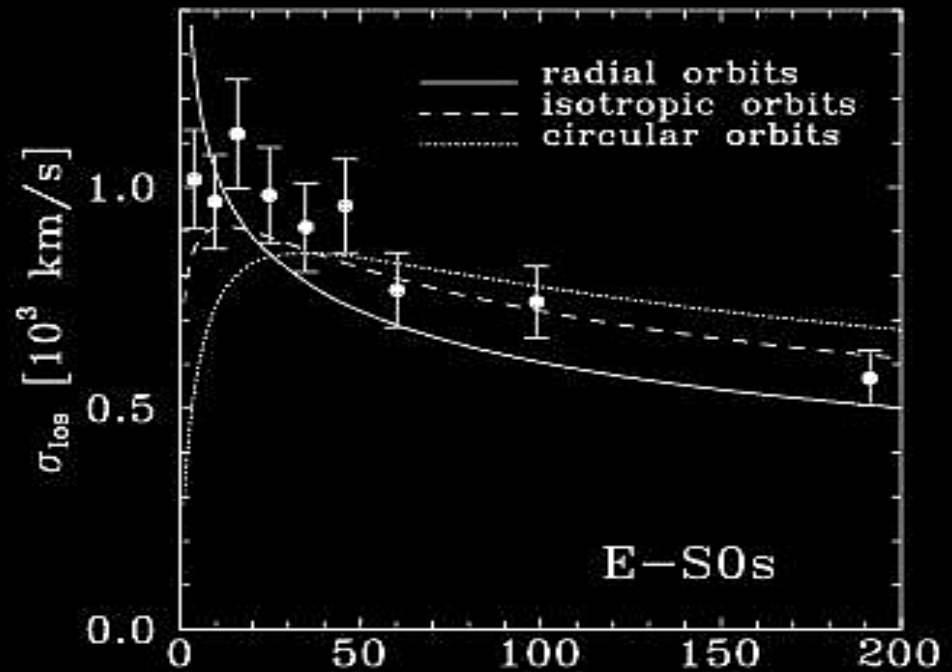
$$\nu \sigma_r^2 = -G \int_r^\infty \nu(\xi) \frac{M(< \xi)}{\xi^2} \exp \left[ 2 \int_r^\xi \frac{\beta dx}{x} \right] d\xi$$

van der  
 Marel 94

# Breaking the $M$ - $\beta$ degeneracy

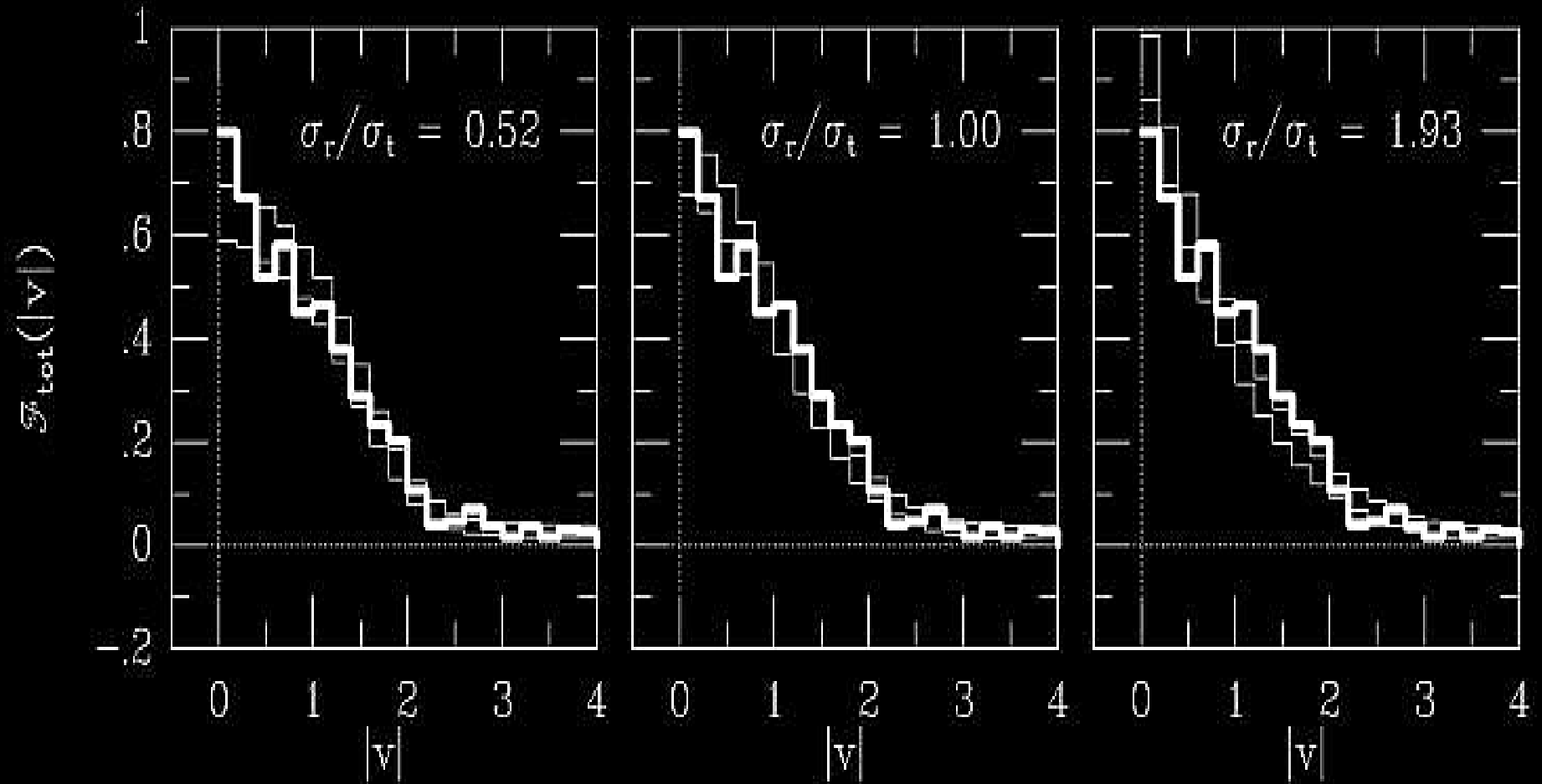
- D.F. models compared to proj. phase-space distrib. via Maximum Likelihood analysis
- Fit the whole velocity distribution, not only  $\sigma_p(R)$
- Use several tracers of the gravitational potential

E.g., use  
Kurtosis profile  
to constrain  $\beta(r)$   
of the Coma cluster  
(Łokas & Mamon 03)



Velocity dispersion

Velocity kurtosis



E.g. fit the whole velocity distribution of a stacked  
of several clusters from the CNOC survey  
(van der Marel + 00)

# Additional problems:

- clusters are not closed systems

*...but almost: 8% total mass in last  $0.1 t_H$*

*Intense accretion phase seen as subclustering*

*More problems for groups and high- $z$  systems*

- no net rotation assumed

*...OK, little if any evidence for rotation*

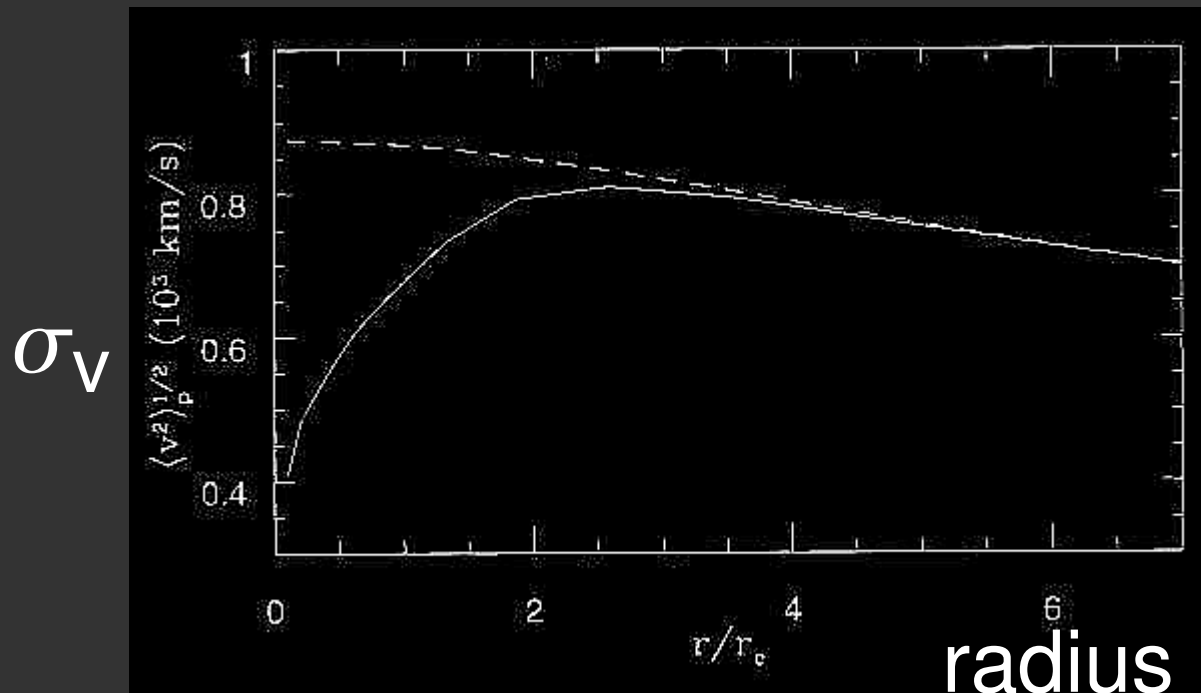


# Additional problems:

- collisionless systems?

*...high- $\sigma_v \Rightarrow$  no mergers, no dissipation*

*BUT beware of groups & dynamical friction!*



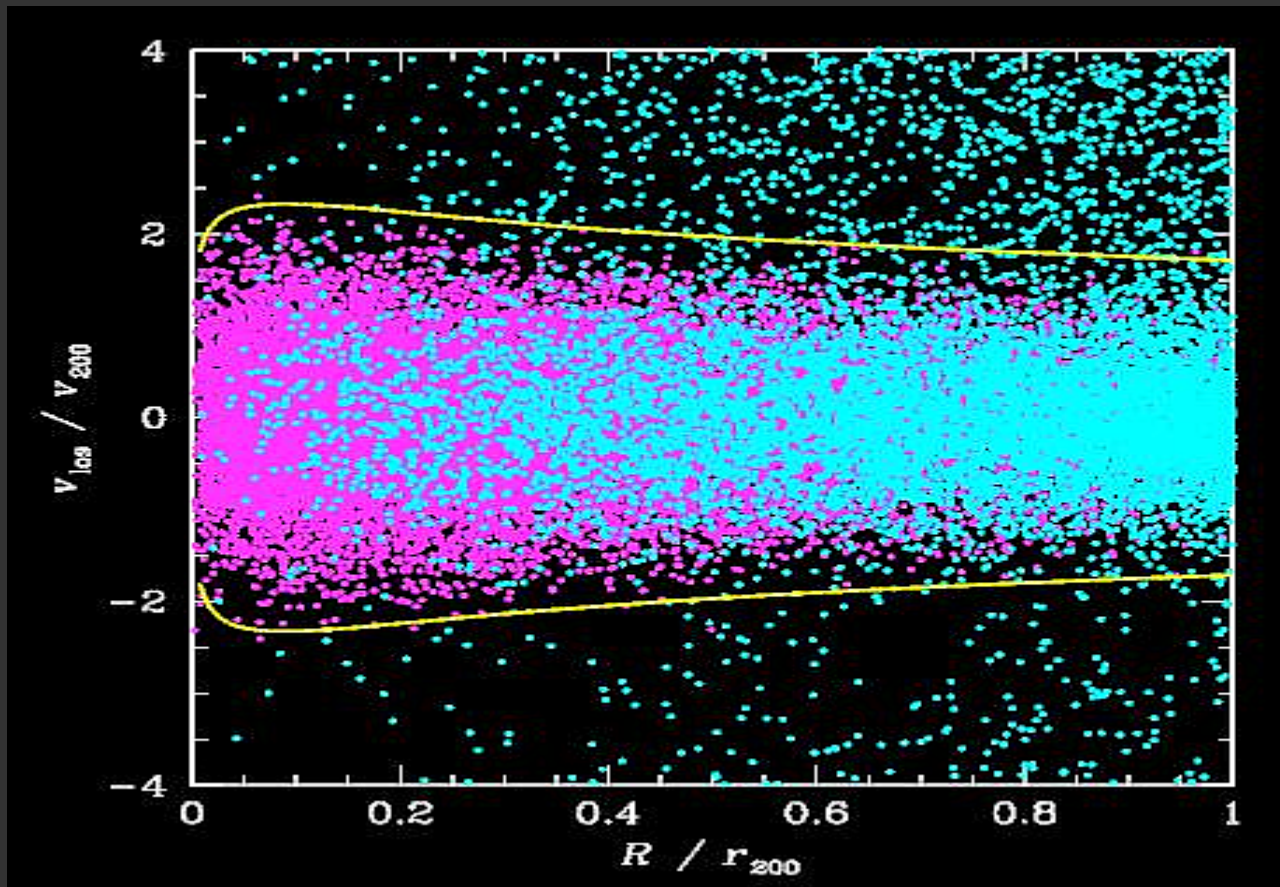
(Menci & Fusco-Femiano 96)

# Additional problems:

- interlopers

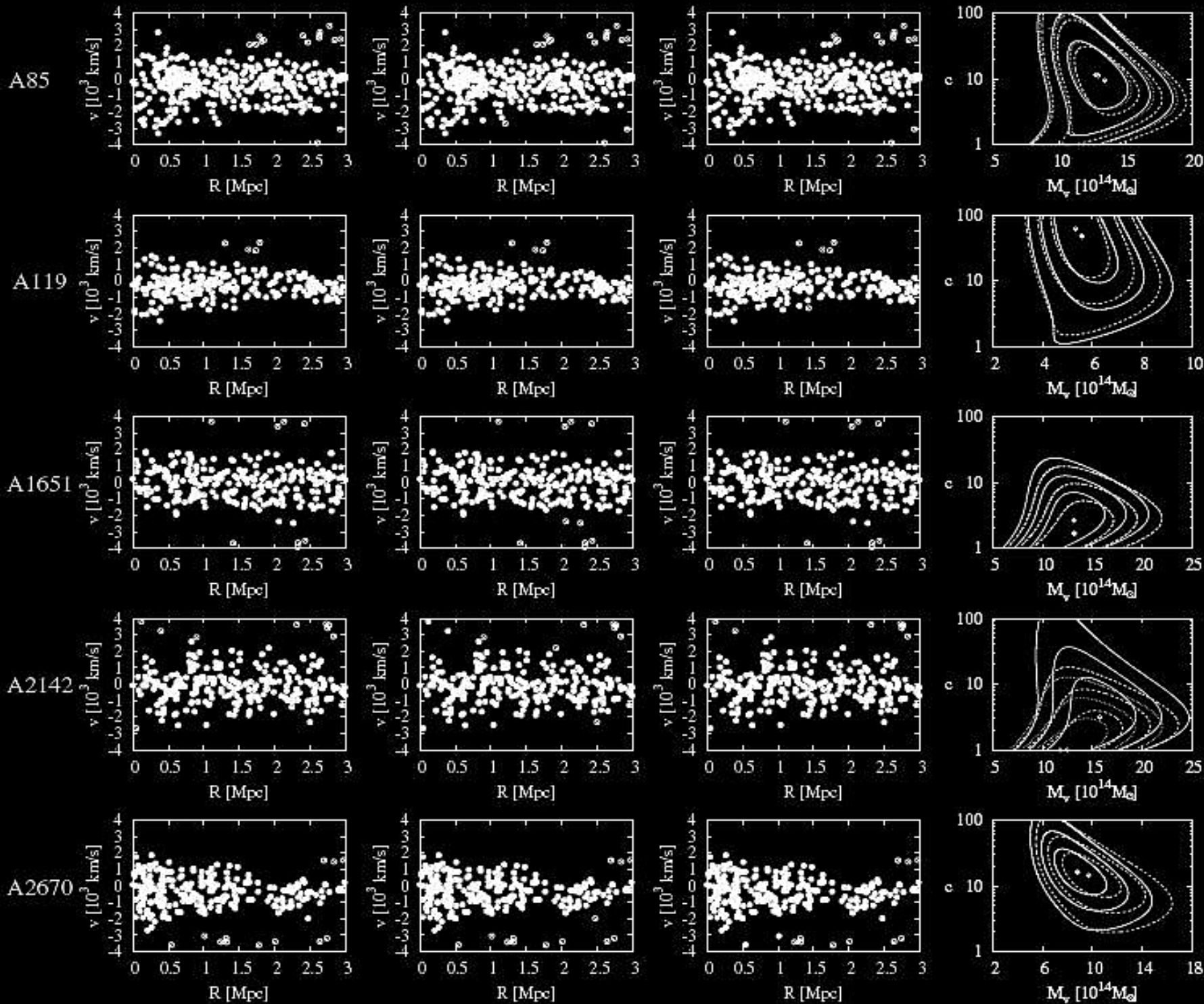
*...several techniques, they work pretty well*

Velocity



Radius

(Mamon+08)



# Additional problems:

- small number statistics

*...few clusters with  $N_z > 500 \rightarrow$  STACK MANY  
Scale  $R$  and  $V$  with virial quantities ( $r_{200}$ ,  $v_{200}$ )  
(clusters quasi-homologous family of objects)*

# Samples of (stacked) clusters

- CNOC, 16 clusters,  $\langle z \rangle = 0.17-0.55$ ,  $\langle \sigma_v \rangle \approx 900$  km/s,  $\approx 1000$  gals out to  $r < r_{200}$  (Carlberg+97)
- ENACS, 59, 700 km/s, 2700 gals (Katgert+96)
- CAIRNS, 9, 700 km/s, 800 gals (Rines+03)
- CIRS, 65, 600 km/s, 3300 SDSS gals (Rines & Diaferio 06)
- EDisCS, 16,  $0.4 < z < 0.9$ , 600 km/s, 500 gals (White+05)
- 2dFGRS, 43, 500 km/s, 700 gals (Biviano & Girardi 03)
- GEMS, 31 X-ray, 350 km/s, 700 gals (Osmond & Ponman 02)
- + WINGS (Fasano+06) + LARCS (Pimbblet+01)
- + ICBS (Dressler+09)

# An alternative to Jeans: the Caustic technique

$A(r)$



$\phi(r)$

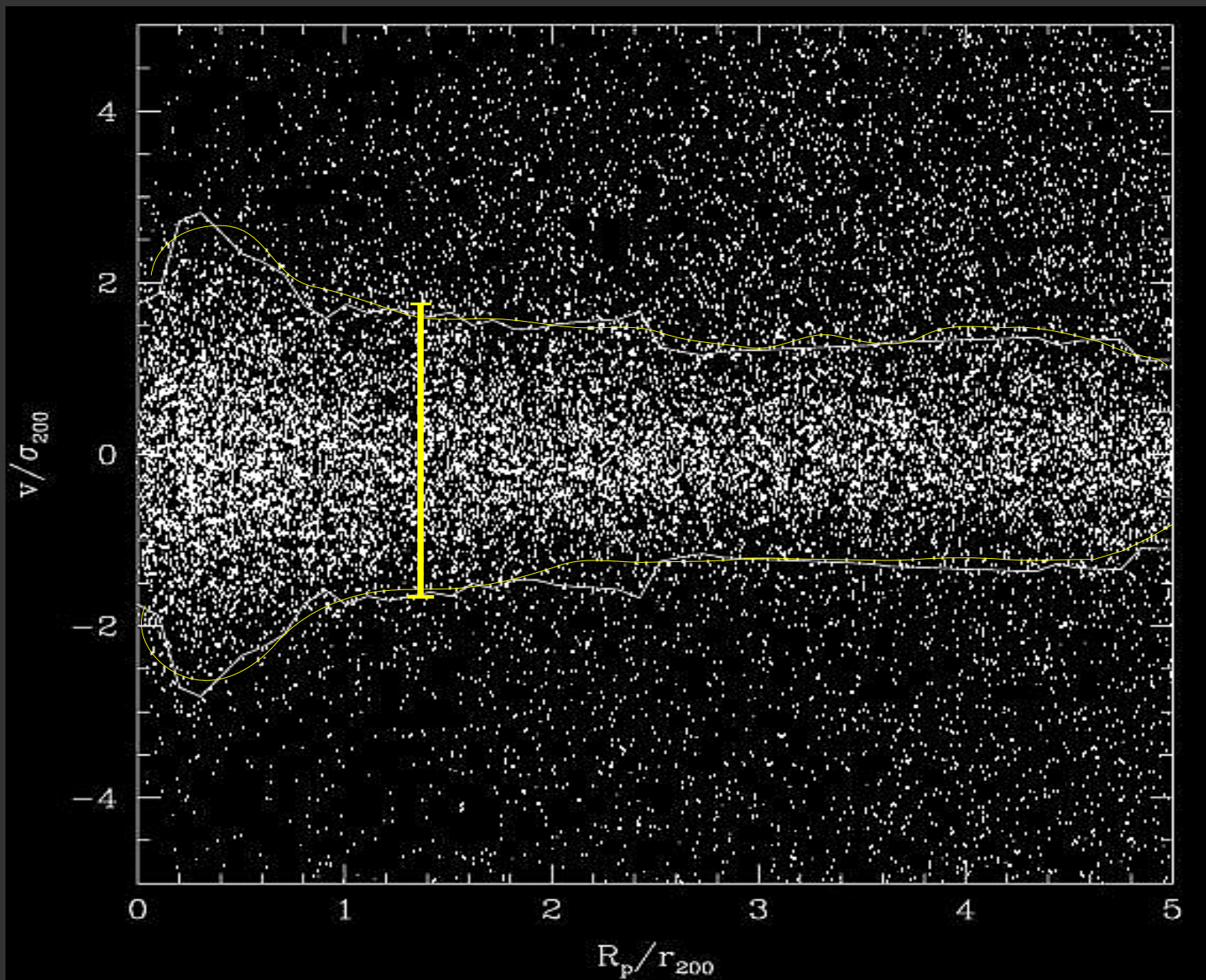
through

$F(r; \beta, \phi)$

$\approx \text{const}$

outside

the center

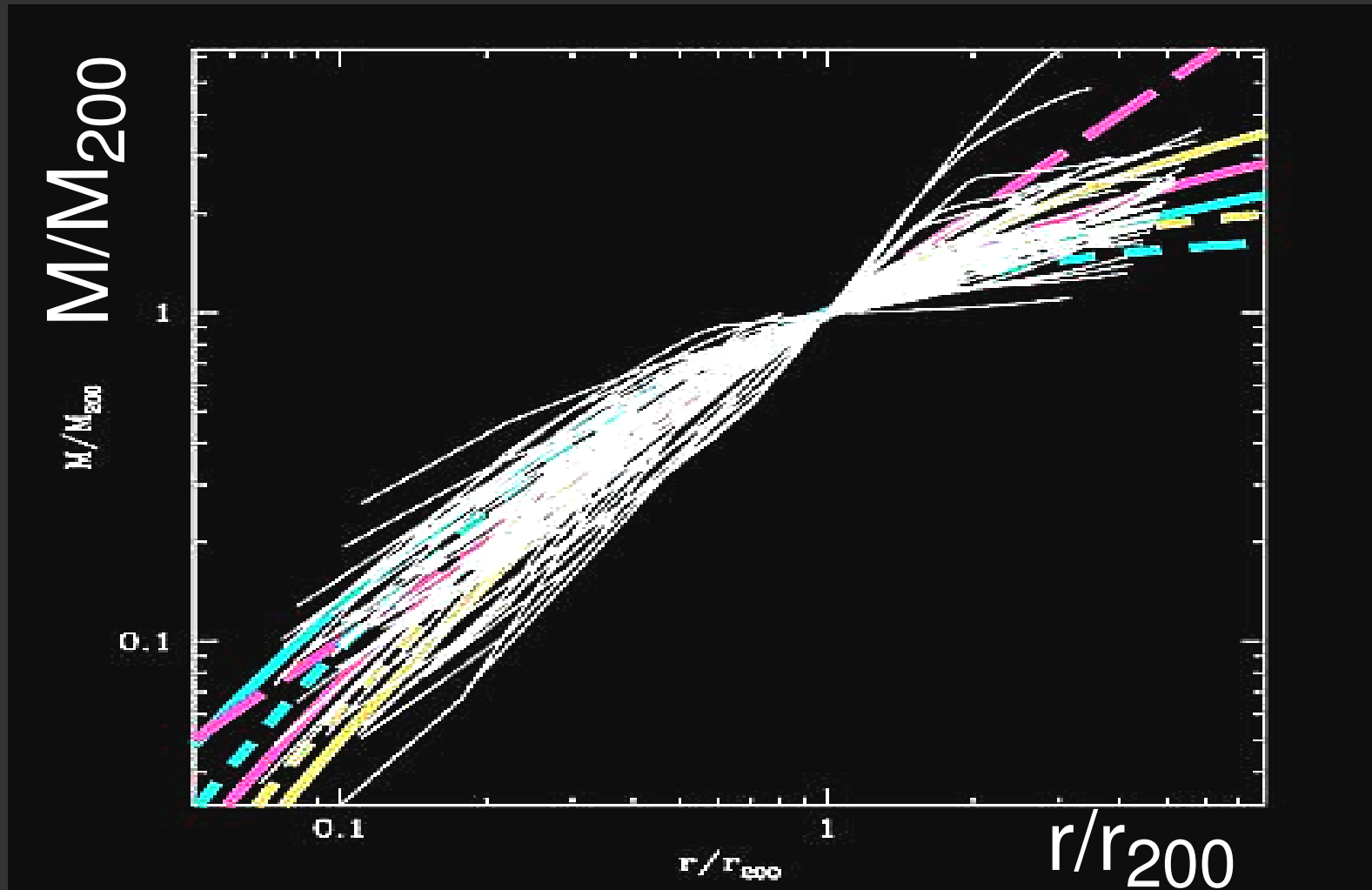


(Diaferio 99; Rines & Diaferio 06)

# Mass profiles

# CIRS cluster mass profiles (Caustic)

(Rines & Diaferio 06)



Fitting models: Solid lines: NFW  $c=3, 5, 10$

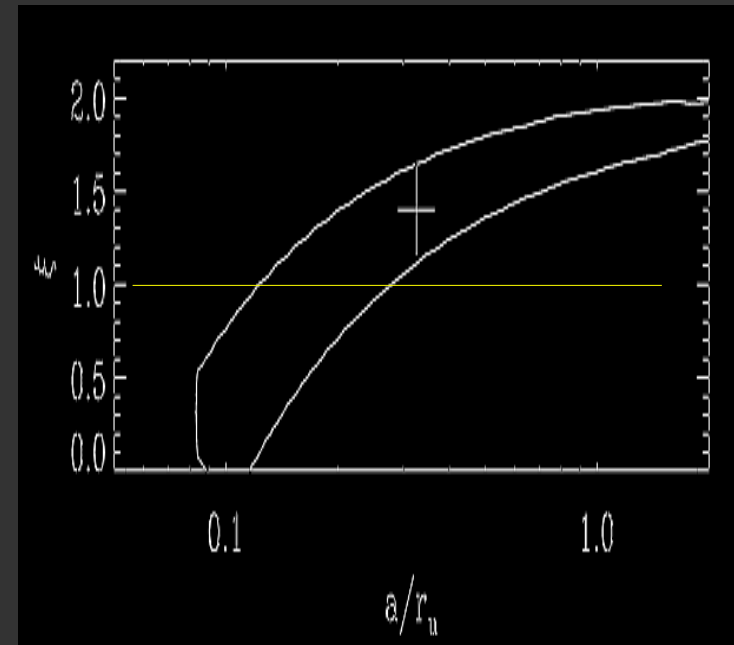
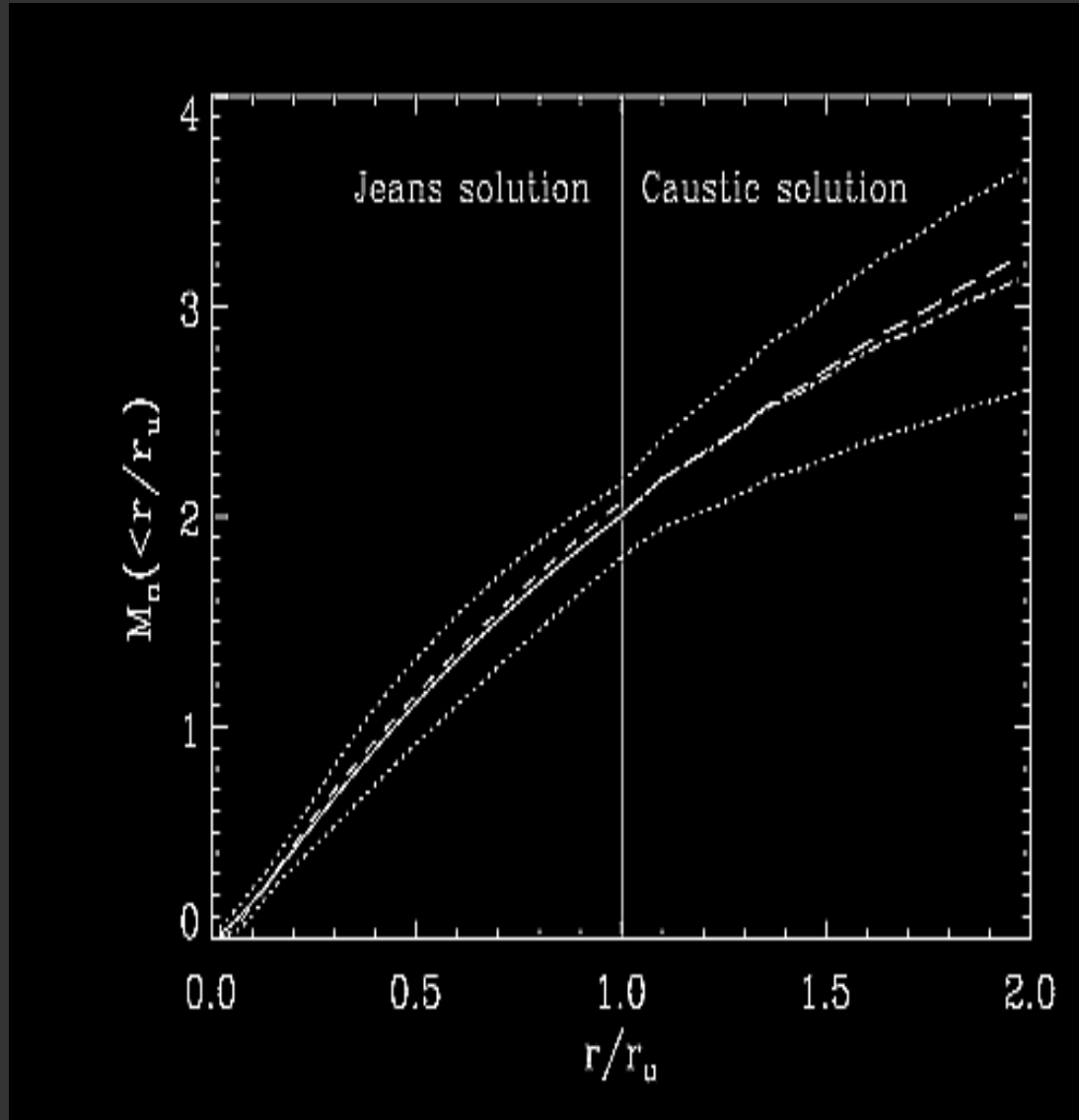
Short dashed: Hernquist

Long dashed: Isothermal sphere



# 2dFGRS (Jeans + caustic)

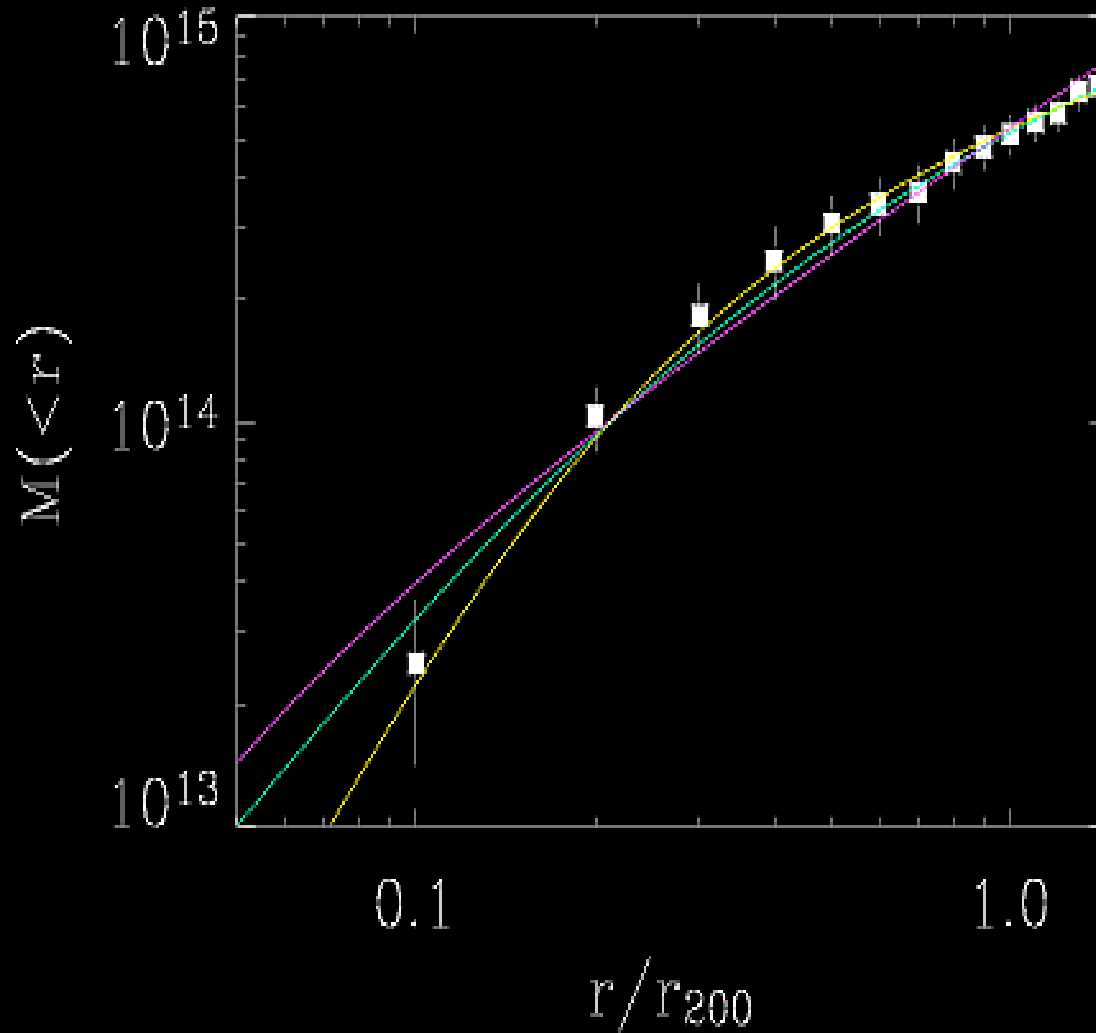
(B. & Girardi 03)



Best-fit inner slope  
consistent with NFW

# ENACS (Jeans)

(Katgert+04)



Burkert

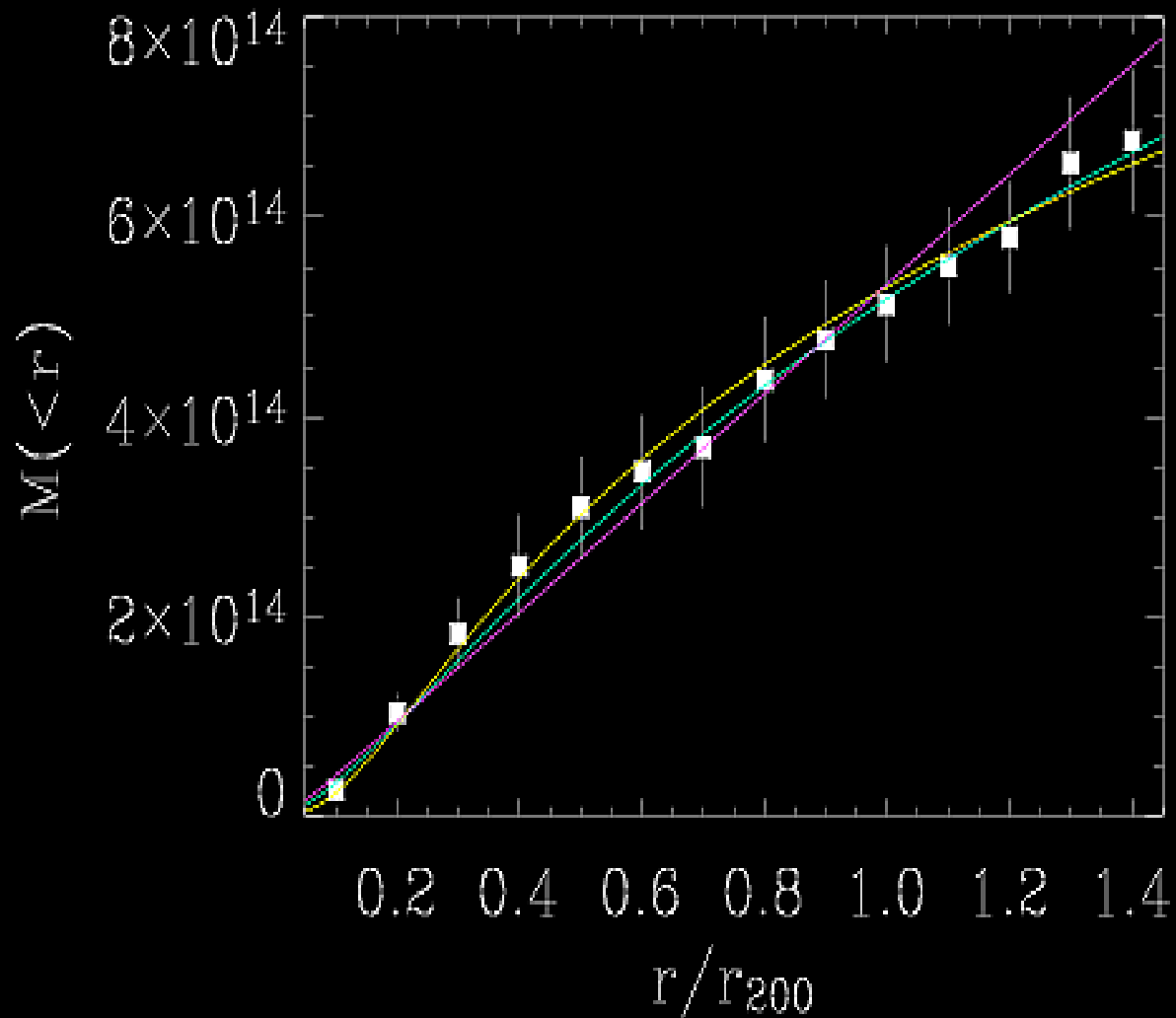
$r_c/r_{200}=0.15$

NFW  $c=4 \pm 2$

SIS

# ENACS (Jeans)

(Katgert+04)



Burkert

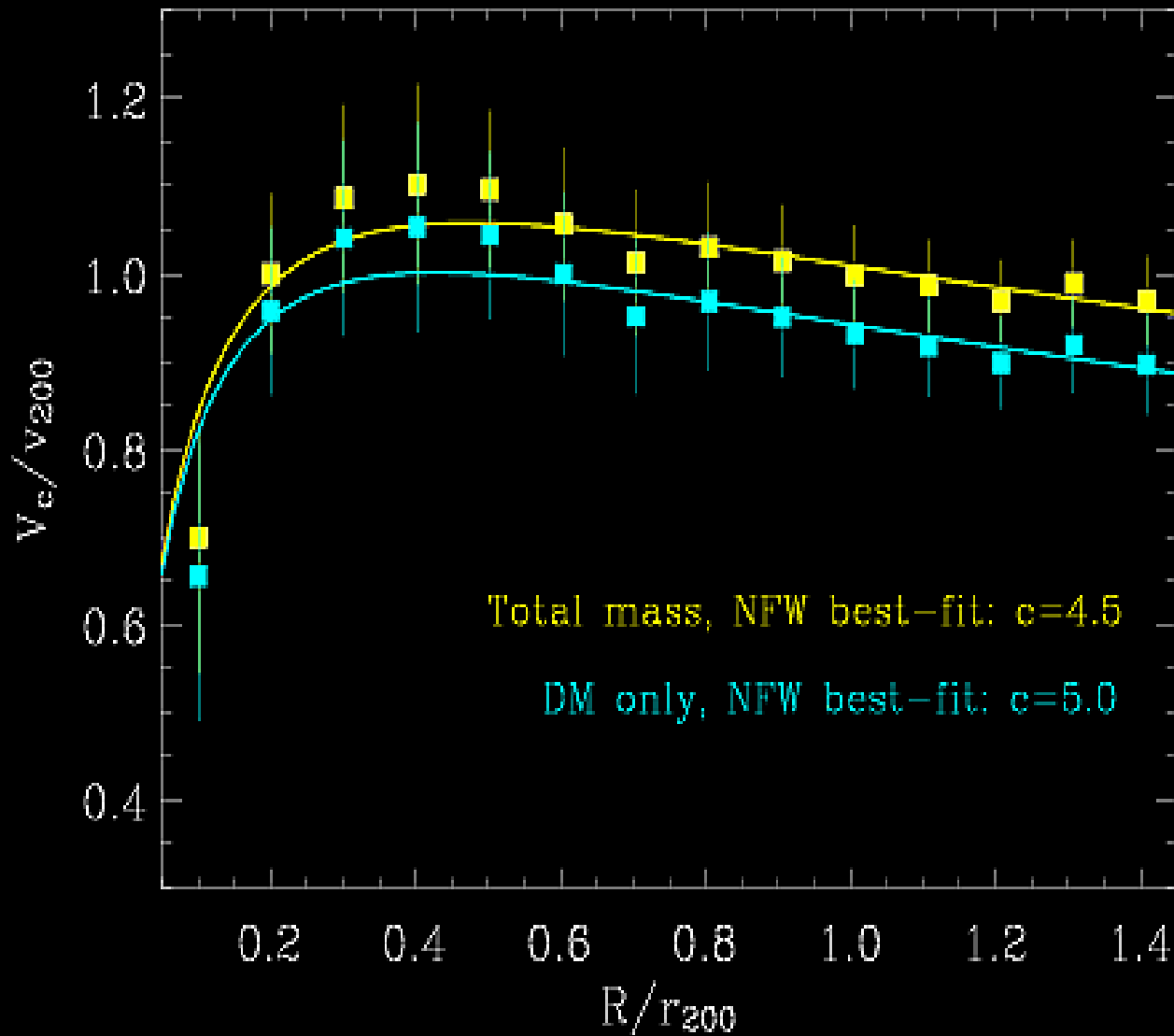
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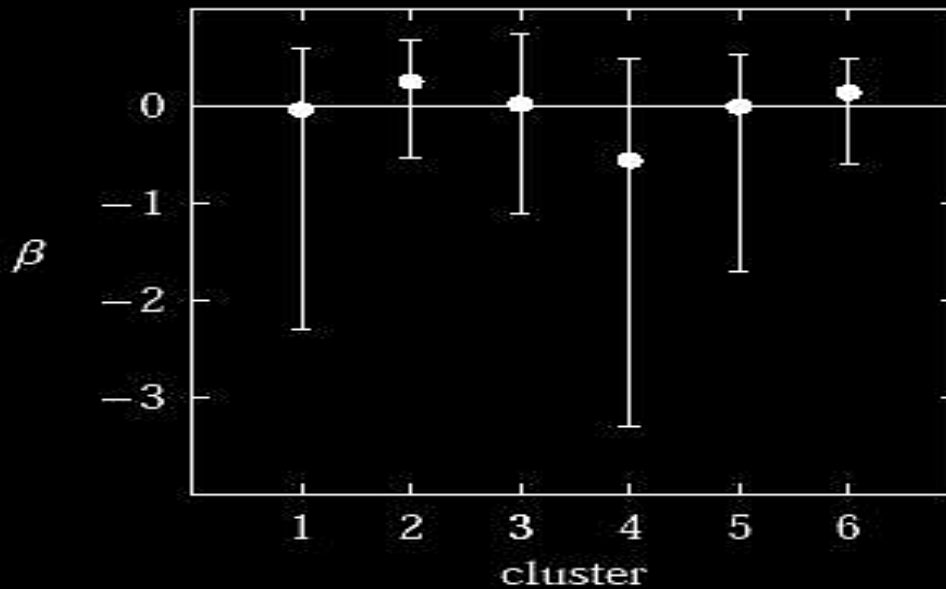
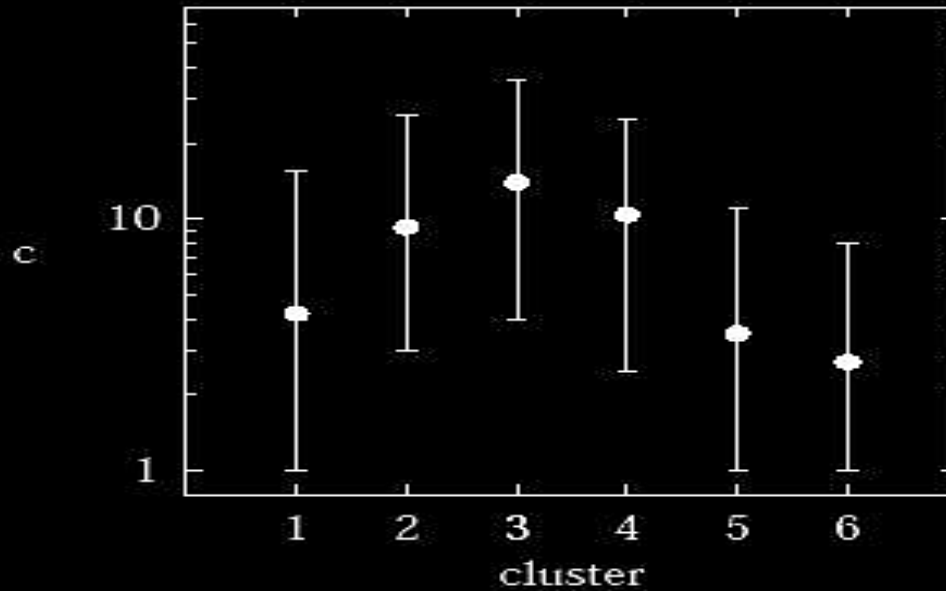
(B. & Salucci 06)



$$V_c(r) \equiv \sqrt{\frac{GM(r)}{r}}$$

# Individual clusters (Jeans)

(Lokas+06)



NFW  
concentration

Velocity  
constant  
anisotropy,  
 $\beta$

Cluster low- $z$   $M(r)$ : **NFW OK**

Cluster low- $z$   $M(r)$ : **NFW OK**

Core allowed, but  $r_c \sim$  size **BCG**

Cluster low- $z$   $M(r)$ : **NFW OK**

Core allowed, but  $r_c \sim$  **size BCG**

→ DM scattering cross section  **$< 2 \text{ cm}^2 \text{ g}^{-1}$**   
*(by cmp w. num. sims. Meneghetti+01)*

**$5 \text{ cm}^2 \text{ g}^{-1}$**  required on galaxy scales (Davé+00)



Cluster low- $z$   $M(r)$ : **NFW OK**

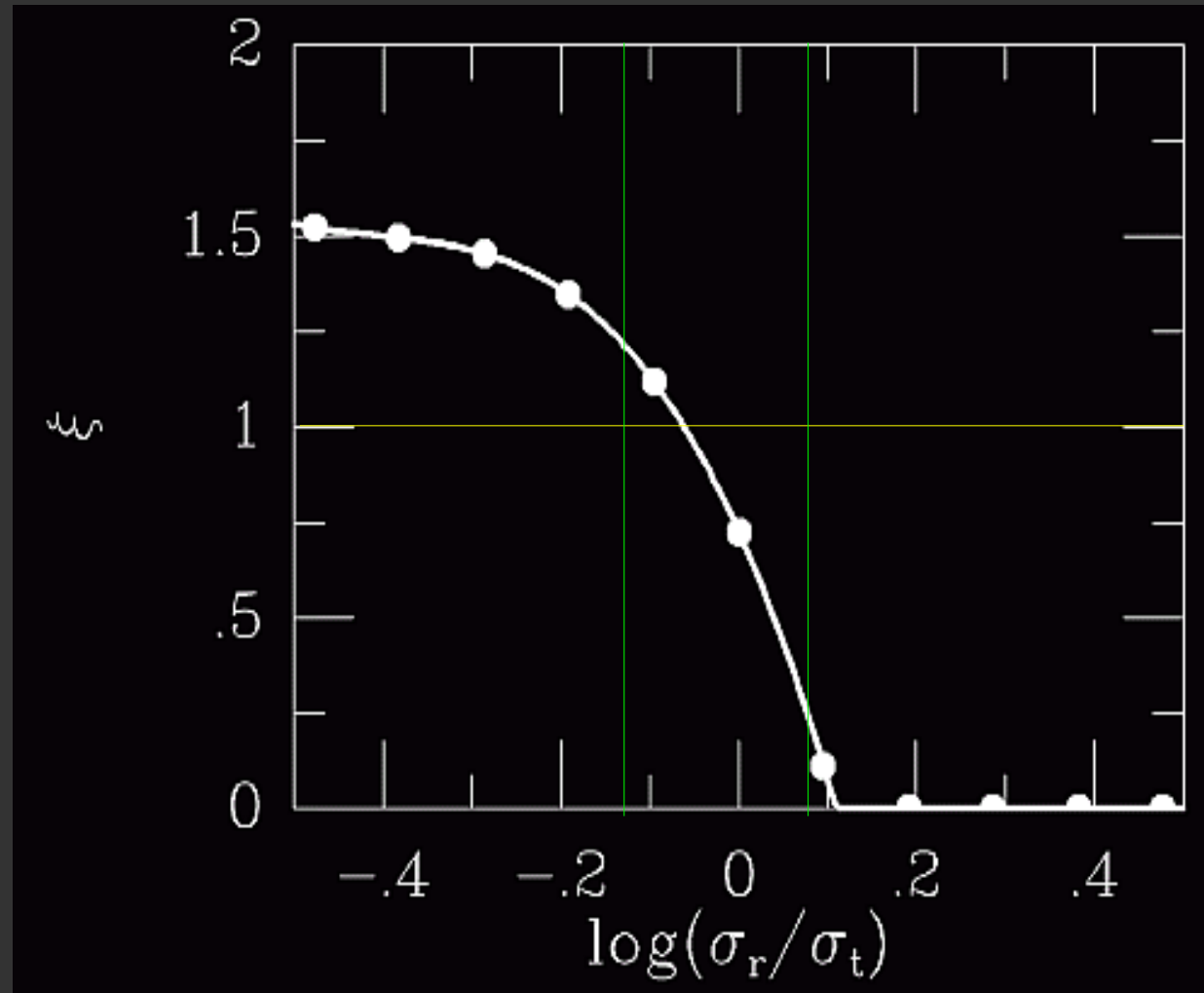
Core allowed, but  $r_c \sim$  **size BCG**

→ DM scattering cross section  **$< 2 \text{ cm}^2 \text{ g}^{-1}$**   
*(by cmp w. num. sims. Meneghetti+01)*

$5 \text{ cm}^2 \text{ g}^{-1}$  required on galaxy scales (Davé+00)

→ Dynamical friction not very effective  
*or counteracted by adiabatic contraction*  
(baryonic infall, Blumenthal+86)

# Cluster medium-z M(r): **NFW still OK**



(van der Marel+00)

# Group M(r): controversial results

Hernquist (Mahdavi+99)

Power-law (Mahdavi & Geller 04)

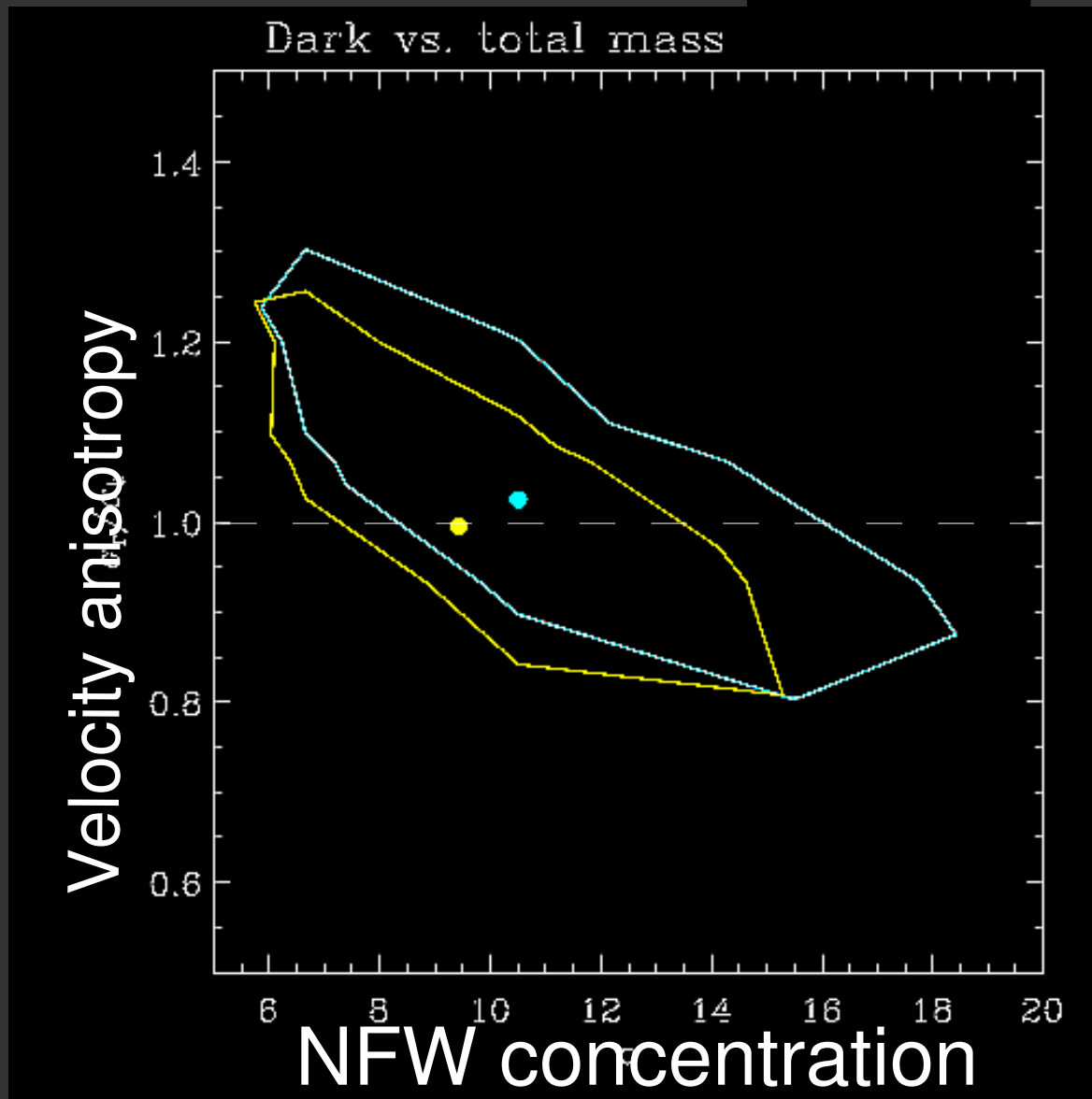
Core (Carlberg+01)

**Not all groups are virialized systems**

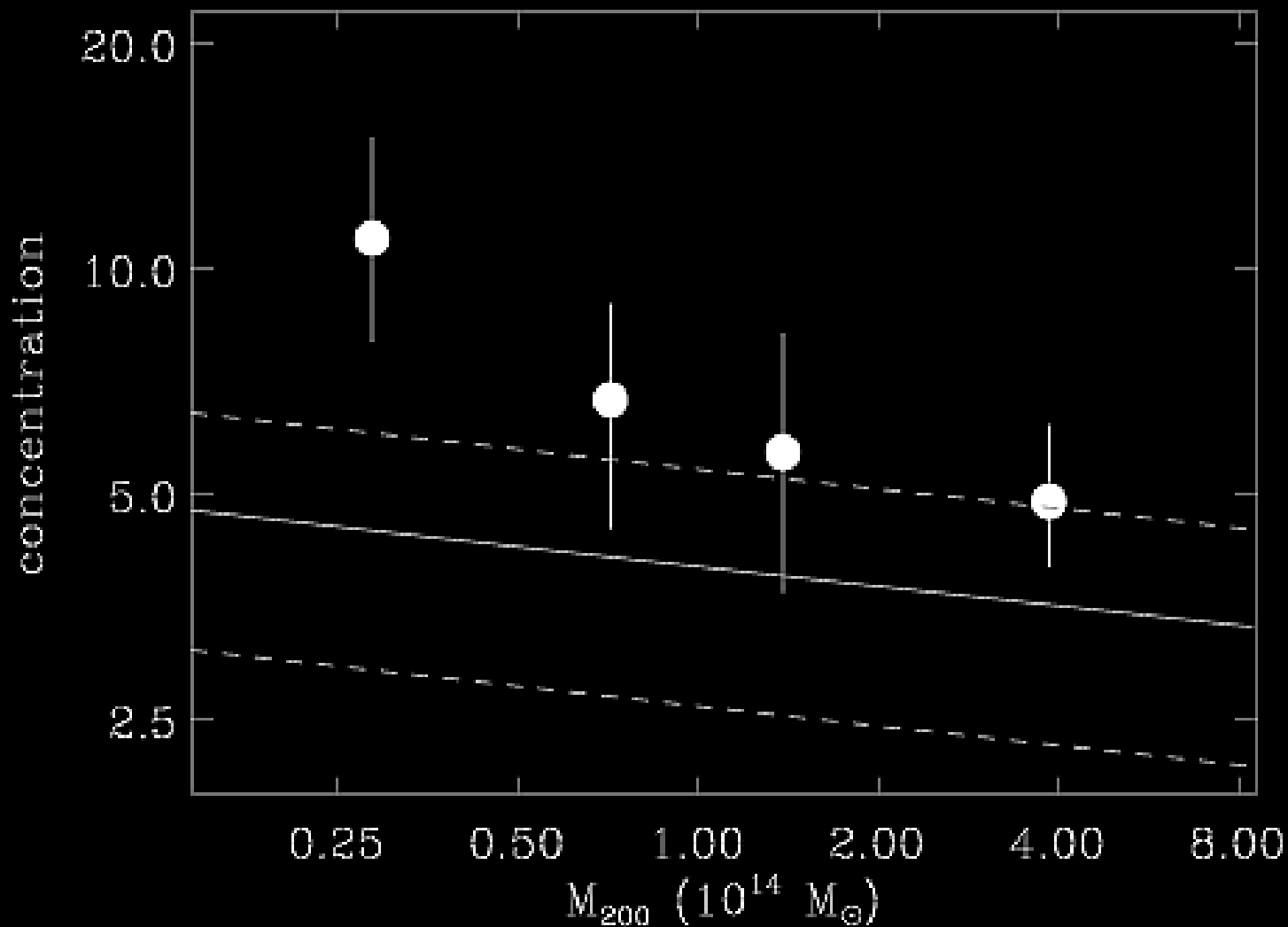
*Different samples → different results*

# GEMS: X-ray luminous groups (more likely to be in a virialized state)

(B., Mamon, Ponman, in prep.)



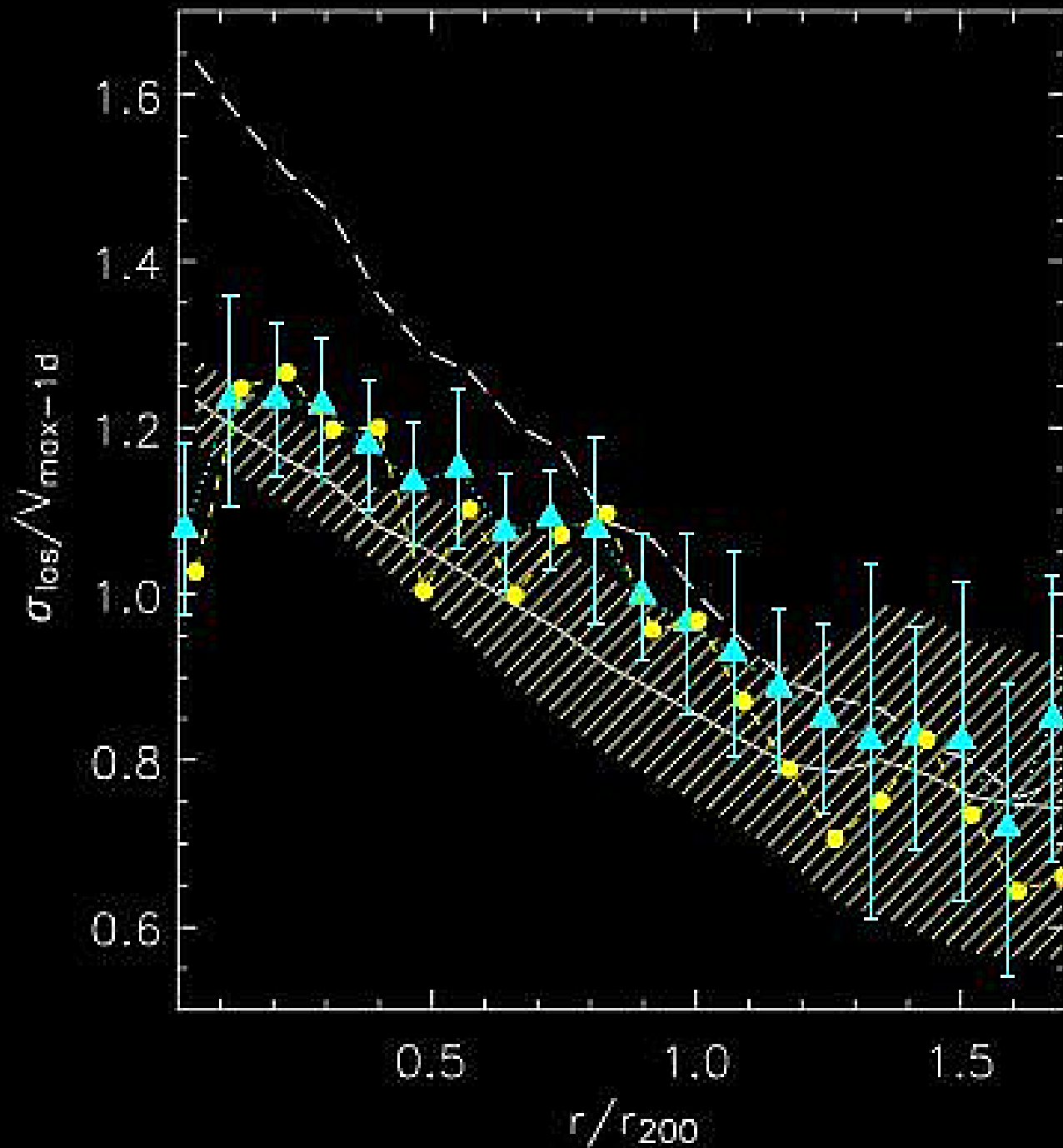
# NFW c vs. M



Model from  
Duffy+08

4 samples: B.+09, Mahdavi+99, B. & Girardi 03, B. & Salucci 06

# The relative distribution of dark and baryonic matter



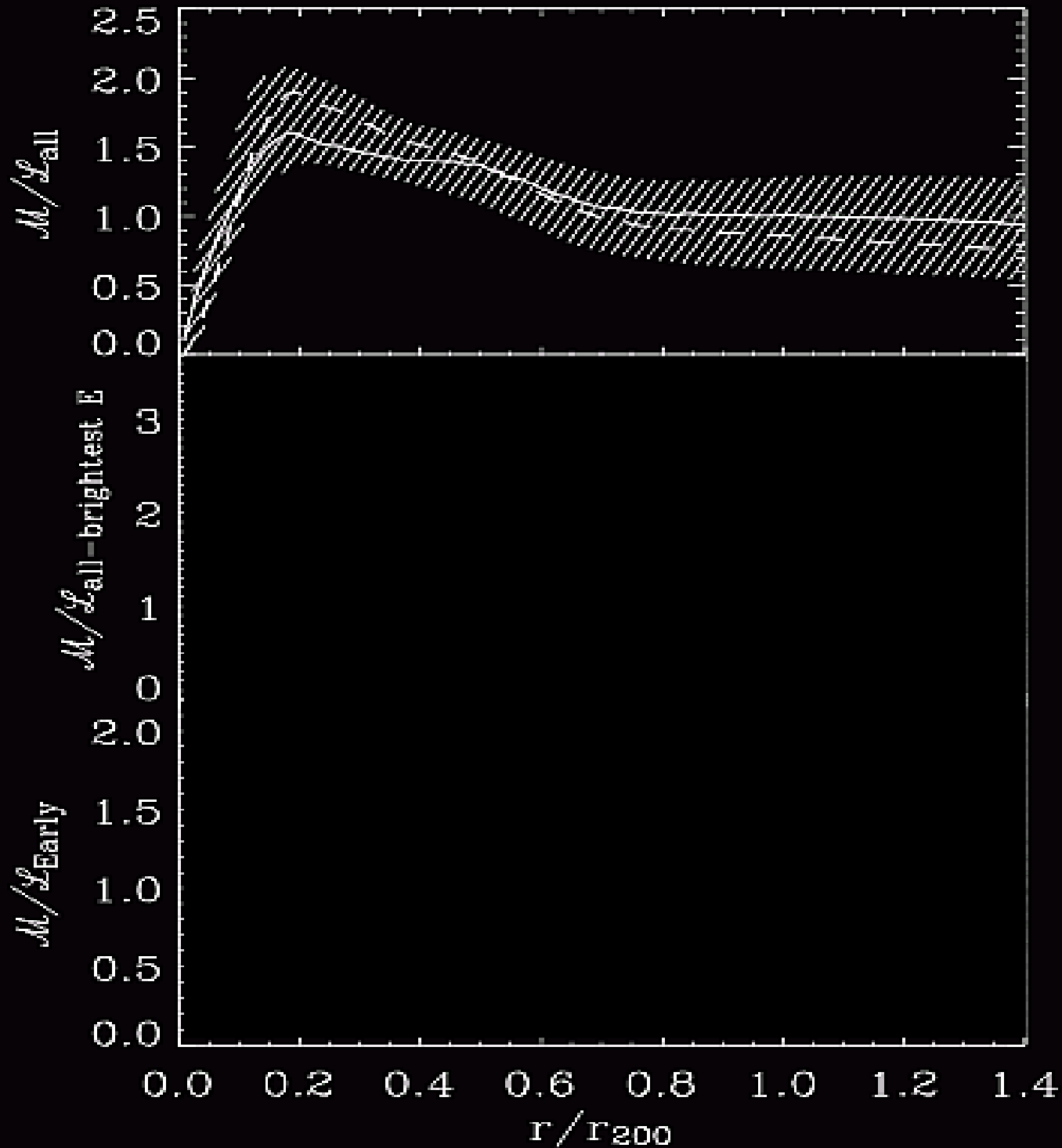
Theoretical  
expectation

(Gao+04)

velocity  
dispersion  
profiles  
of subhalos  
vs. galaxies  
vs. DM

# ENACS

(Katgert+04)

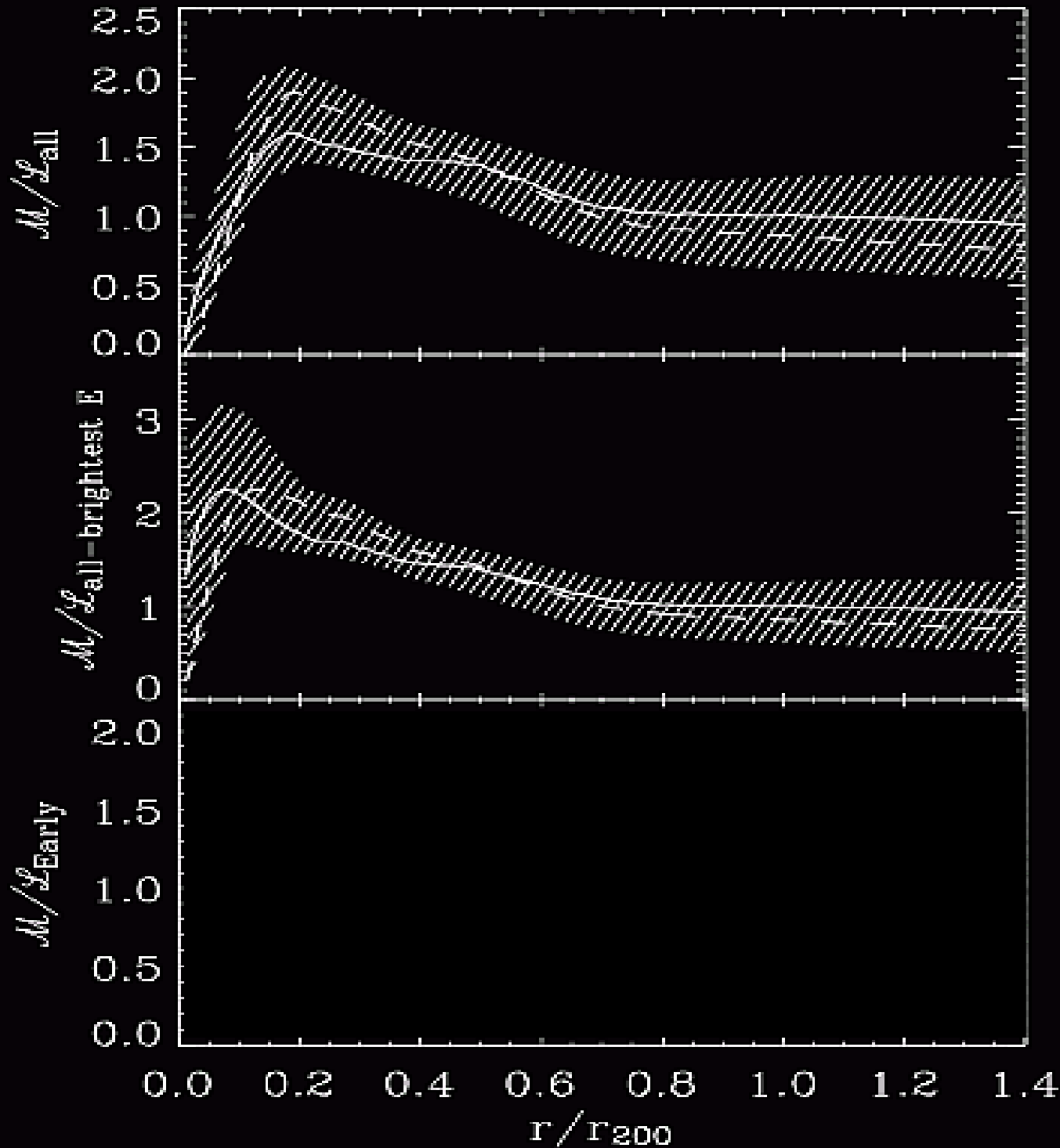


Mass density  
divided by  
Luminosity  
density  
vs. distance  
from cluster  
center



# ENACS

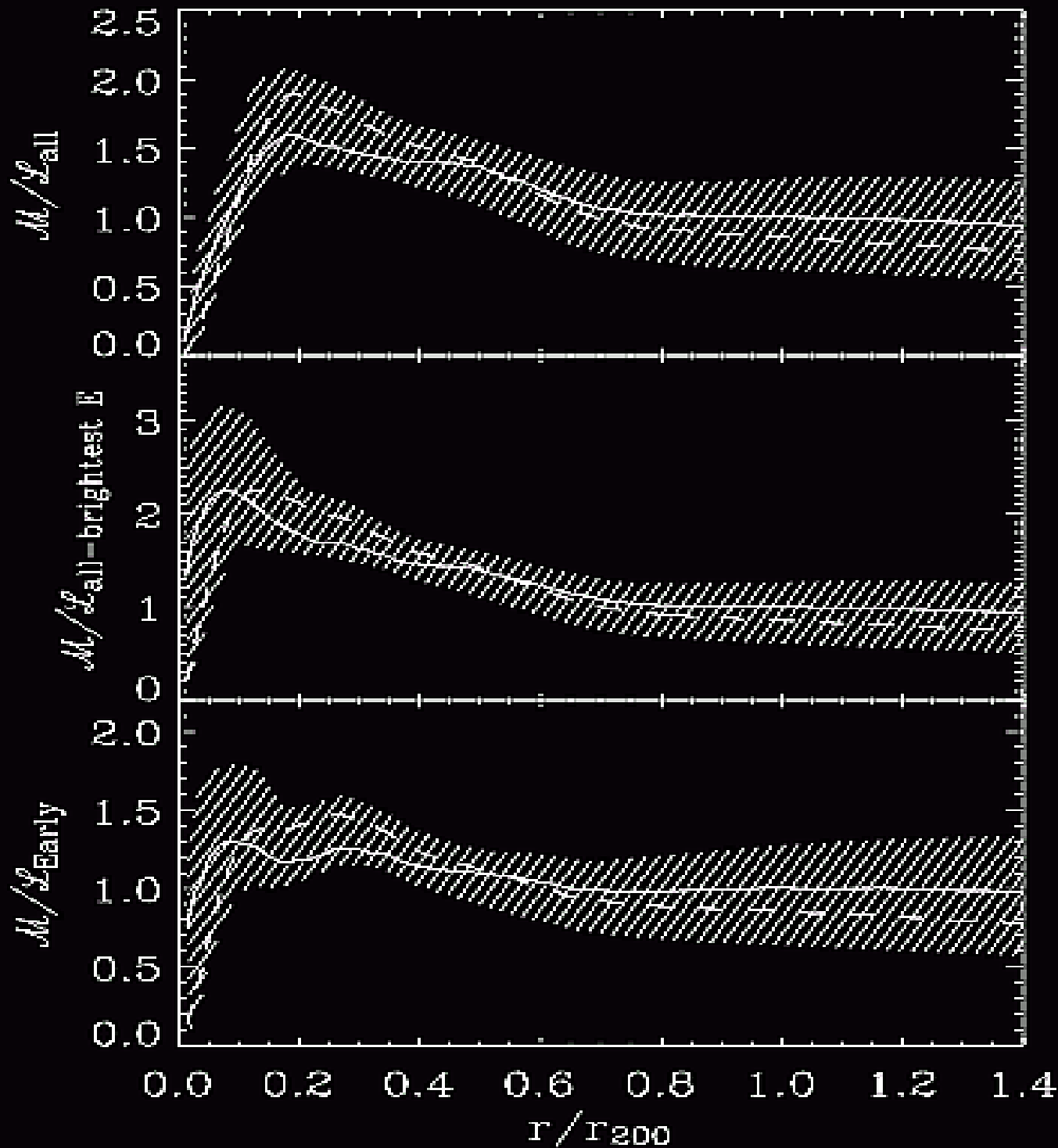
(Katgert+04)



Mass density  
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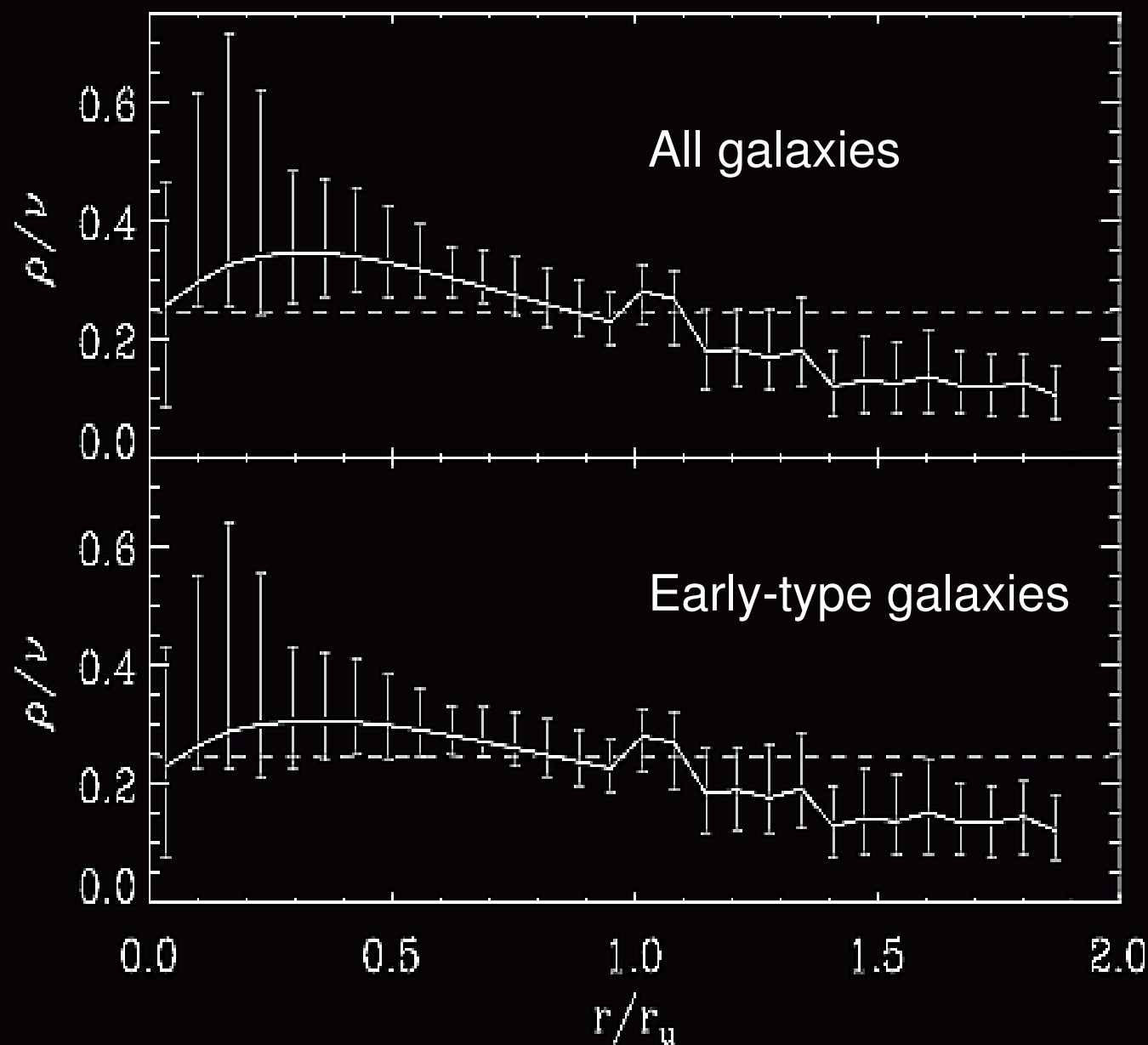


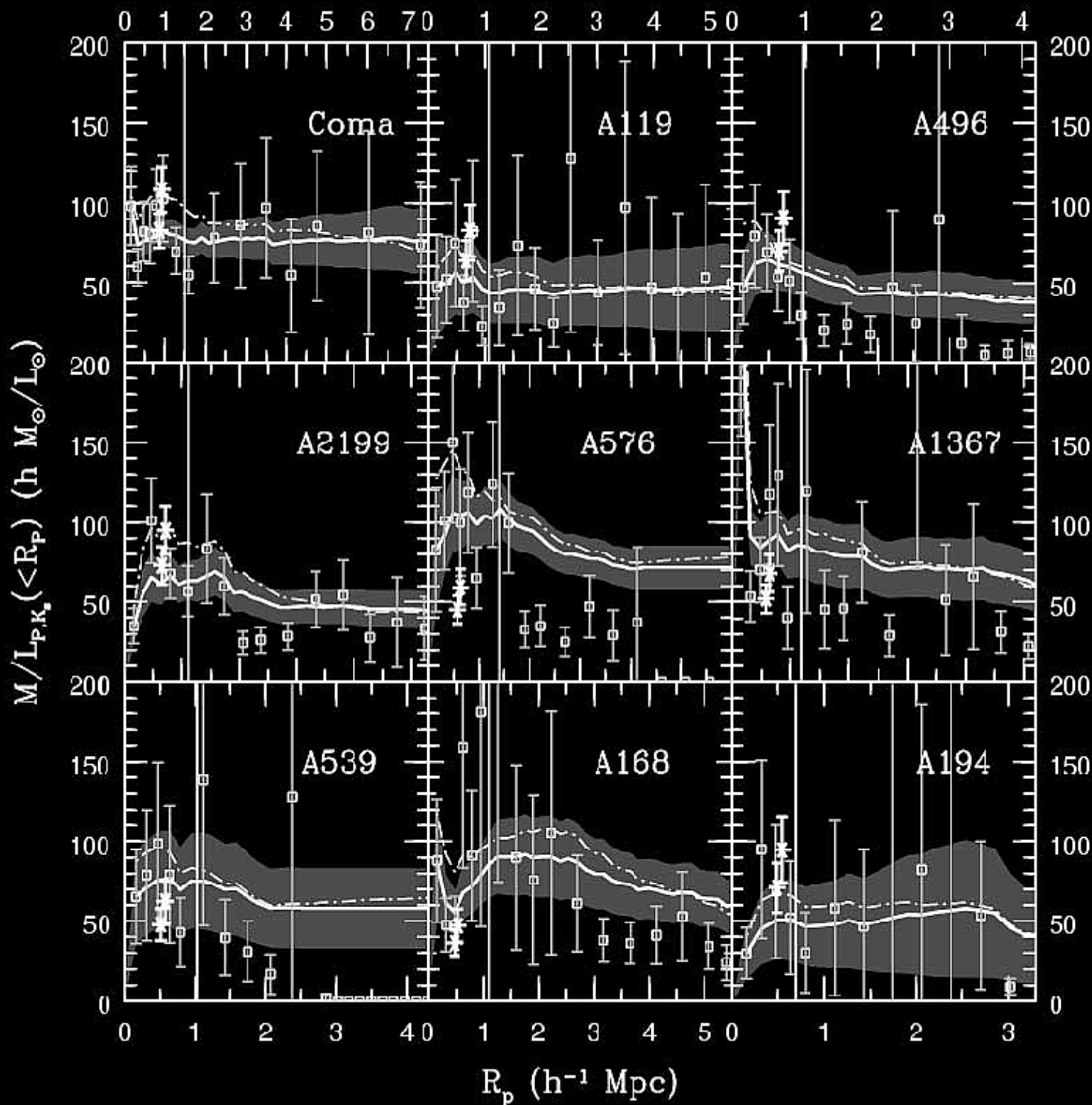
Mass density  
divided by  
Luminosity  
density  
vs. distance  
from cluster  
center

## 2dFGRS

(B. &  
Girardi 03)

Mass density  
divided by  
Number  
density  
vs. distance  
from cluster  
center





**CAIRNS**

(Rines+04)

$M(<r)$

divided by

K-band  $L(<R)$

vs. distance

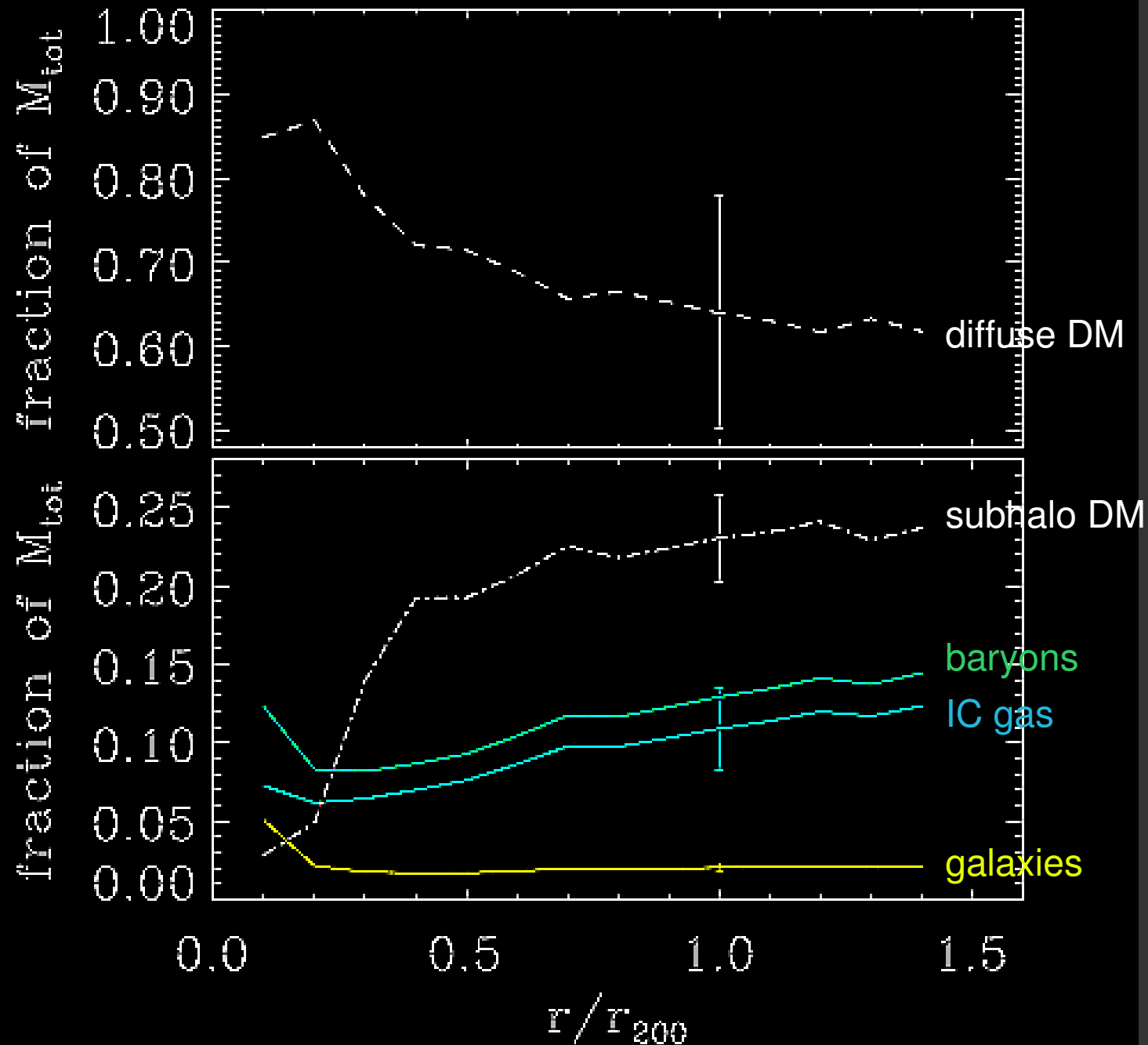
from cluster

center

# ENACS

(B.  
& Salucci 06)

The mass  
budget in  
clusters of  
galaxies

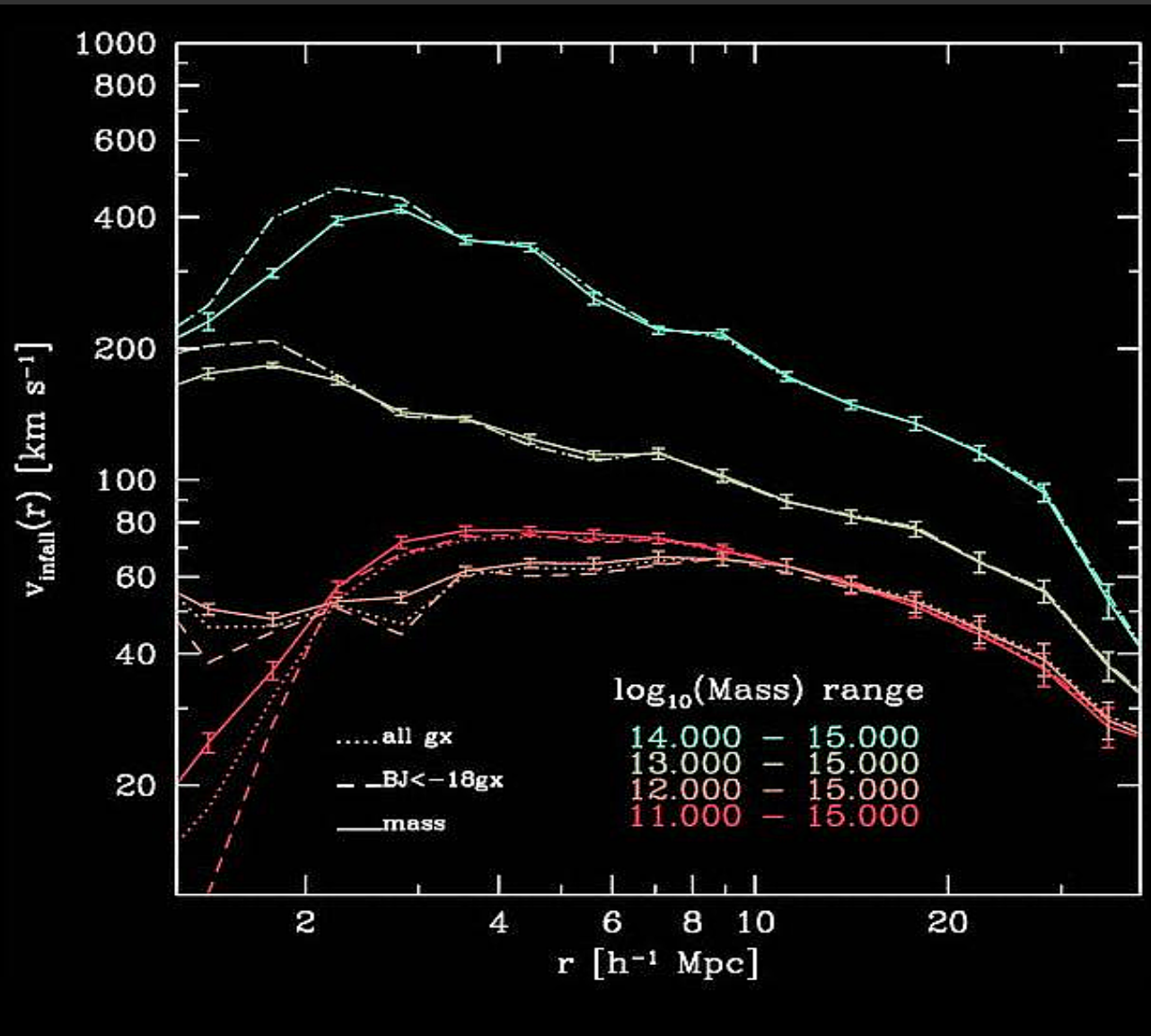


# Mass accretion

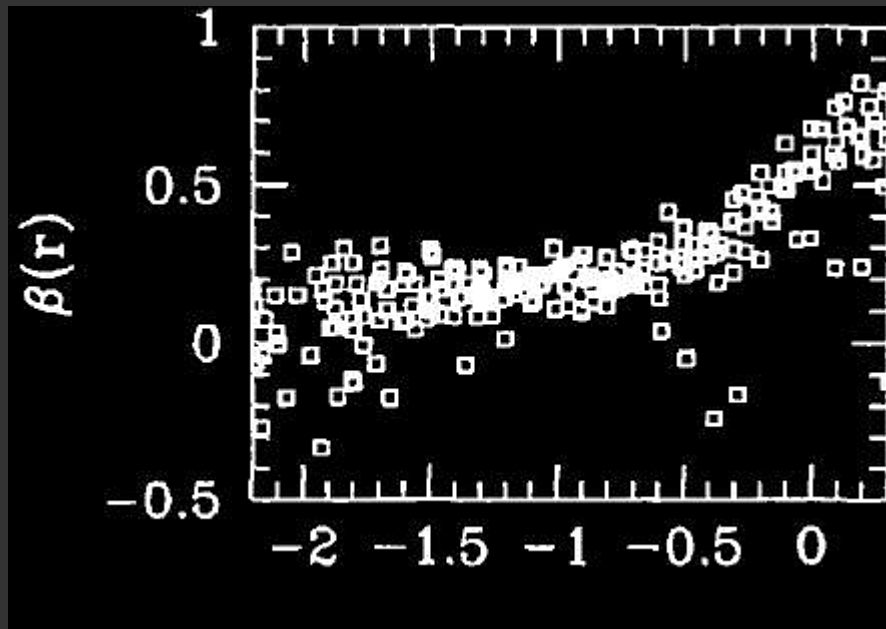
# Direct test of hierarchical clustering: evidence for infall?

Theoretical  
predictions

(Ceccarelli+05)



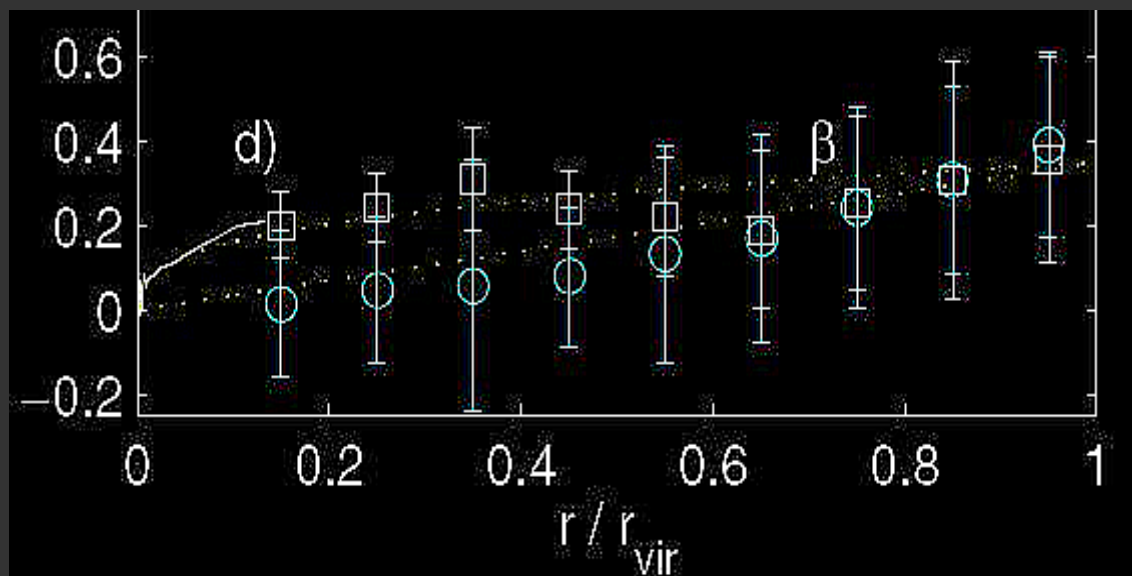
# Direct test of hierarchical clustering: evidence for infall?



Theoretical  
predictions

(Tormen+97)

(Diemand+04)

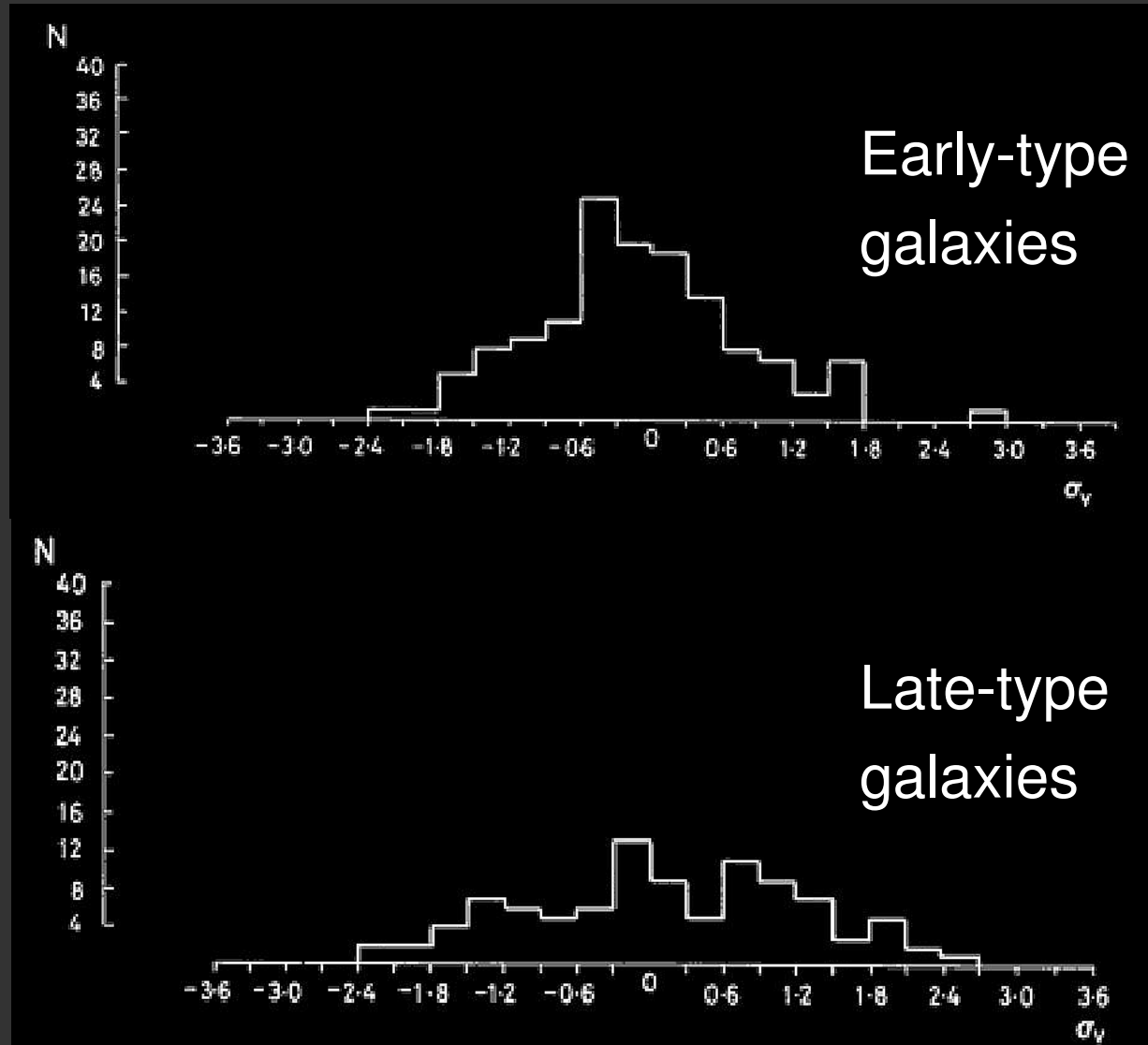


$$\beta(r) \equiv 1 - \frac{\langle V_t^2 \rangle(r)}{\langle V_I^2 \rangle(r)}$$



# Early- and Late-type gals: different distributions

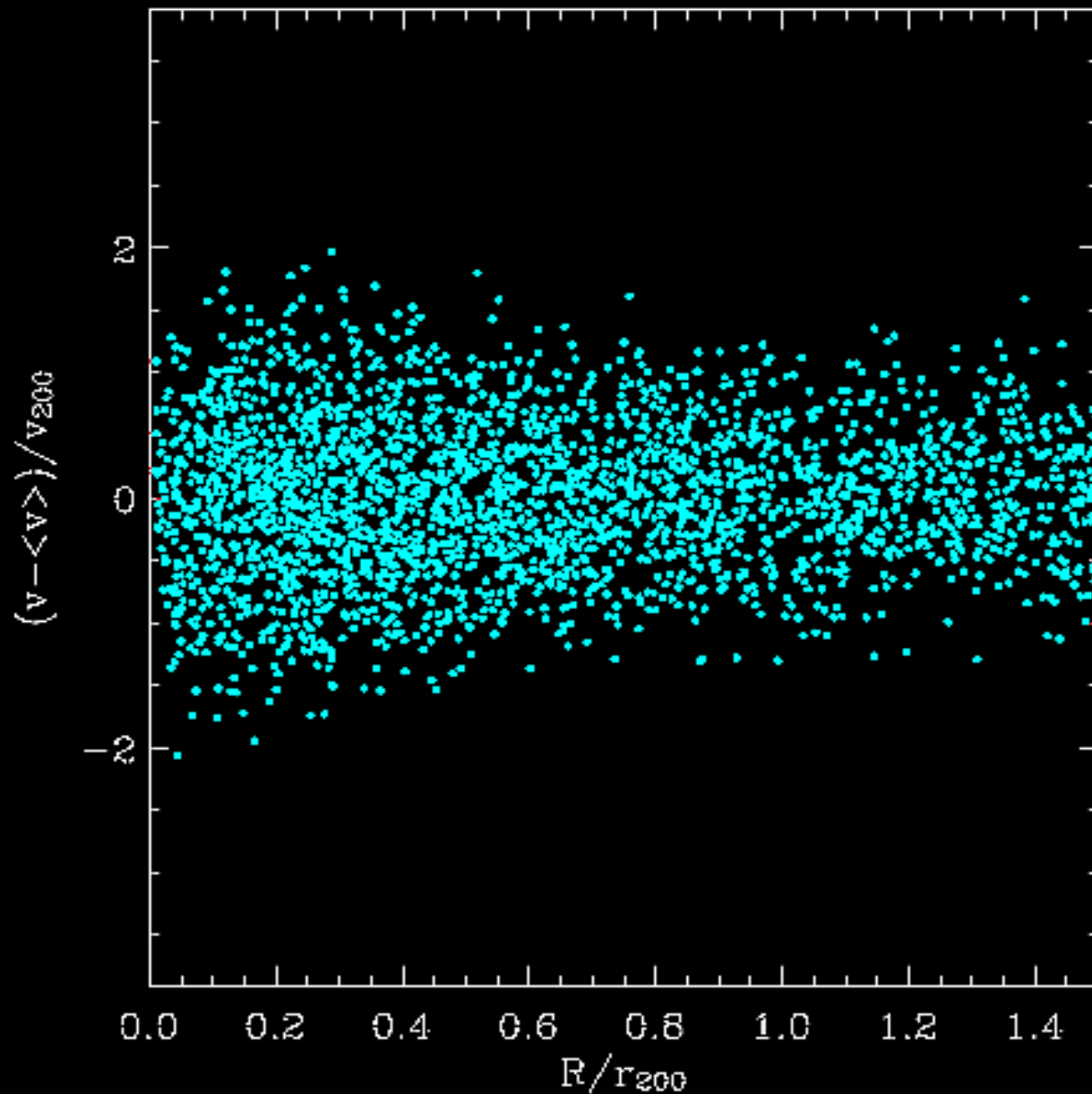
(Moss & Dickens 77)



Velocity wrt cluster mean

# Early- and Late-type gals: different distributions

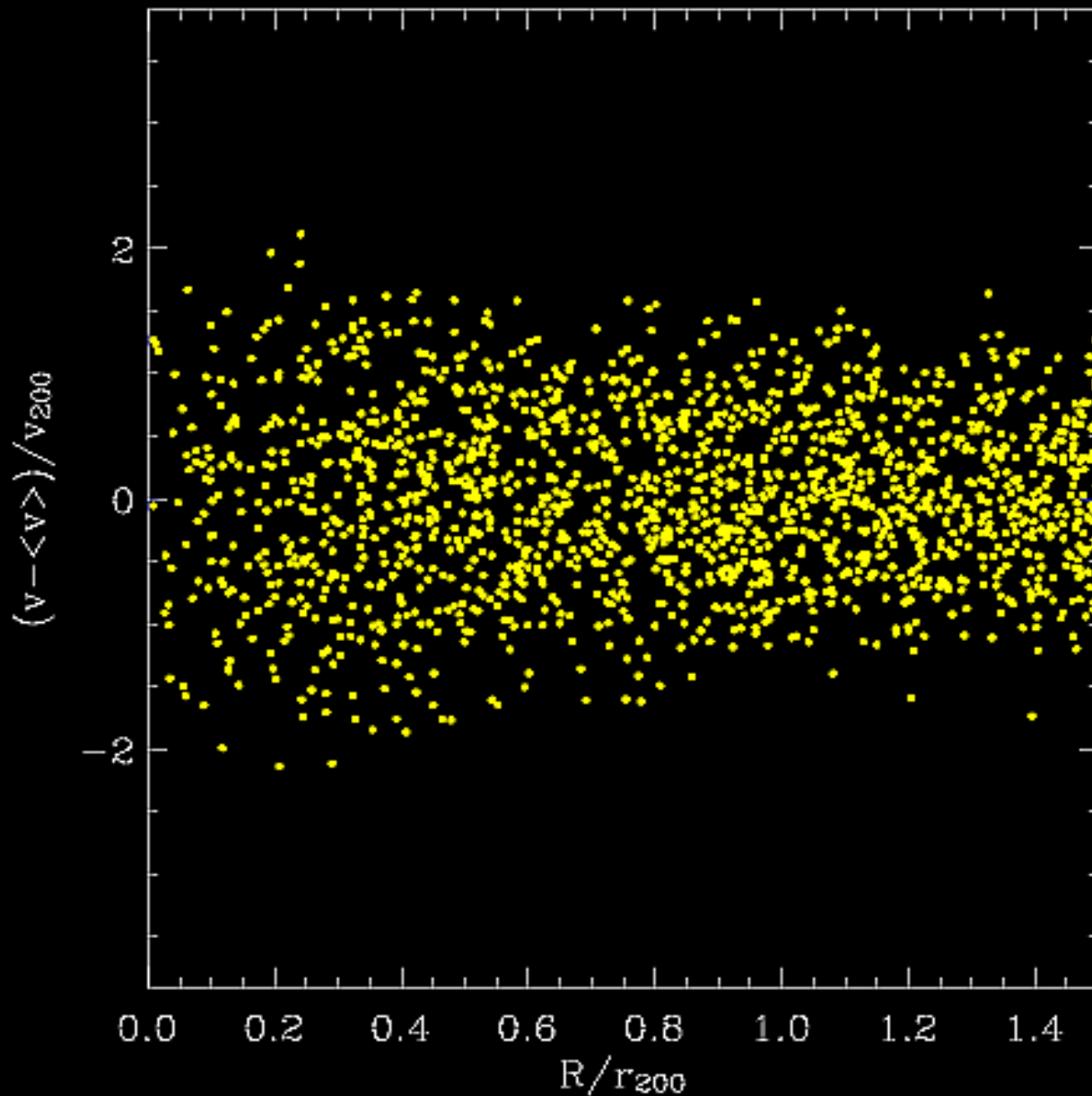
(CIRS; B., Diaferio, Rines, in prep)



Early-type  
galaxies

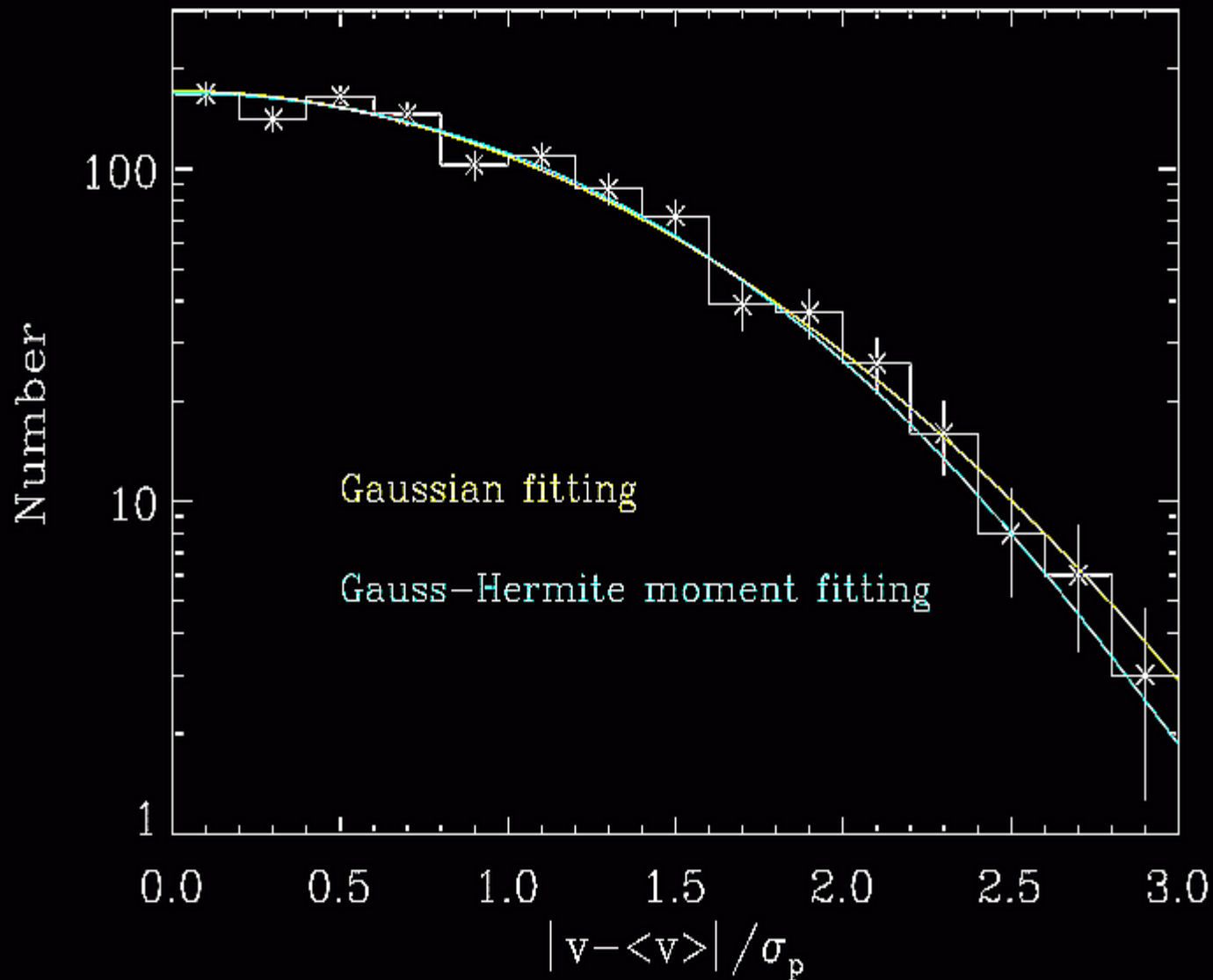
# Early- and Late-type gals: different distributions

(CIRS; B., Diaferio, Rines, in prep)



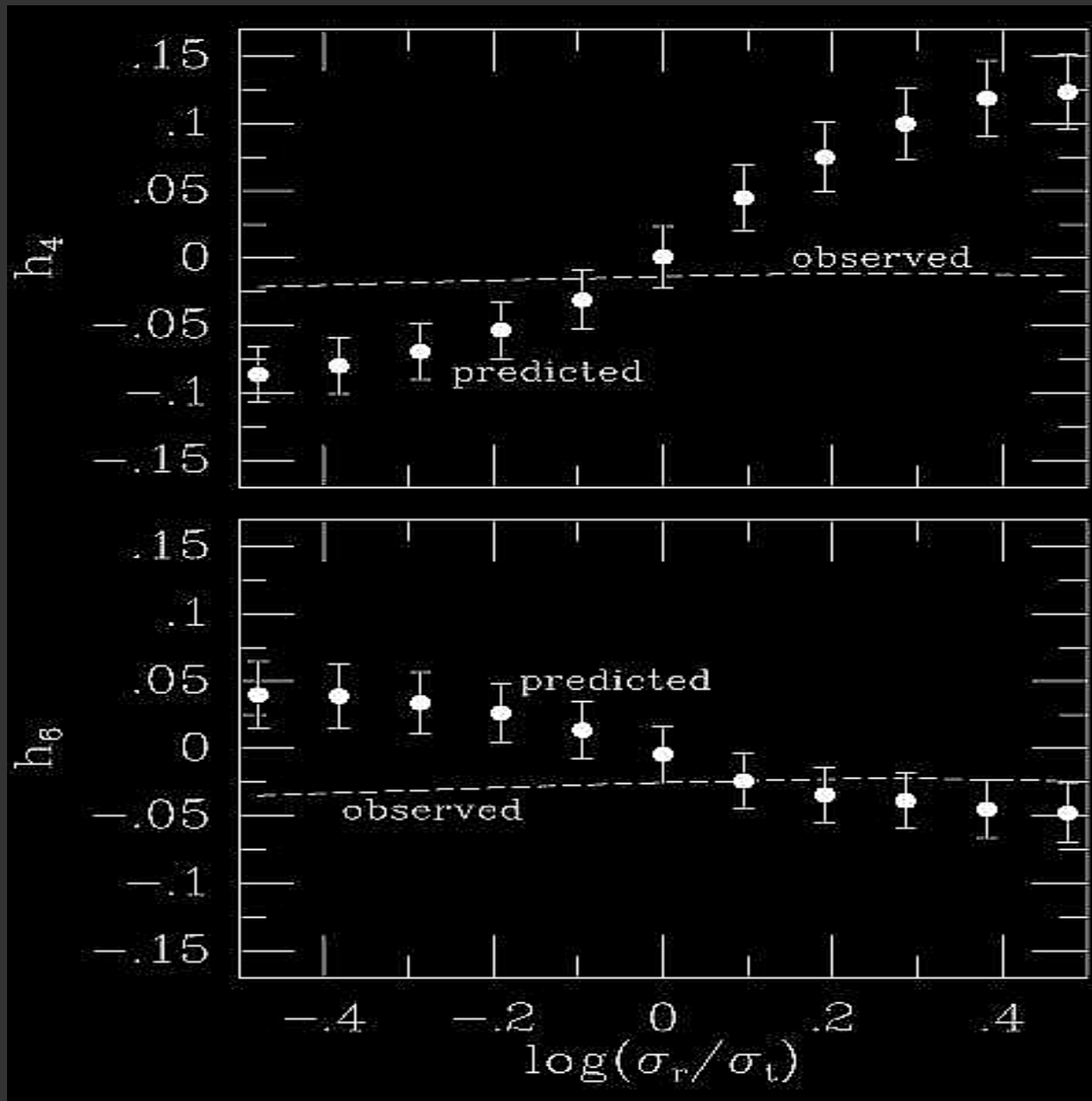
Late-type  
galaxies

# Early-type gals: $\sim$ isotropic orbits, $\beta \approx 0$



ENACS  
(Katgert+04)

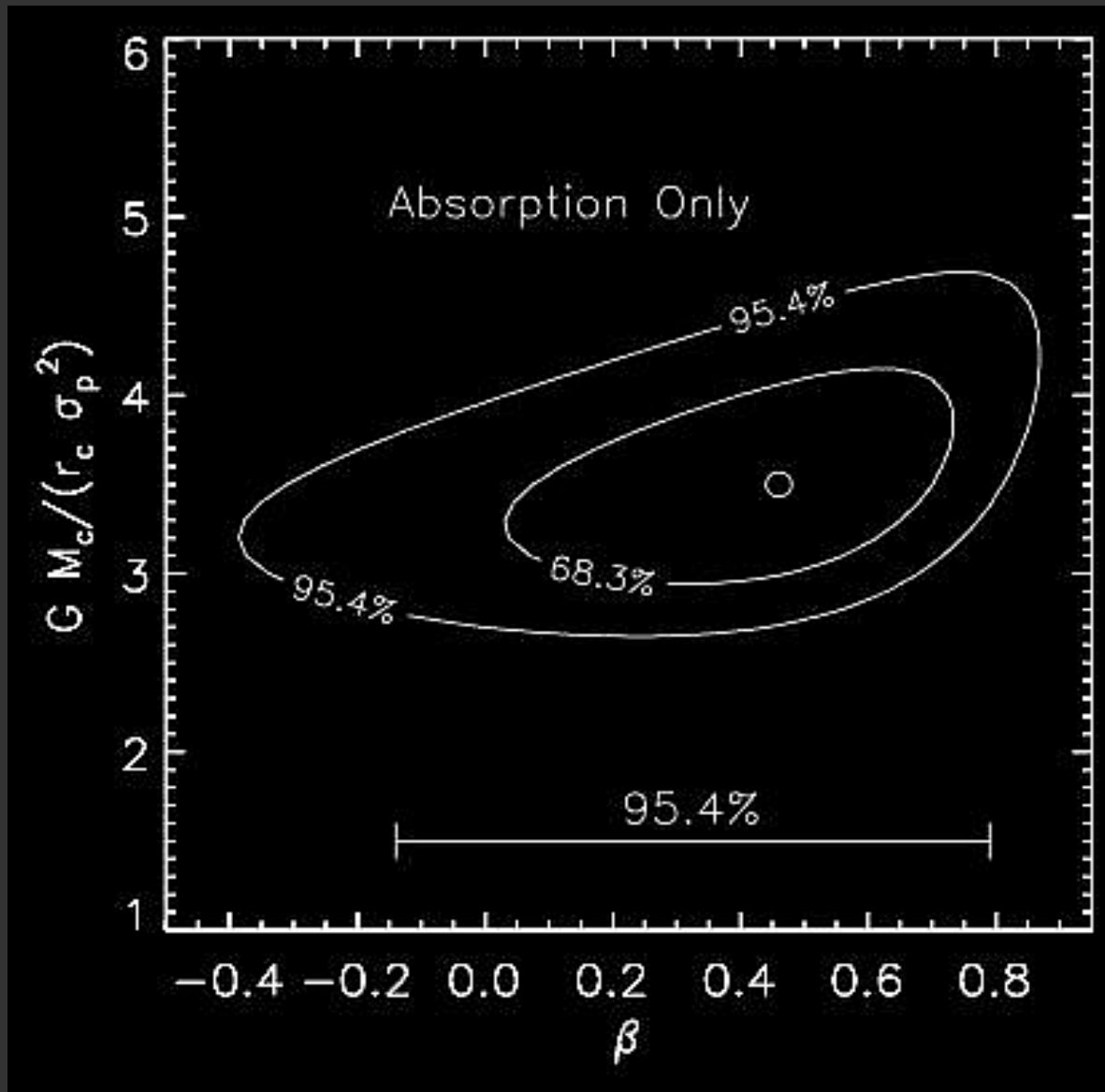
# Early-type gals: $\sim$ isotropic orbits, $\beta \approx 0$



CNOC

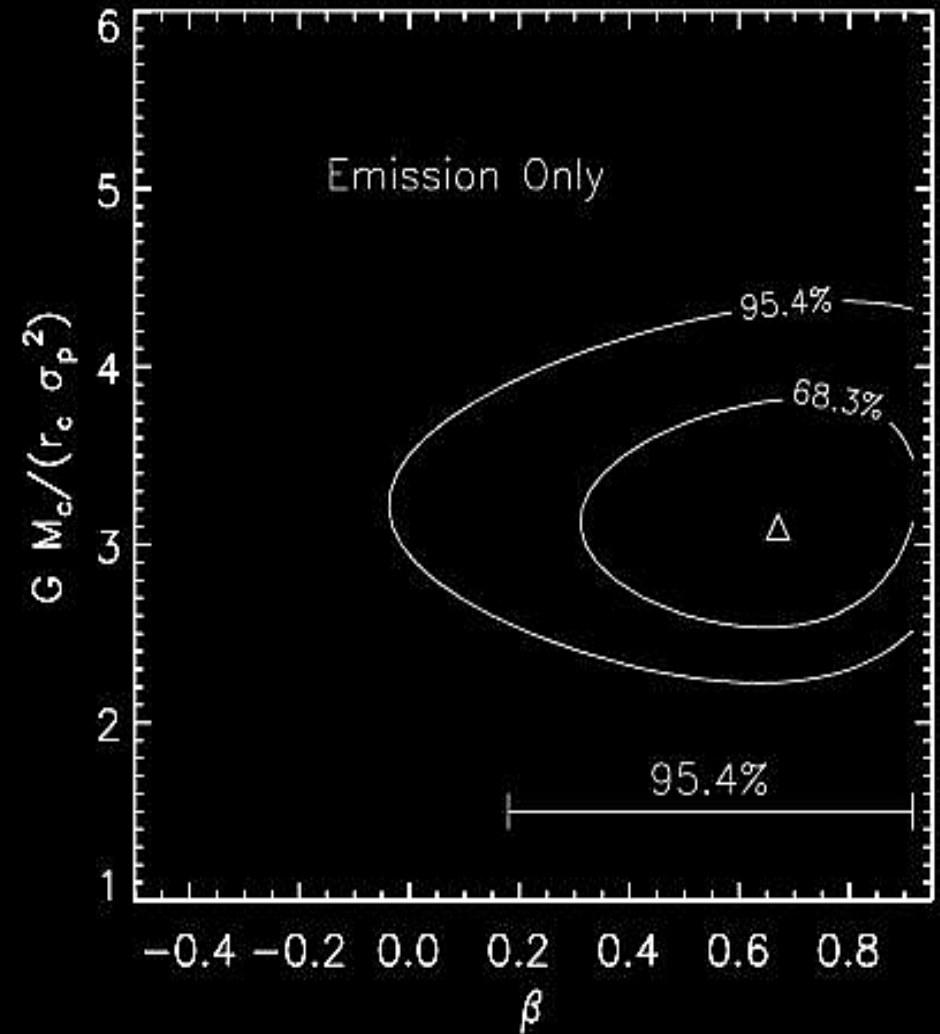
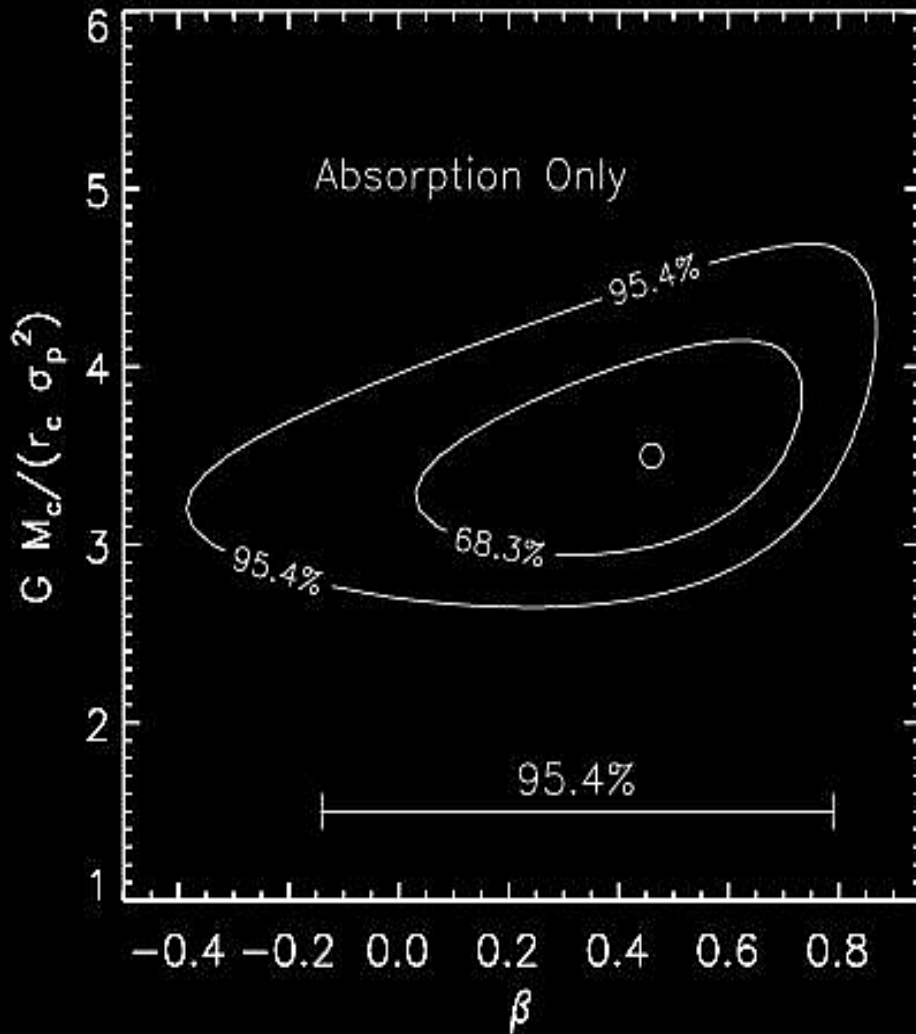
(van der Marel+00)

Early-type gals:  $\sim$ isotropic orbits,  $\beta \approx 0$



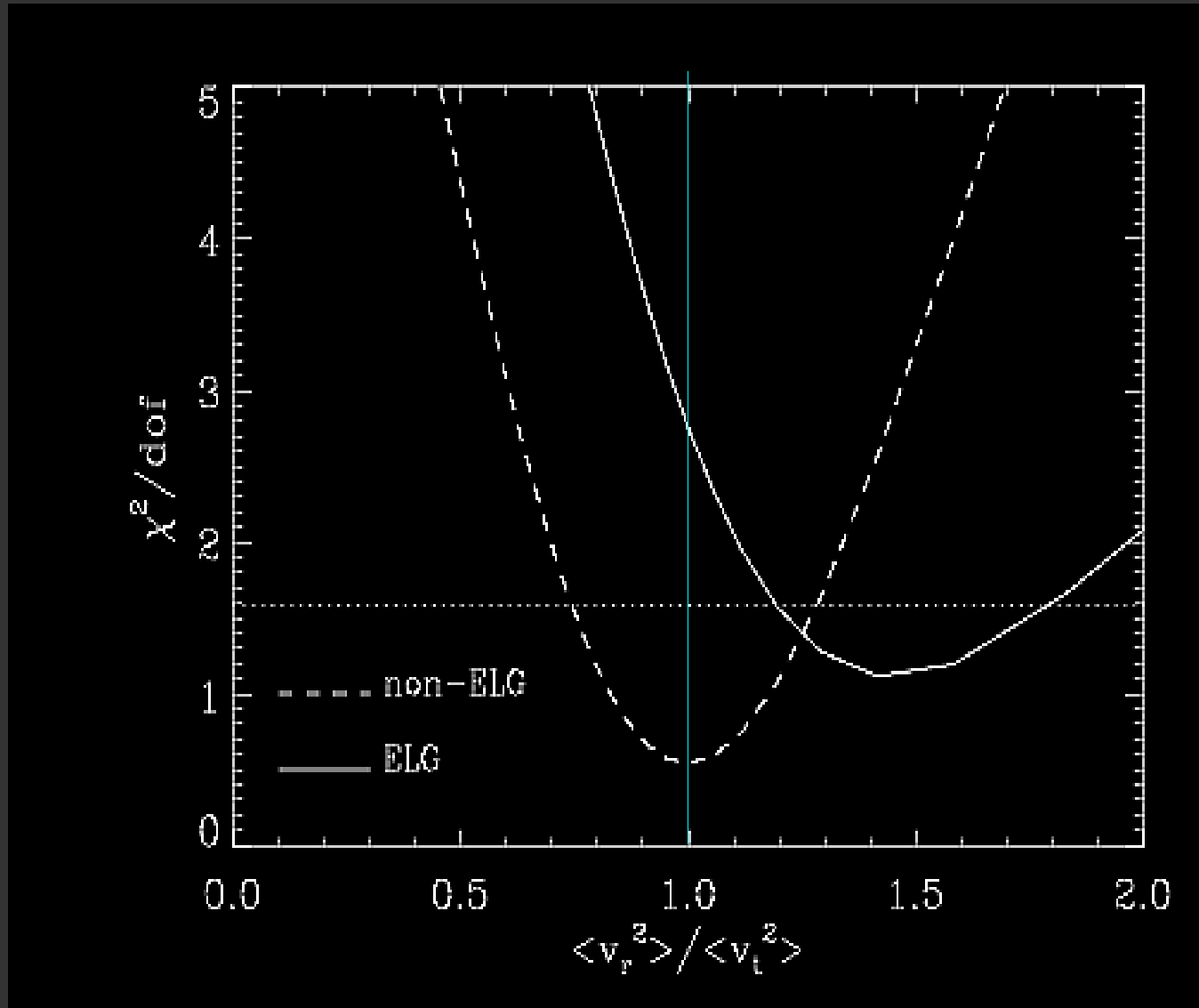
Poor clusters  
(Mahdavi+99)

# Late-type gals: mildy radial orbits, $\beta > 0$



Poor clusters (Mahdavi+99)

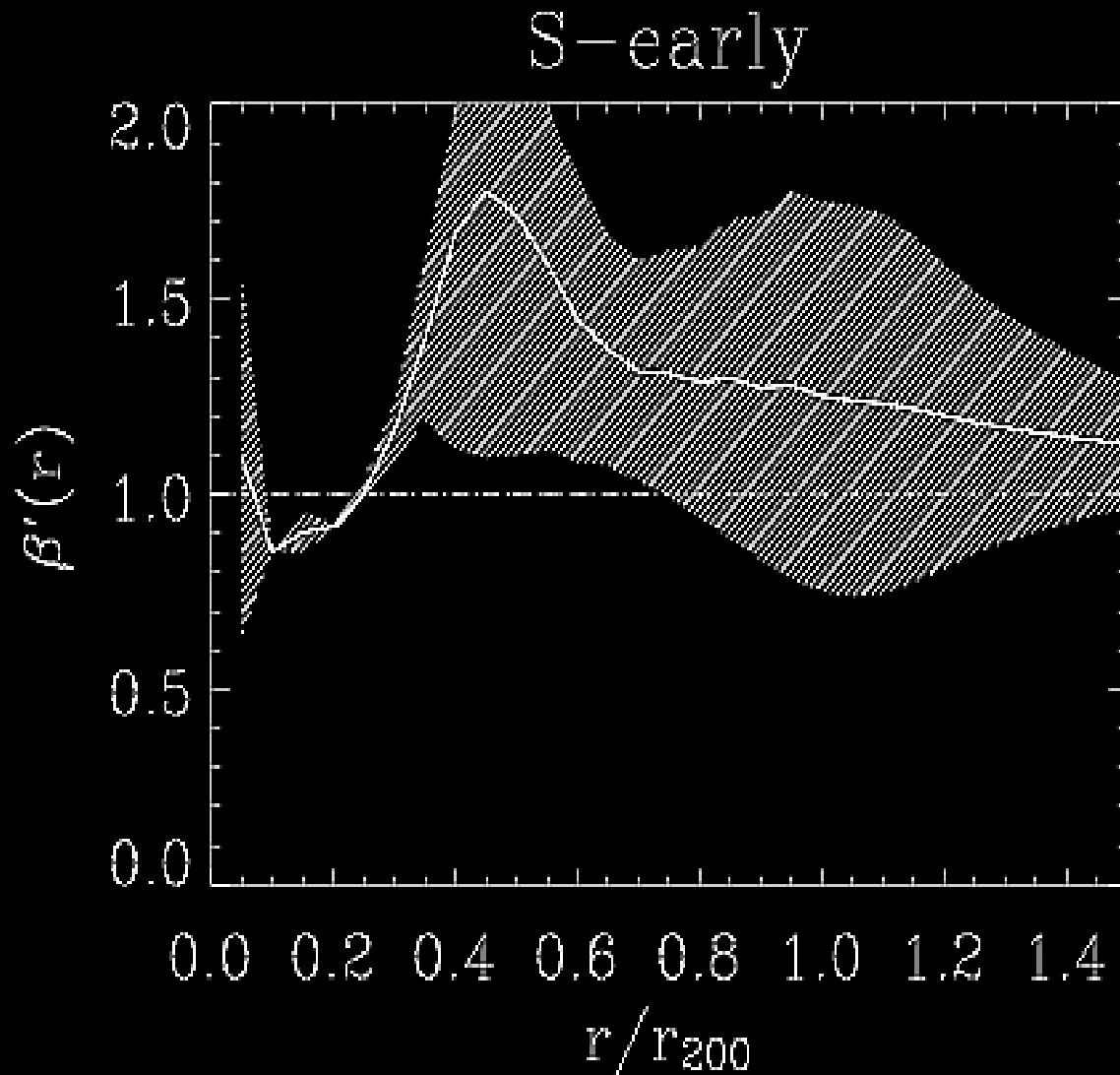
# Late-type gals: mildy radial orbits, $\beta > 0$



ENACS  
(B. 01)



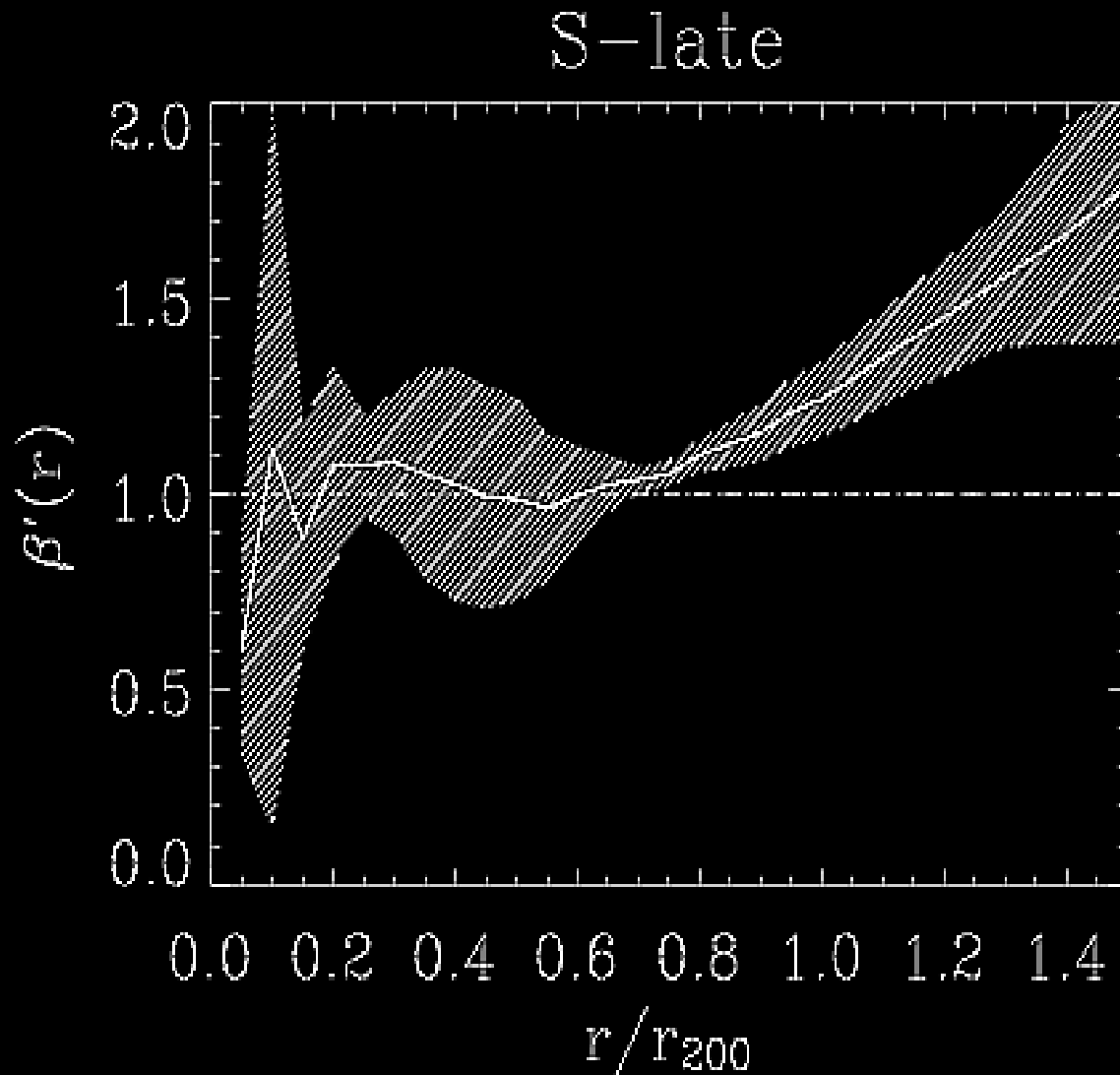
# Late-type gals: $\beta \approx 0$ for Sa $\rightarrow$ Sb



ENACS  
(B. &  
Katgert 04)

$$\beta'(r) = \left( \frac{\langle v_r^2 \rangle}{\langle v_t^2 \rangle} \right)^{1/2}$$

# Late-type gals: $\beta > 0$ at large $r$ for Sbc $\rightarrow$ Irr

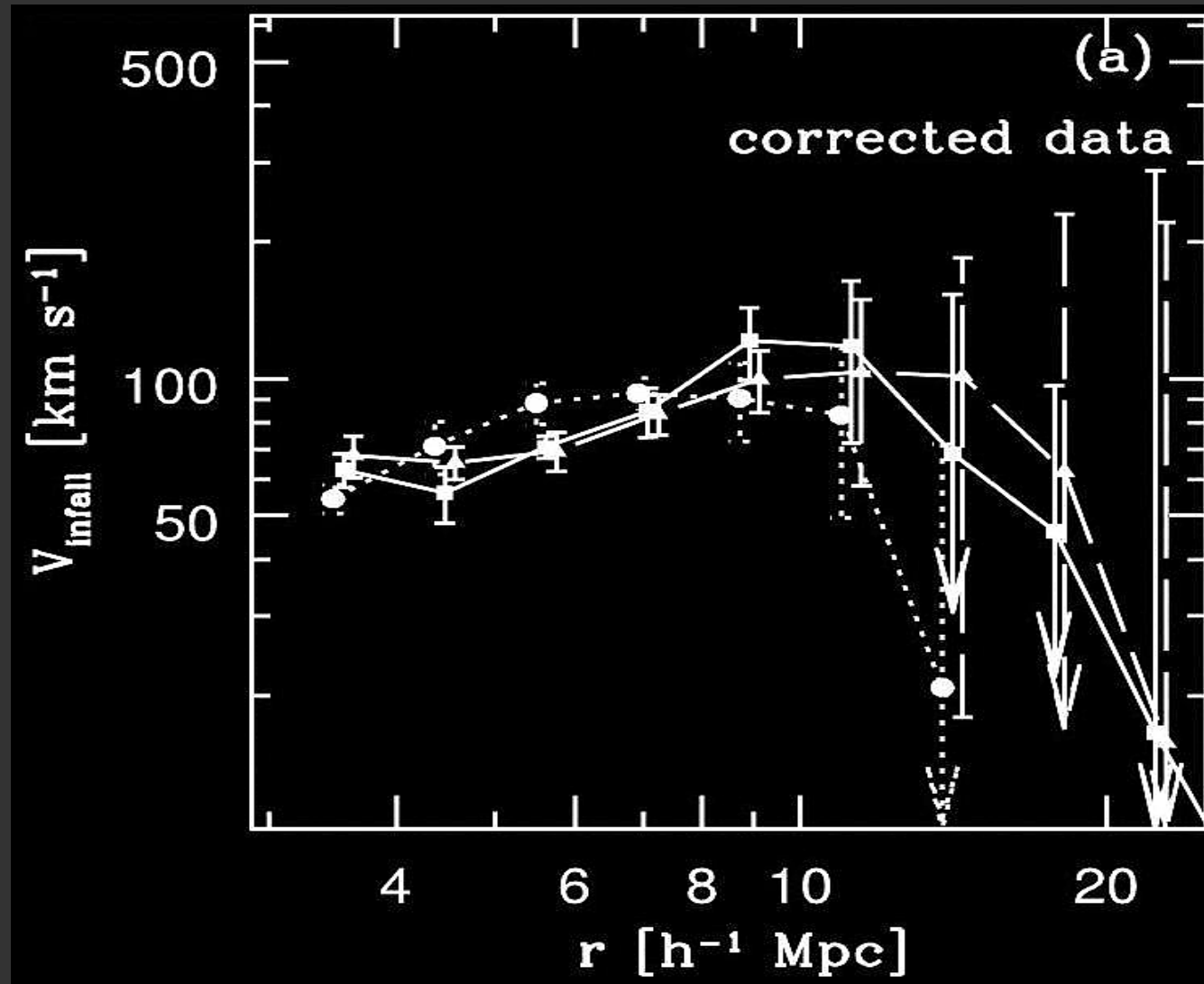


ENACS  
(B. &  
Katgert 04)

$$\beta'(r) = \left( \frac{\langle v_r^2 \rangle}{\langle v_t^2 \rangle} \right)^{1/2}$$

# Direct evidence of Spiral infall into clusters

## I.o.s. velocities vs. Tully-Fisher distances



(Ceccarelli+05)

Estimates of  $dM/dt$  from  $M(r>r_{200})$ :

$dM/dt \approx 0.06 M_{200}/\text{Gyr}$  (Rines & Diaferio 06)

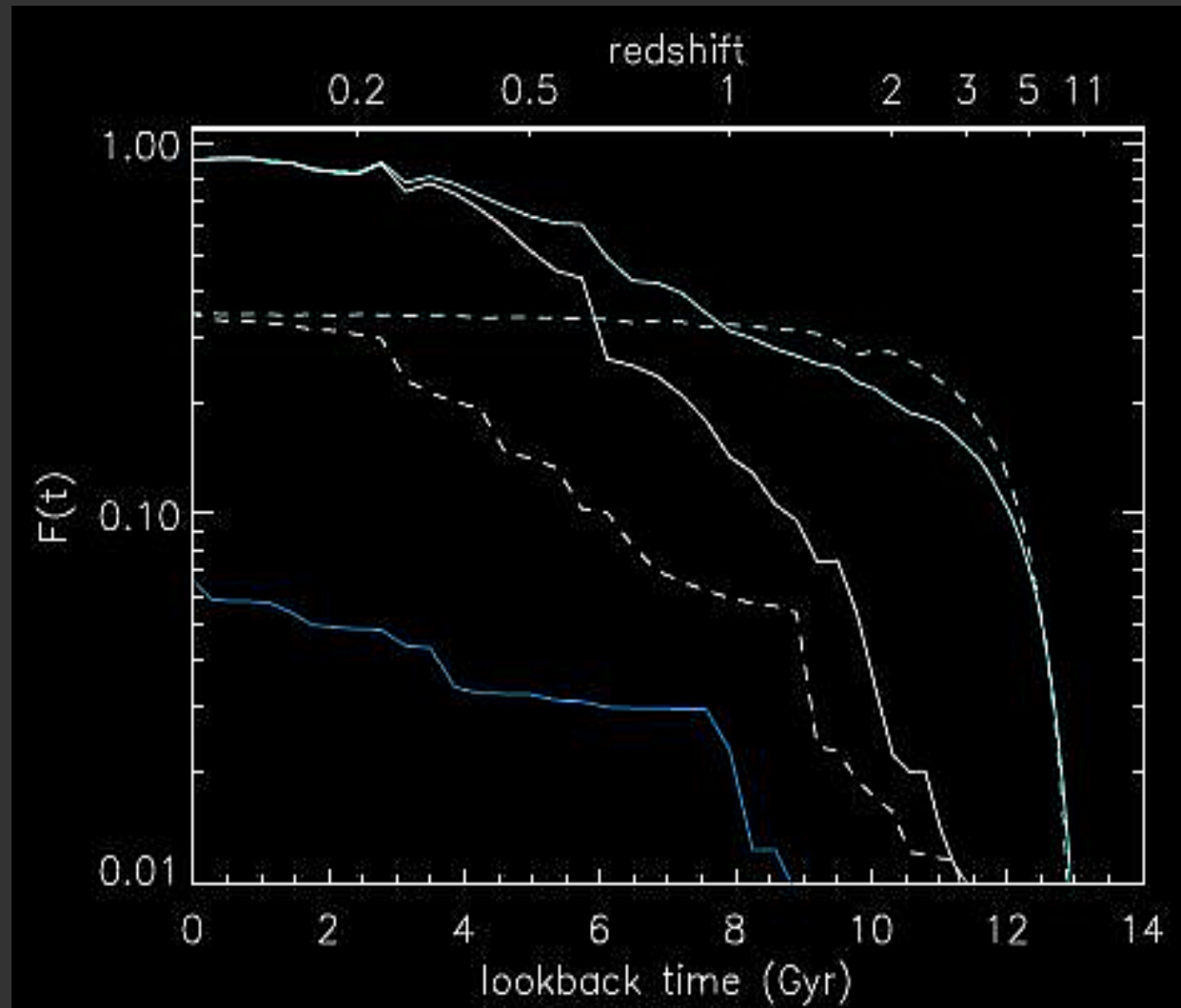
$\approx 0.02-0.11 M_{200}/\text{Gyr}$  (Adami+05)

If late-type gals are infalling population, their decreasing number density with time  $\Rightarrow$  also

$dM/dt$  decreases with time (x2 from  $z=0.45$  to 0.20)

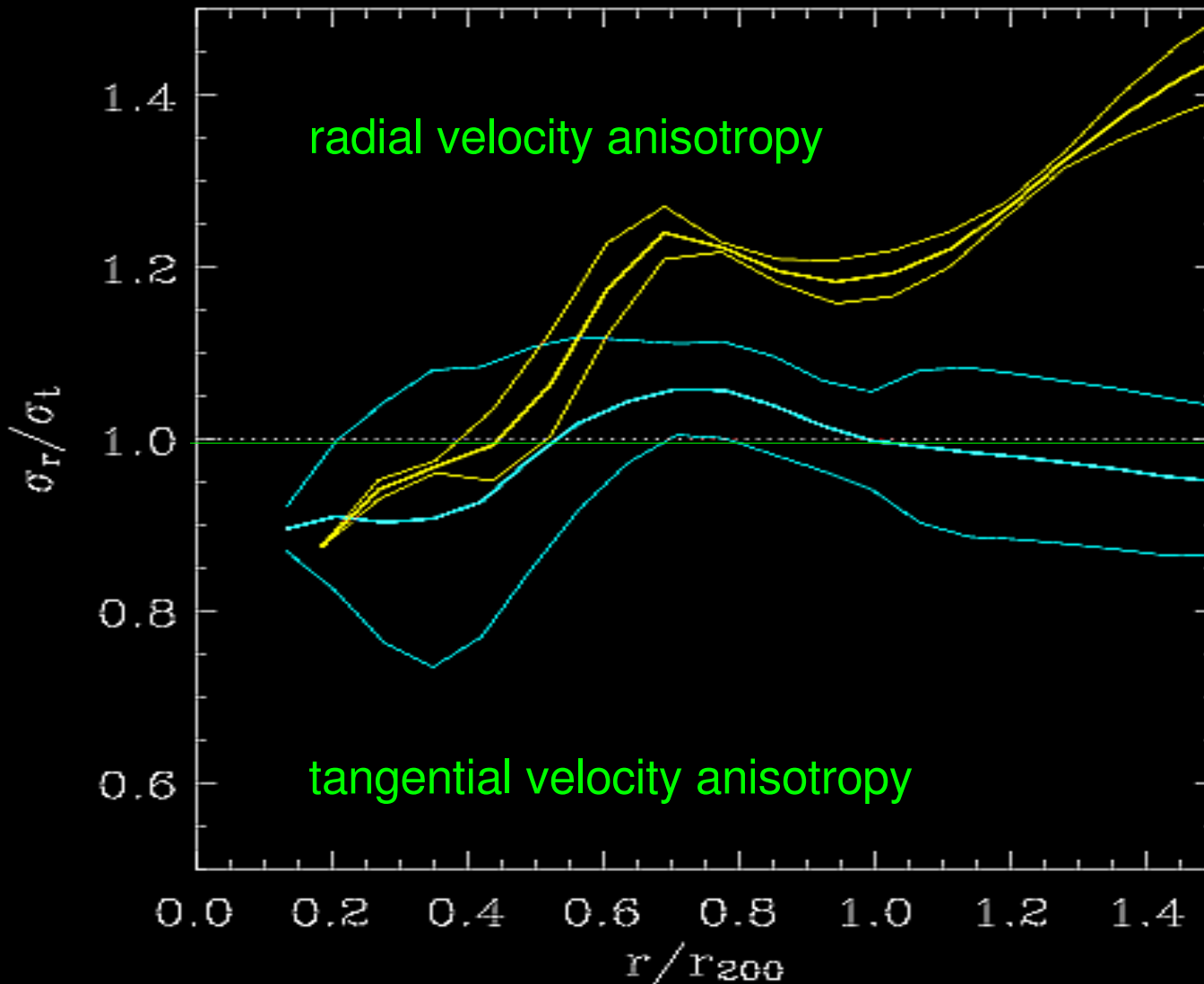
(Ellingson+01)

Estimates of  $dM/dt$  from  $M(r>r_{200})$   
in agreement with  $\Lambda$ CDM num. sims.  
(De Lucia & Blaizot 06)



# Early- and late-type gals: different $\beta(r)$

(CIRS; B., Diaferio, Rines, in prep)



# Isotropic orbits of early-type galaxies:

violent relaxation, phase- and chaotic-mixing

(Hénon 64, Lynden-Bell 67, Kandrup+Siopis 03)

at cluster formation and during major mergers

(Manrique+03, Peirani+06, Valluri+07)

secular growth of cluster mass (Gill+04)

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## Radial orbits of late-type galaxies:

similar to DM particles in num. sims.

recent infall (they still have gas)

after last major merger



# Subclusters

## Theoretical expectations (De Lucia + 04)

- Halos accrete subhalos
- Subhalo survival =  $f(\text{orbit}, \text{mass})$   
regulated by dyn. friction + tidal truncation
- Shape of subhalo  $f(M)$  independent of  $M_{\text{halo}}$
- Most massive subhalos avoid the halo center

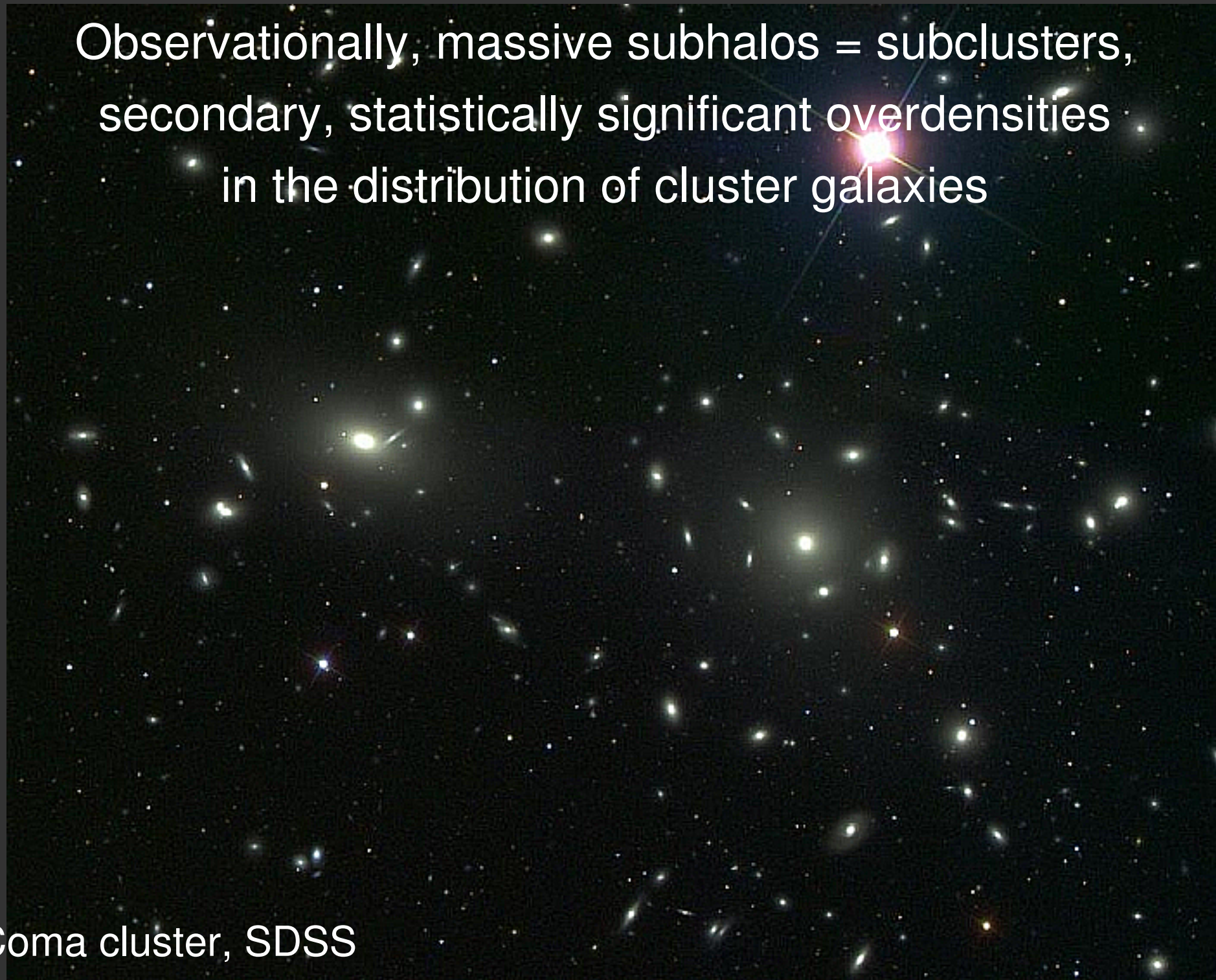
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Can we test the expectations?

Observationally, massive subhalos = subclusters,  
secondary, statistically significant overdensities  
in the distribution of cluster galaxies

Coma cluster, SDSS



# Subcluster identification:

Deviation from symmetry

and/or detection of

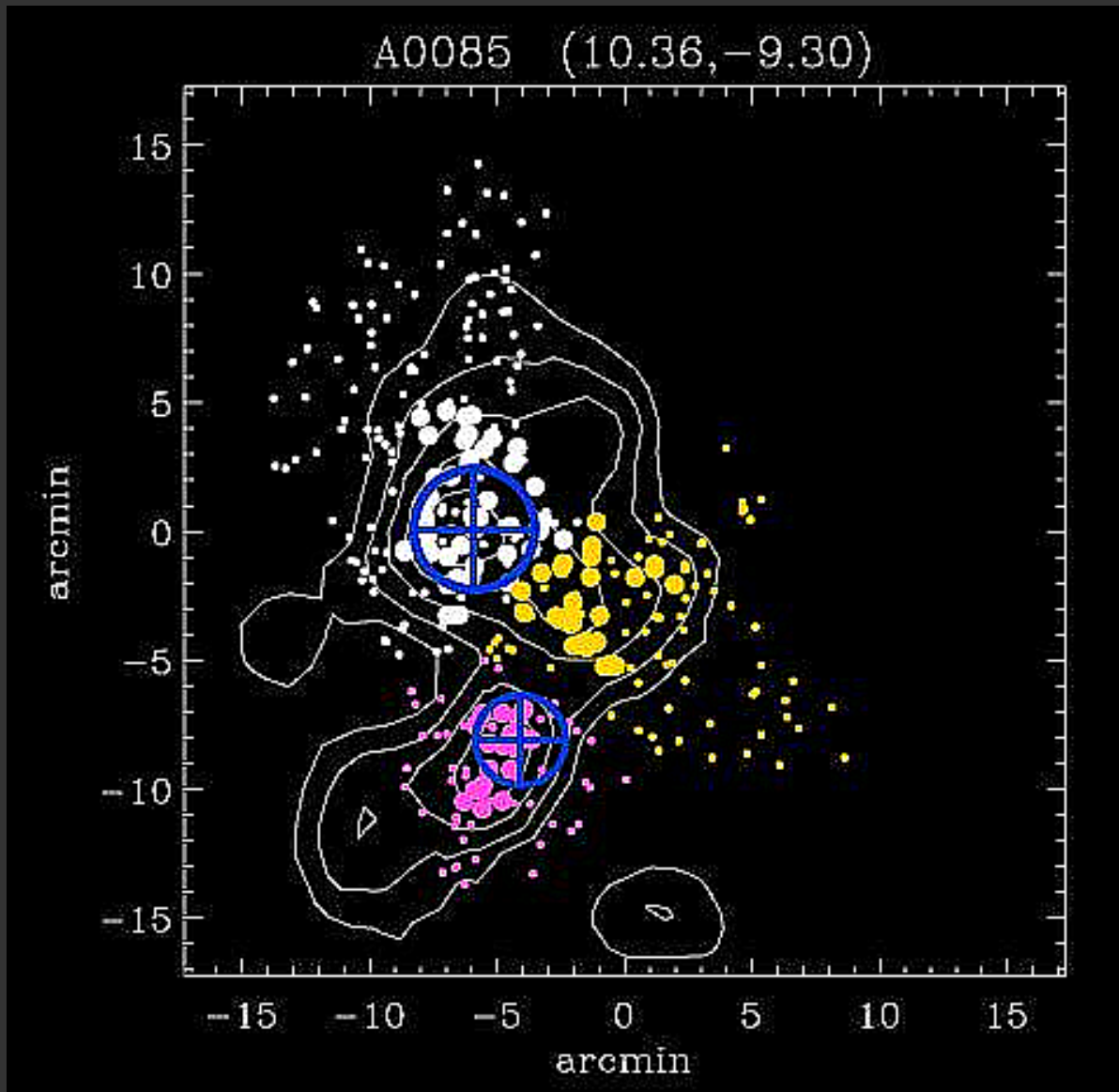
secondary

overdensities

in the spatial and/or

velocity distribution

of cluster galaxies



(Ramella+07)

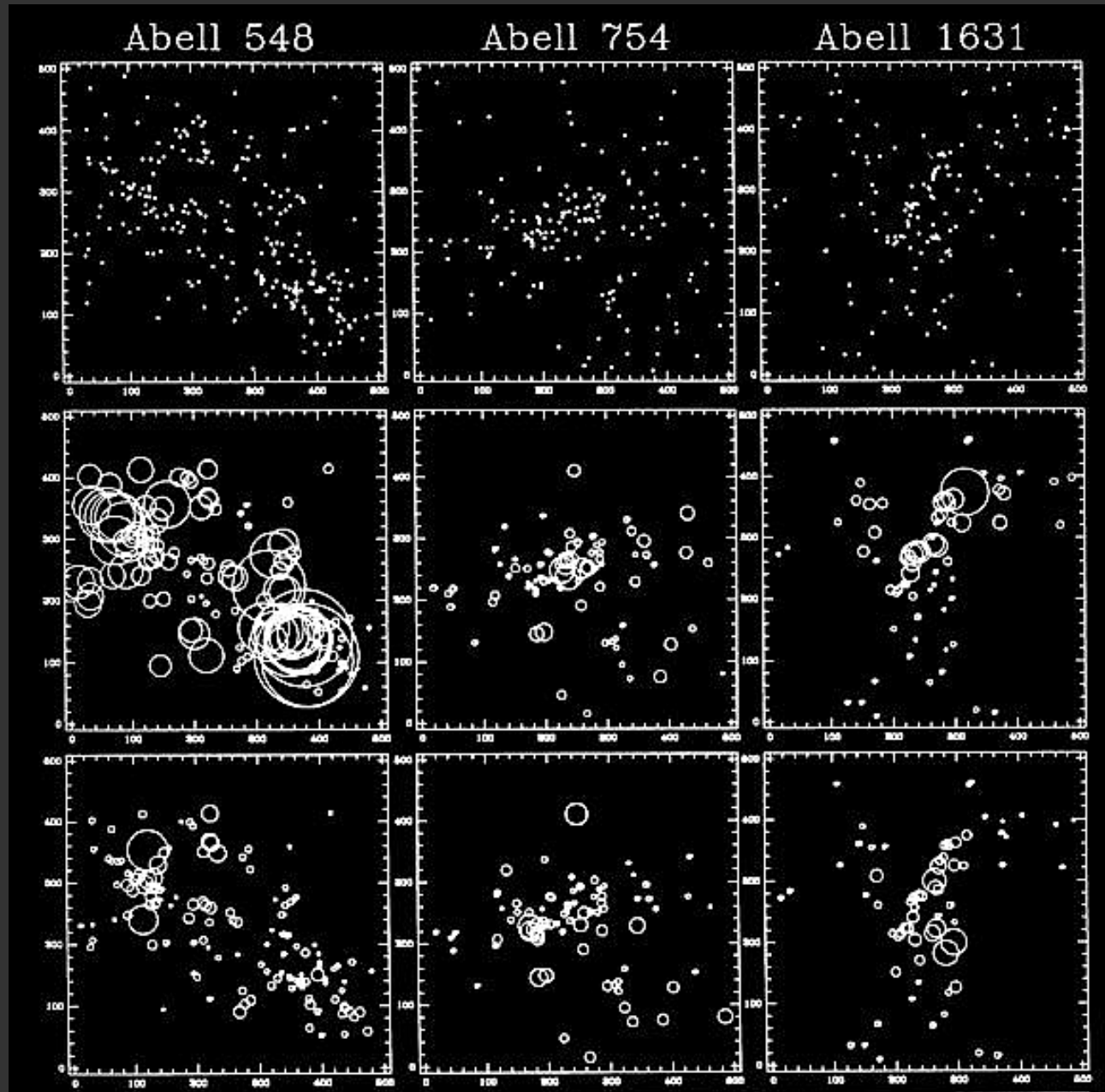
The method of Dressler & Shectman (1988):

$$\Delta = \sum_{i=1}^N (11/\sigma_p^2) [(\bar{v}_i - \bar{v})^2 + (\sigma_{p,i} - \sigma_p)^2]$$



Typically, >50 galaxy velocities needed

# The method of Dressler & Shectman (1988):



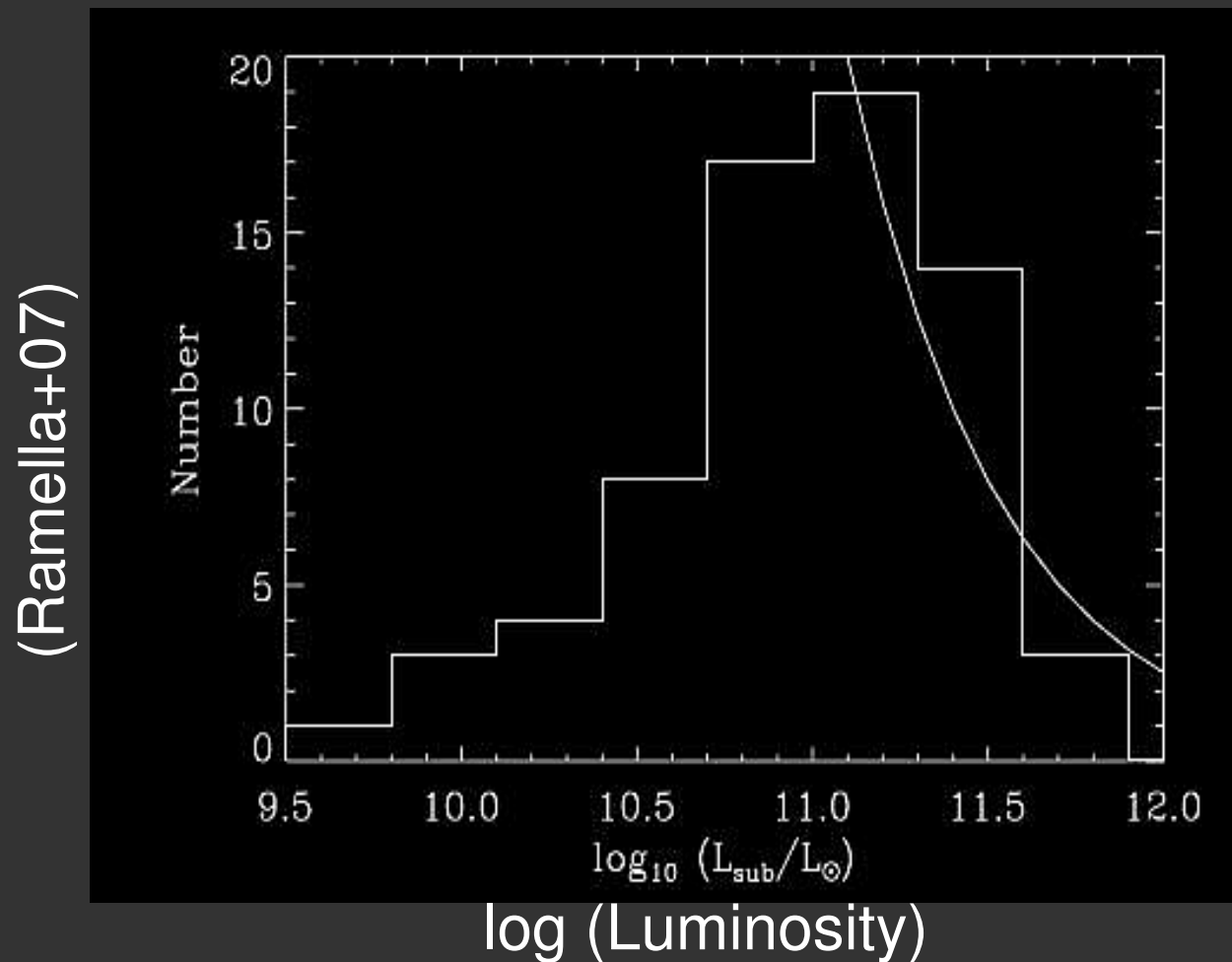
$\simeq 1/3$  nearby clusters show subclustering



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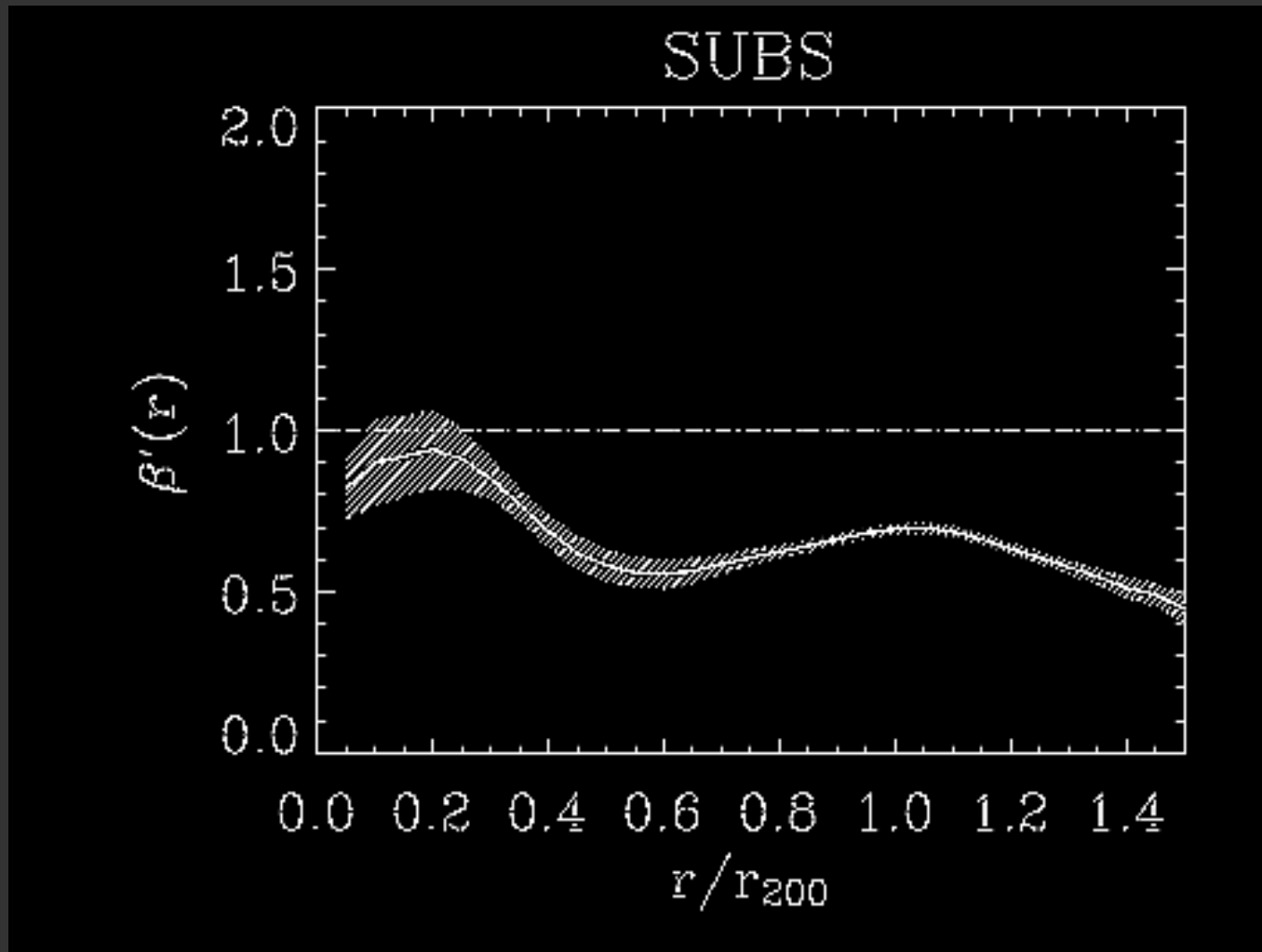


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Spatial and velocity distributions  
of subclusters suggests tidal disruption

(B. & Katgert 04)



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# Perspectives

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- $M(r)$  depends on  $M(t)$ ?  $\triangleleft$   $M(r)$  and  $M_{\text{subcl}}$

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- Mass accretion vs.  $z$ ?  $\triangleleft$  subclustering at high- $z$