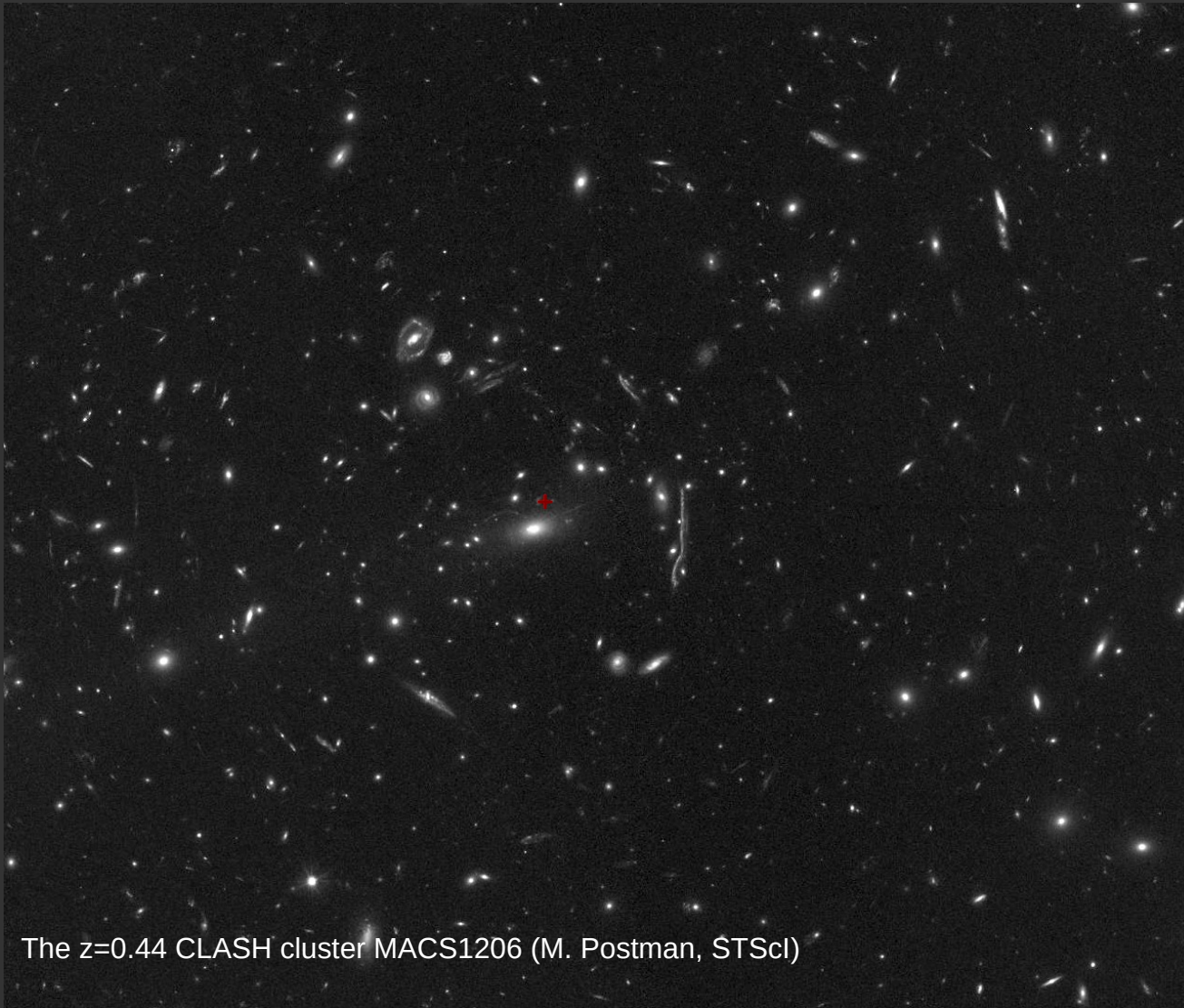


The inner slope of the cluster mass density profiles*



The $z=0.44$ CLASH cluster MACS1206 (M. Postman, STScI)

Andrea Biviano

INAF-OATs
& IFPU

Trieste, Italy



* *Mostly based on:*

- *Sartoris, AB + 2020, A&A, 637, A34*
- *AB + 2023, ApJ, submitted*

Outline of this talk

- ◆ Introduction - *the mass distribution in clusters of galaxies*
- ◆ Methods - *how to determine cluster mass profiles*
- ◆ Results
 - *the hydrostatic bias of the mass estimate*
 - *the inner slope of the cluster dark matter density profile*
- ◆ Discussion - *the inner slope of the cluster dark matter density profile*
- ◆ Summary and perspectives

Introduction – Clusters of galaxies probe Dark Matter

1933

Die Rotverschiebung von extragalaktischen Nebeln von F. Zwicky.

(16. II. 33.)

1. Setzt man voraus, dass das Comasystem mechanisch einen stationären Zustand erreicht hat, so folgt aus dem Virialsatz

$$\bar{\epsilon}_k = -\frac{1}{2} \bar{\epsilon}_p, \quad (4)$$

wobei $\bar{\epsilon}_k$ und $\bar{\epsilon}_p$ mittlere kinetische und potentielle Energien, z. B. der Masseneinheit im System bedeuten. Zum Zwecke der Ab-

von Beobachtungen an leuchtender Materie abgeleitete¹). Falls sich dies bewahrheiten sollte, würde sich also das überraschende Resultat ergeben, dass dunkle Materie in sehr viel grösserer Dichte vorhanden ist als leuchtende Materie.



2004



WEAK-LENSING MASS RECONSTRUCTION OF THE INTERACTING CLUSTER 1E 0657–558: DIRECT EVIDENCE FOR THE EXISTENCE OF DARK MATTER¹

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ANTHONY GONZALEZ

Department of Astronomy, University of Florida, 211 Bryant Space Science Center, Gainesville, FL 32611-2055

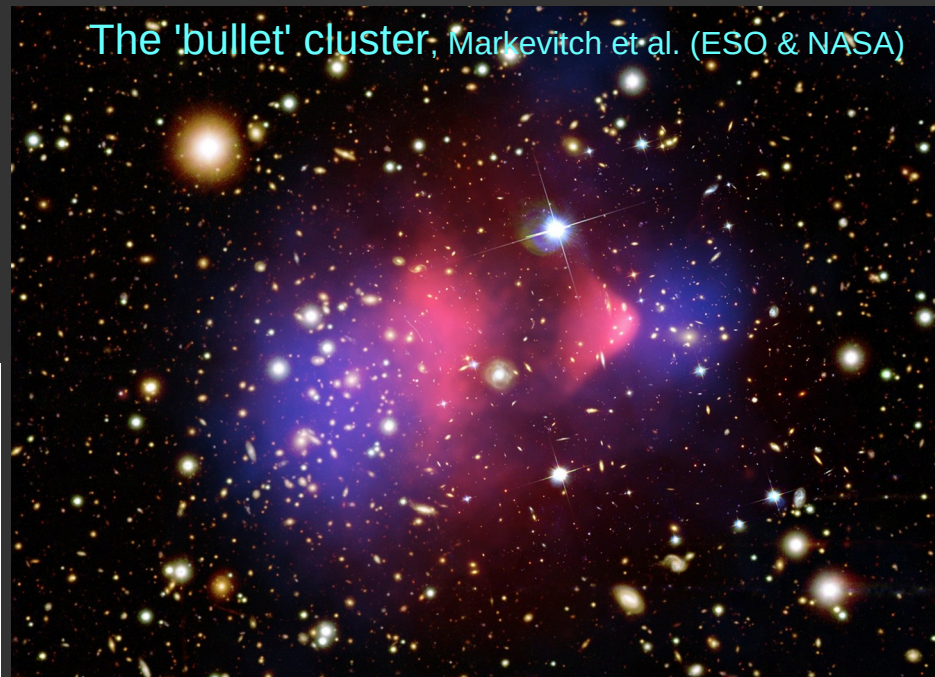
AND

MAXIM MARKEVITCH

Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138

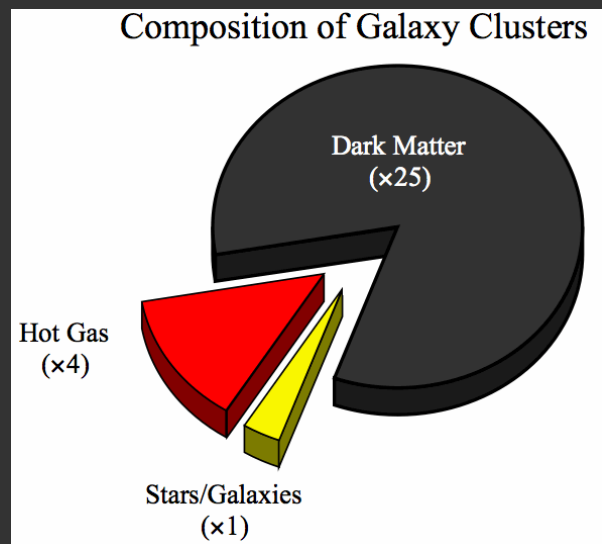
Received 2003 October 28; accepted 2003 December 11

The 'bullet' cluster, Markevitch et al. (ESO & NASA)



of relaxed clusters. The observed offsets of the lensing mass peaks from the peaks of the dominant visible mass component (the X-ray gas) directly demonstrate the presence, and dominance, of dark matter in this cluster. This

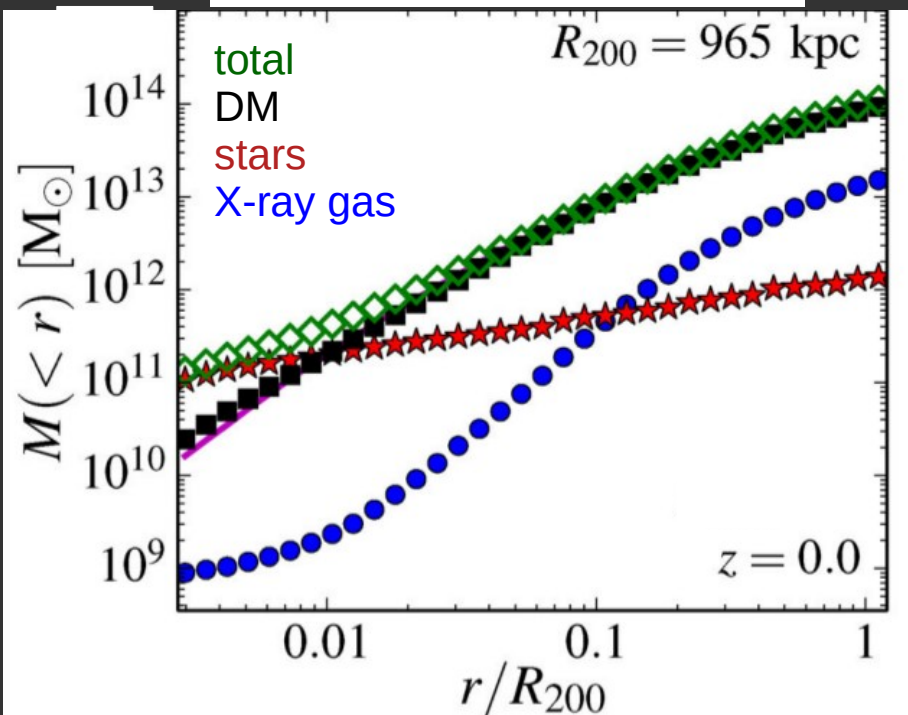
Introduction – Mass components distribution in clusters



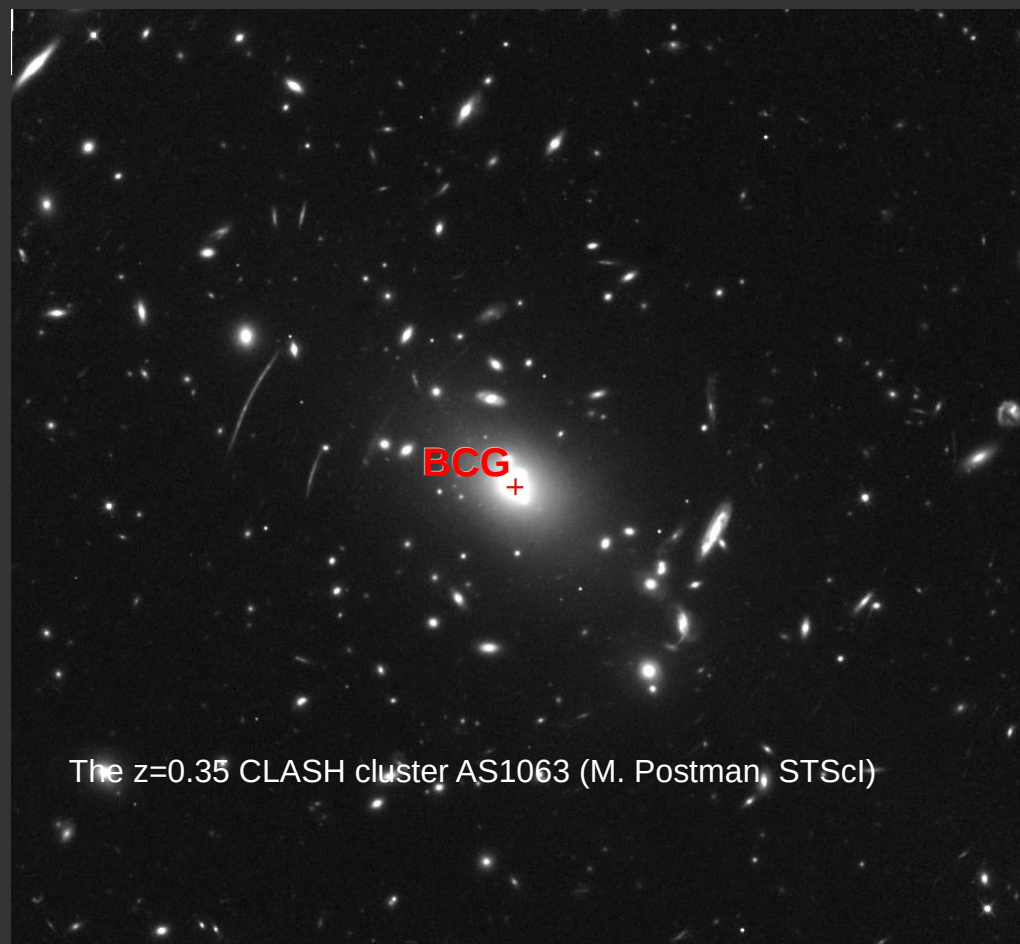
Dark Matter dominates at most radii

Most baryons are in the diffuse, hot, X-ray emitting gas,

At the cluster center the stellar component of the **Brightest Cluster Galaxy (BCG)** becomes dominant



EAGLE simulations, Schaller+15



The $z=0.35$ CLASH cluster AS1063 (M. Postman, STScI)

Introduction – Dark Matter distribution in clusters

Is there **A UNIVERSAL DENSITY PROFILE** of cosmological halos?

Navarro, Frenk & White 97:
the DM density profile, $\rho(r)$, of all
cosmological halos, is **universal**
- based on (collisionless)
Cold DM numerical simulations

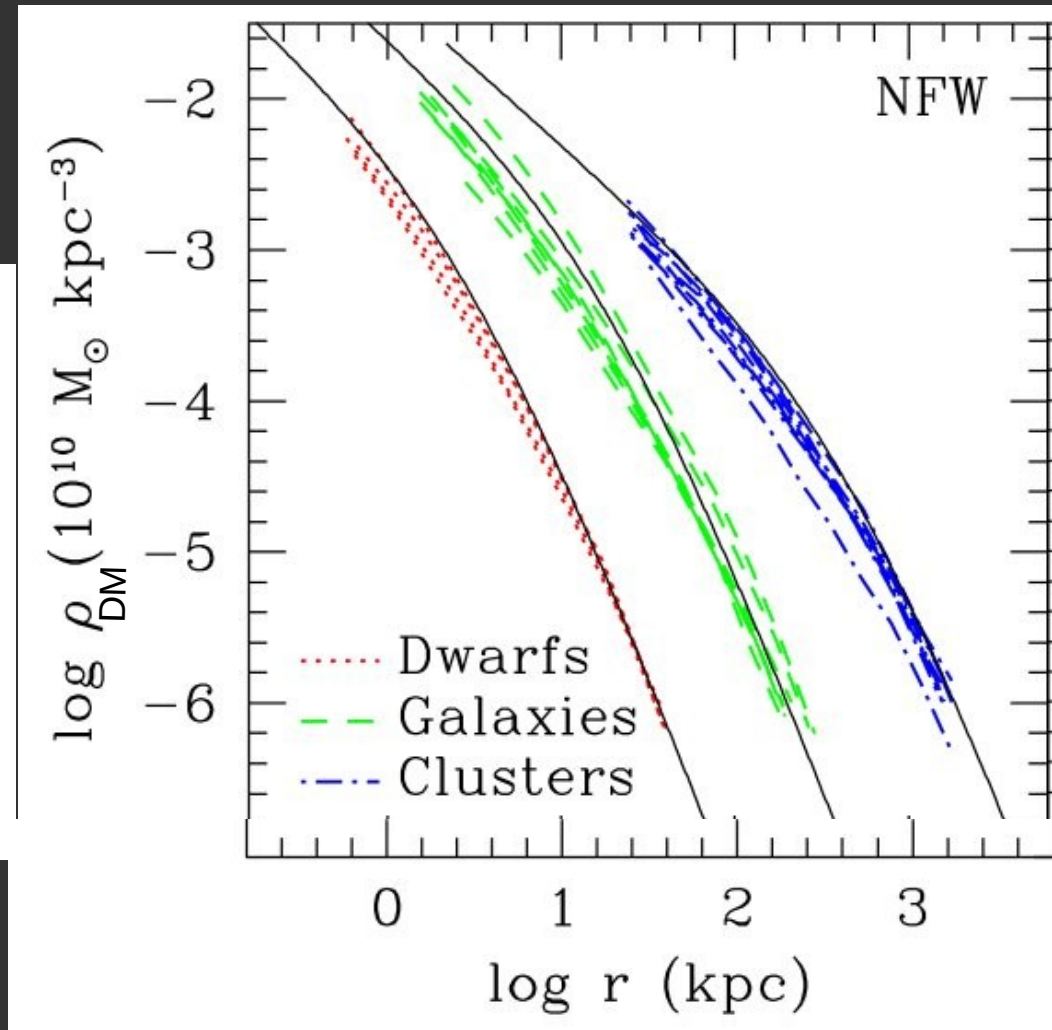


Julio Navarro

$$\rho_{\text{DM}}(r) \propto (r/r_{-2})^{-1} \times (1 + r/r_{-2})^{-2}$$

Inner logarithmic slope -1, asymptotic slope -3
with a change in slope at a characteristic radius r_{-2}

Log Density



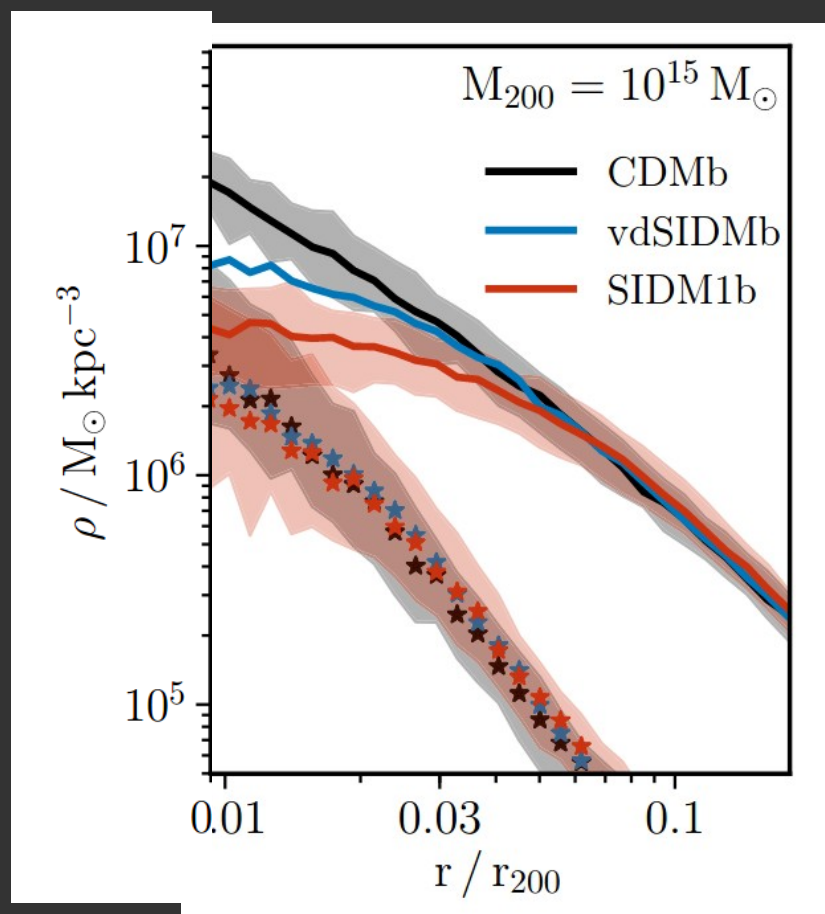
(Navarro+04)

Introduction – Dark Matter distribution in clusters

Clusters are DM dominated \Rightarrow their mass distribution should be similar to the NFW shape found in collisionless Cold DM cosmological simulations

If cluster DM distribution deviates from NFW shape, then:

- DM may not be Cold (e.g. Warm DM; Bode+01),
- or it may be collisional (e.g. Self-Interacting DM; Spergel+Steinhardt 00)



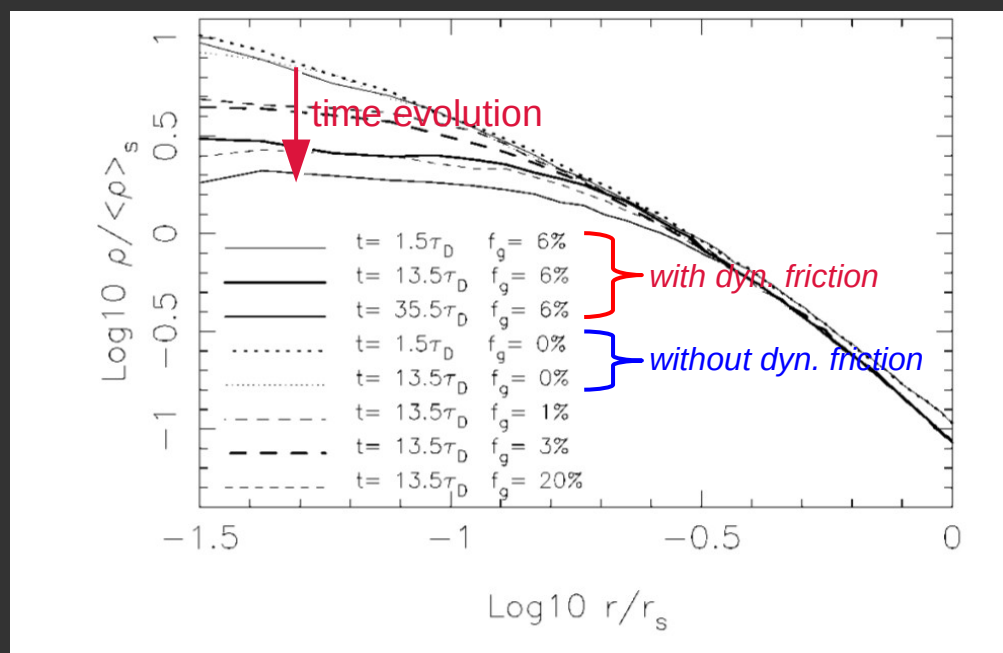
The flattening of the mass density profile of simulated clusters in Self-Interacting DM models compared to Cold DM (Robertson+21)

Introduction – Dark Matter distribution in clusters

However:

the DM distribution can deviate from NFW because of physical processes:

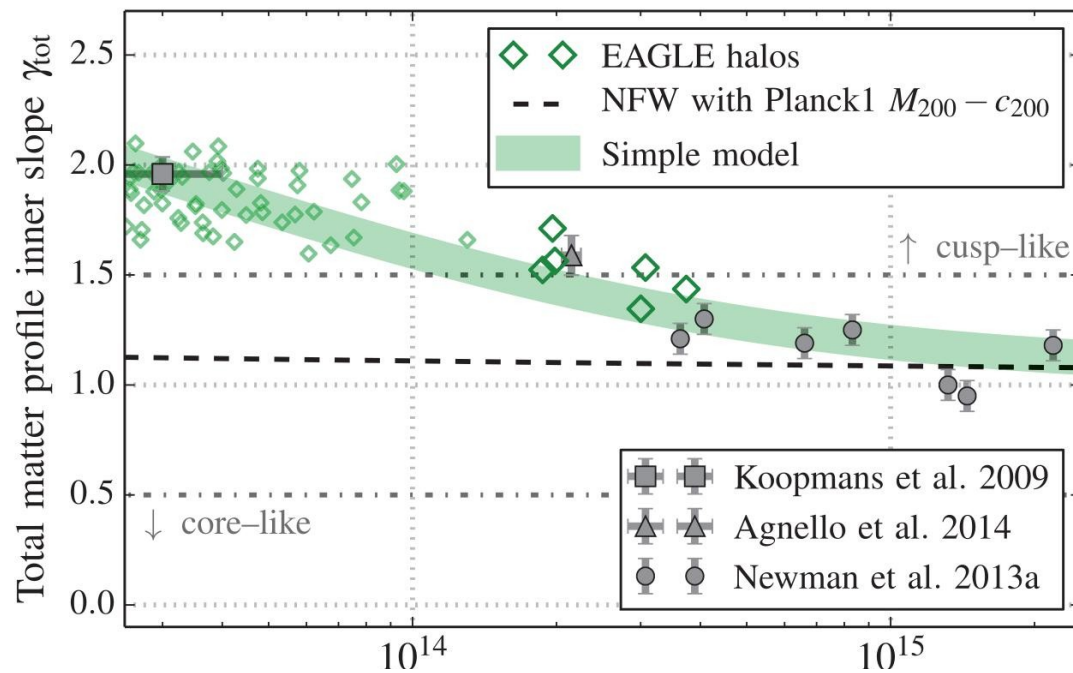
- ♦ Adiabatic contraction (*Blumenthal+86, Gnedin+04*)
 - ♦ Recent accretion of a large subcluster (*Schaller+15*)
 - ♦ Dynamical friction (*El-Zant+01, +04*)
 - ♦ Collisionless mergers (*Laporte+12*)
 - ♦ AGN feedback (*Navarro+96, Ragone-Figueroa+12, Peirani+17*)
- $\rho_{DM}(r \rightarrow 0)$ cuspiers
- $\rho_{DM}(r \rightarrow 0)$ flatter



Time evolution of the mass density profile of simulated clusters in models w/wo dynamical friction energy transfer from subclumps to main halo (*El-Zant+04*)

⇒ Measuring the inner slope of several cluster DM profiles at different redshifts constrains the properties of DM and/or these physical processes

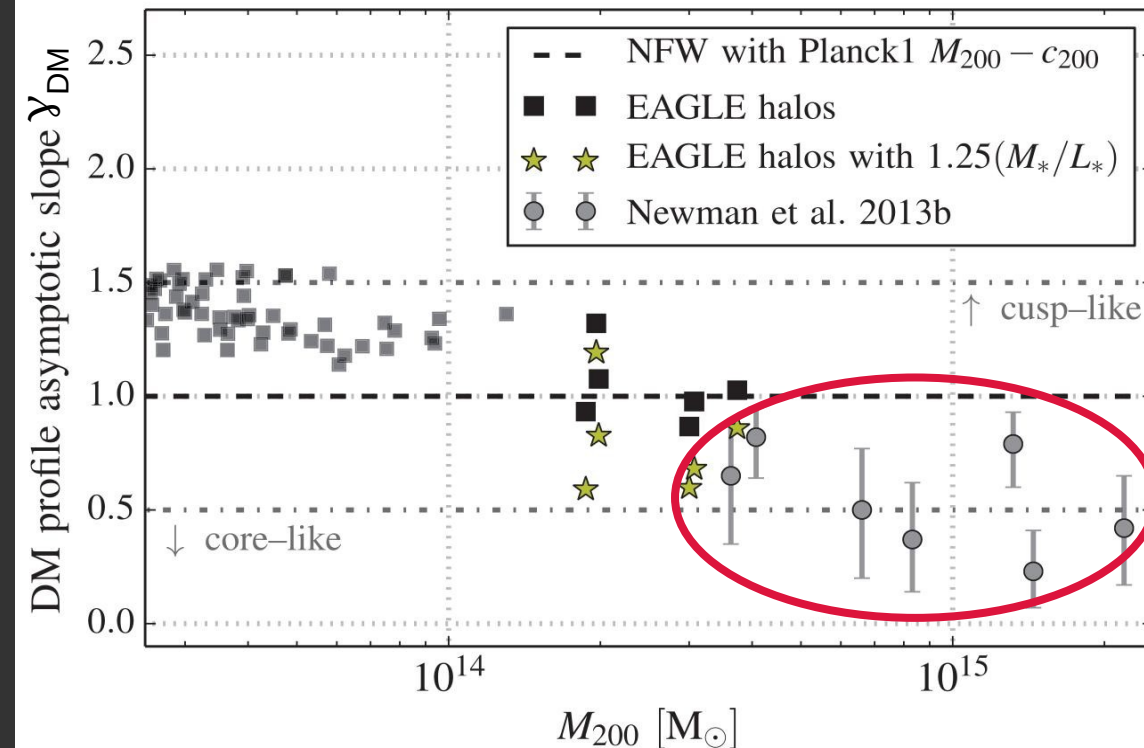
Introduction – Dark Matter distribution in clusters



Schaller+15:

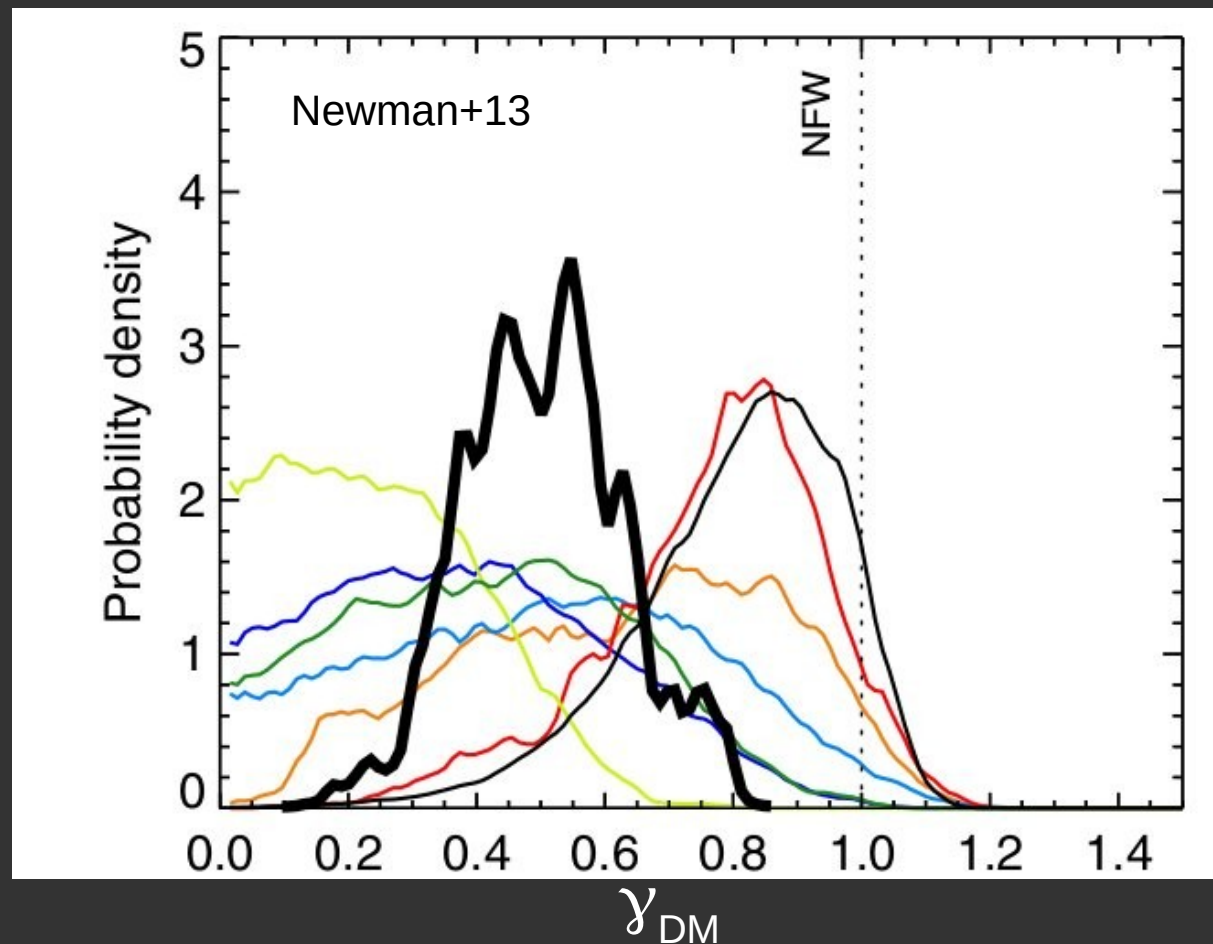
We must distinguish the inner logarithmic slope of the *total* matter profile, γ_{tot} , from the inner logarithmic slope of the DM profile $\gamma_{\text{DM}} \equiv d \log \rho_{\text{DM}} / d \log r$

The stellar mass contribution to the total mass makes $\gamma_{\text{tot}} > \gamma_{\text{DM}}$ ($\gamma_{\text{tot}} - \gamma_{\text{DM}} \approx 0.1$ for very massive halos)



Newman+13's determinations of γ_{DM} for clusters based on observations of gravitational lensing and kinematics are in disagreement with the results from the EAGLE simulations

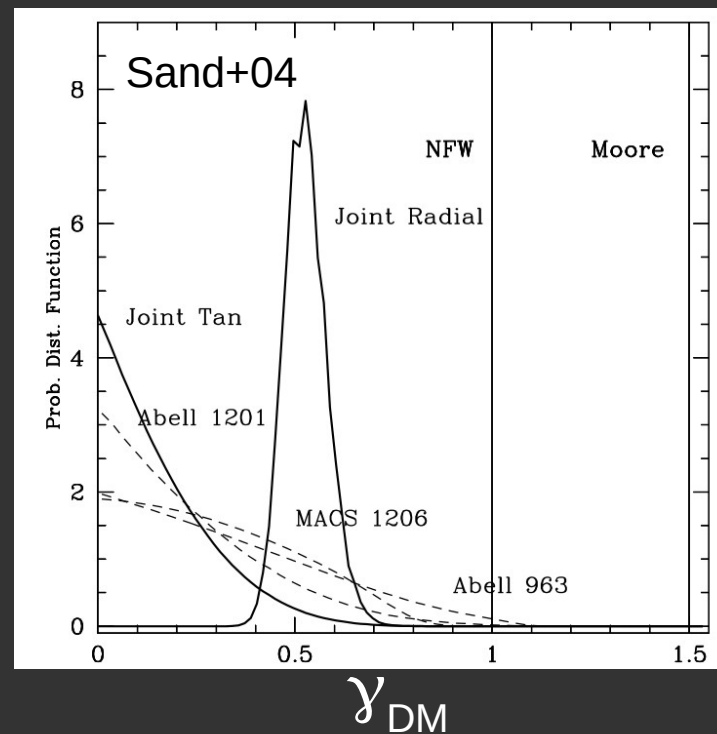
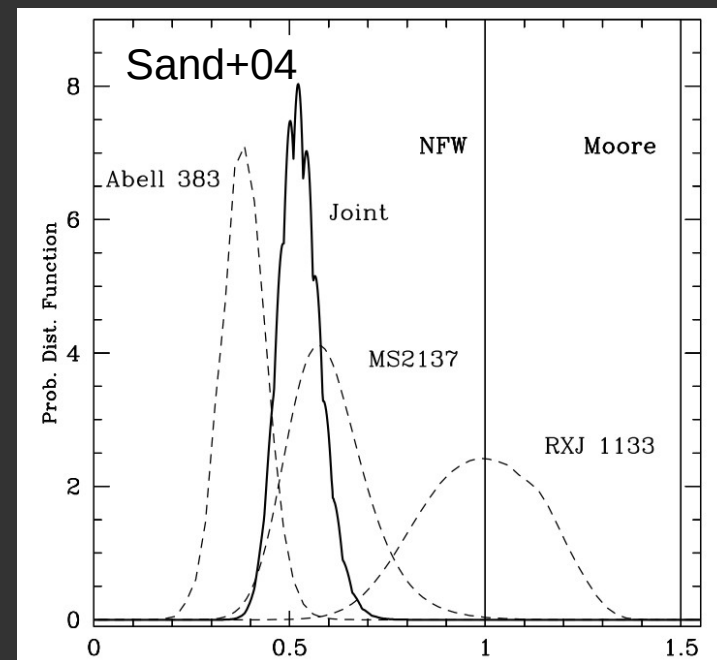
Introduction – Dark Matter distribution in clusters



Previous results for 10 clusters based on Strong Lensing + kinematics of BCG (Sand+04, +08; Newman+13) find

$$\gamma_{DM} = 0.5 \pm 0.1$$

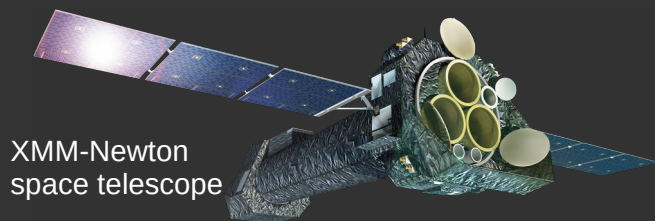
(<1 , flatter than NFW at the center)



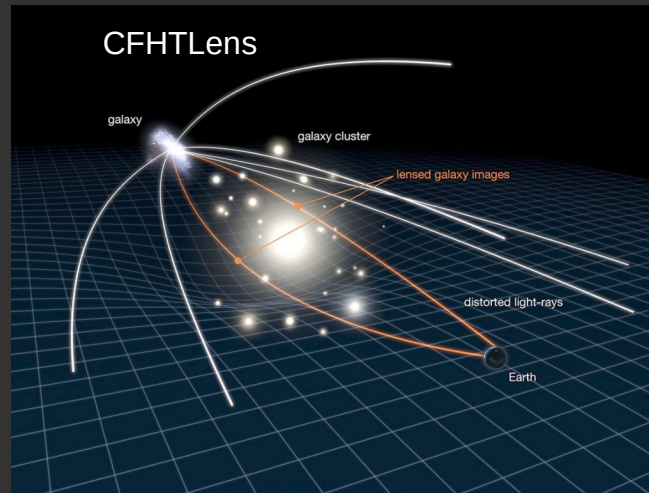
Methods – How to determine the cluster mass distribution



X-ray & radio (Sunyaev-Zeldovich) observations: assuming hydrostatic equilibrium of the intra-cluster gas



ACT radio telescope



Optical observations: using the deflected and amplified light from background galaxies due to the gravitational lensing effect



Hubble space telescope

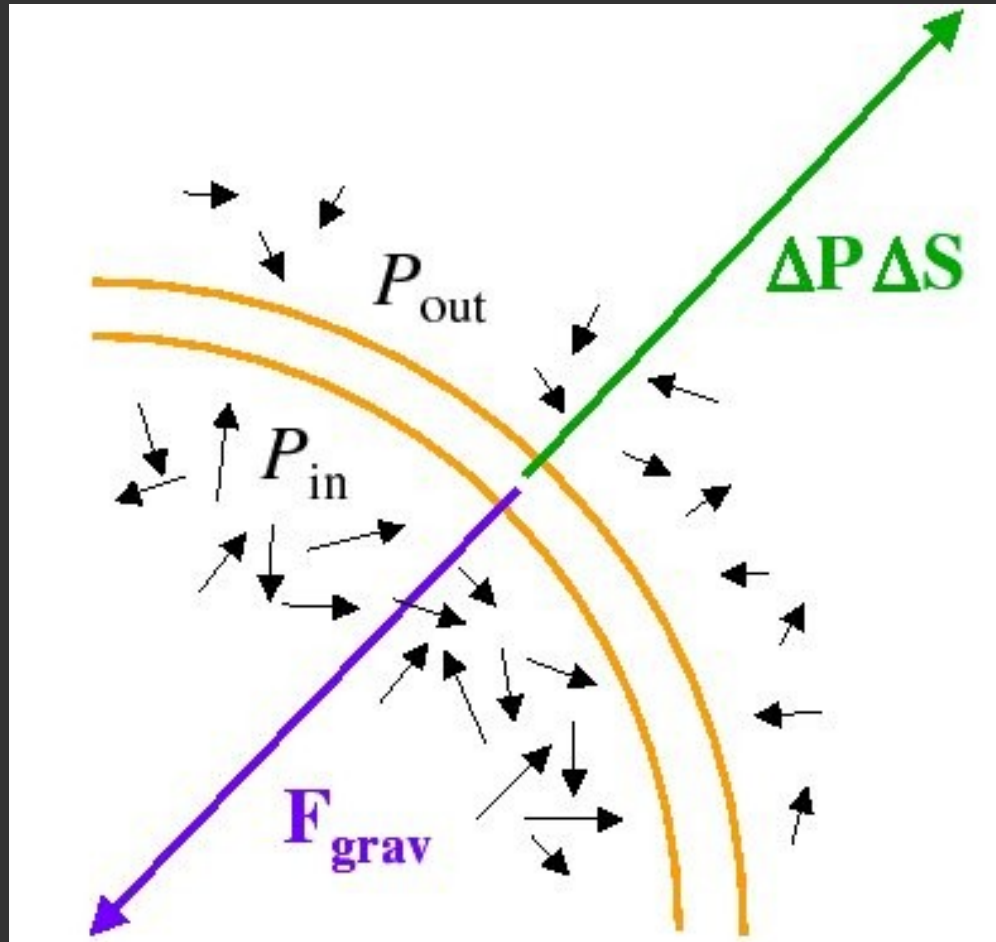


Optical observations: using the spatial and velocity distributions of cluster galaxies and BCG stars



Very Large Telescope

Methods – How to determine the cluster mass distribution

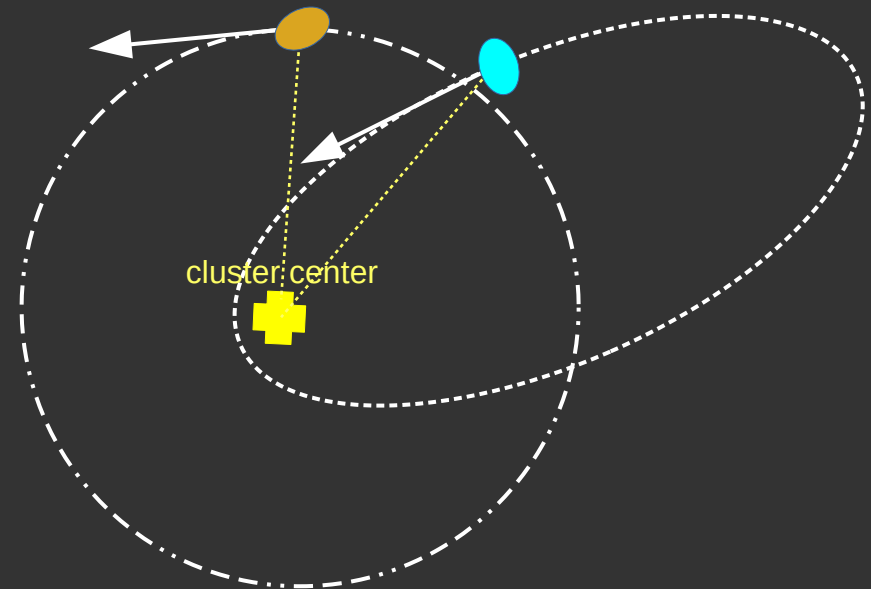


(courtesy of G. Mamon)

Cluster mass \Rightarrow Gravitational pull

Number density +
velocity distribution of galaxies \Rightarrow
Pressure against gravitational pull

Pressure is different if the velocity
vector is aligned with or orthogonal to
the gravitational pull, i.e. it depends
on the galaxy orbital shape
(radial vs. tangential)



Methods – How to determine the cluster mass distribution

$$M(< r) = -\frac{r\sigma_r^2}{G} \left(\frac{d \ln \nu}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right)$$

Mass profile

3D number density profile

Velocity dispersion profile along the radial direction, r

Velocity anisotropy profile

$$\beta(r) = 1 - \frac{\sigma_\theta^2(r)}{\sigma_r^2(r)}$$

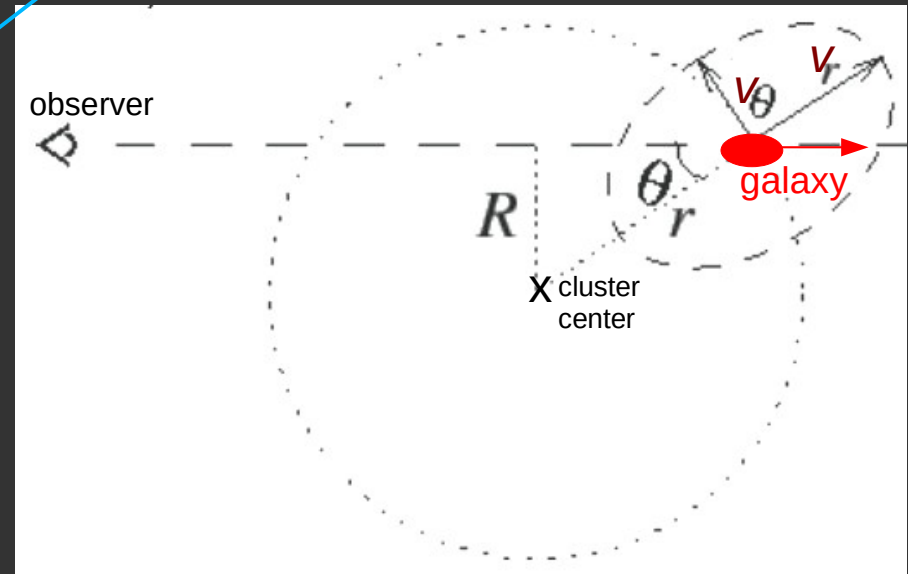
Velocity dispersion profile along the tangential direction

$\beta(r)$ is related to the orbital distribution of cluster galaxies:
 $\beta(r) < 0$ tangentially elongated
 $\beta(r) > 0$ radially elongated



The solution for the mass profile $M(< r)$ is degenerate with the solution for the velocity anisotropy profile $\beta(r)$:

Mass-Anisotropy Degeneracy



(courtesy of G. Mamon)

Methods – How to determine the cluster mass distribution

MAMPOSSt (*Mamon, AB, Boué 13*)

It performs a maximum likelihood fit of model $M(<r)$ and model $\beta(r)$ to the projected phase-space distribution of cluster galaxies

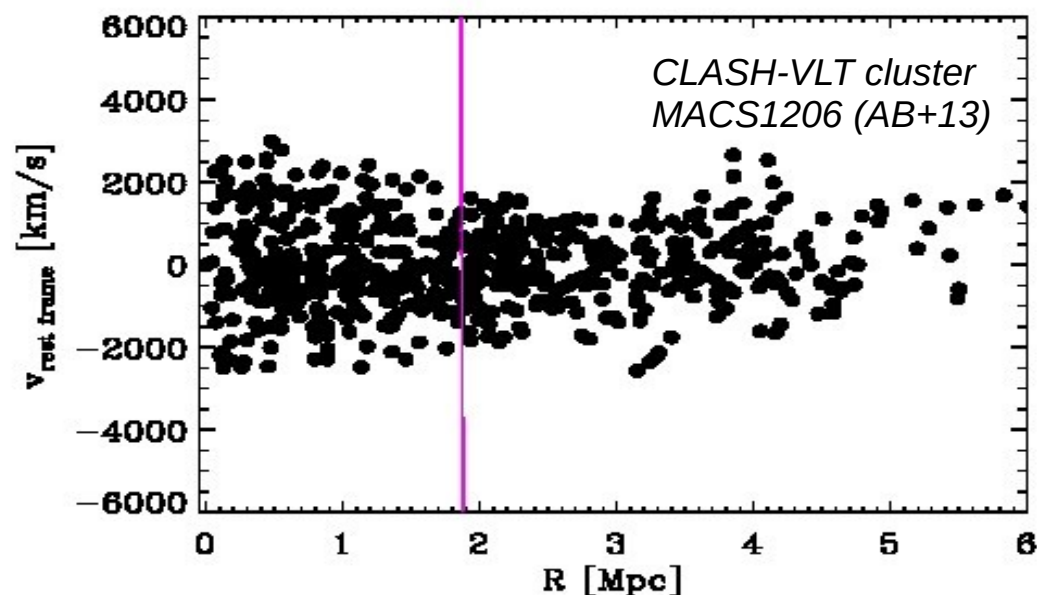
Modelling
Anisotropy and
Mass
Profiles of
Observed
Spherical
Systems

Traditional approaches cannot solve the Jeans equation without making assumptions on the distribution of the orbital shapes of cluster galaxies

MAMPOSSt breaks the mass-anisotropy degeneracy of the Jeans equation by using the full information available in the spatial and velocity distributions of cluster galaxies

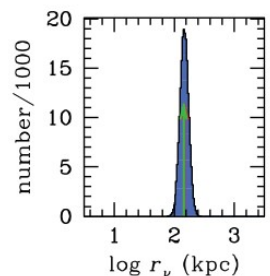
MAMPOSSt constrains $M(<r)$ and $\beta(r)$ at the same time

Fortran+python code available on GitHub (Pizzuti+23)



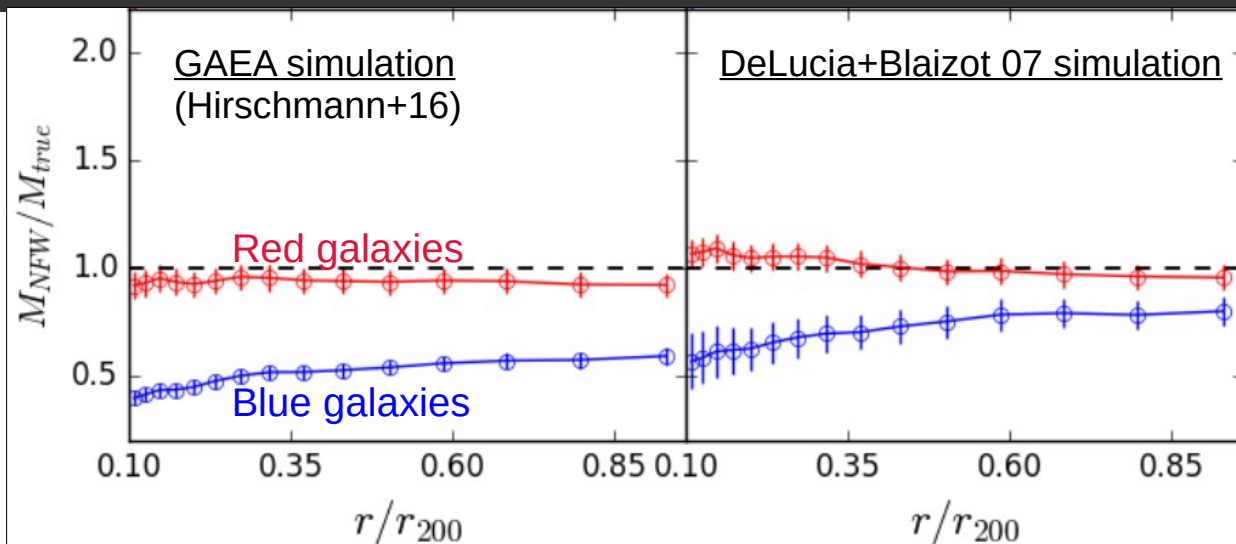
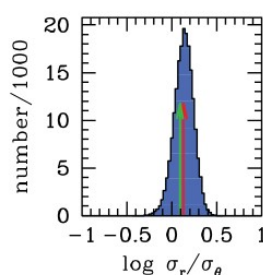
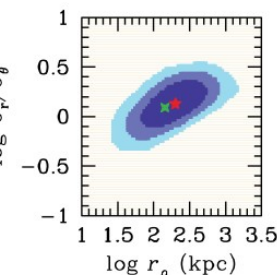
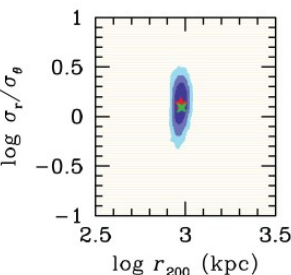
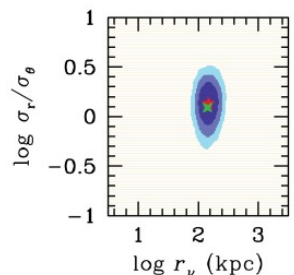
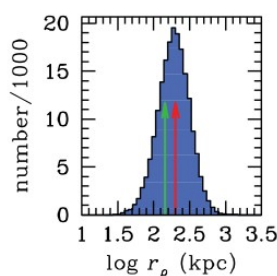
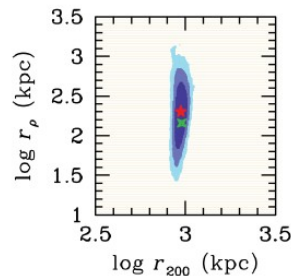
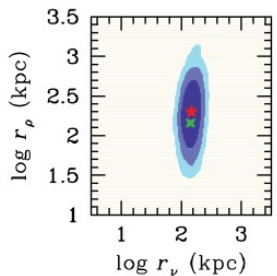
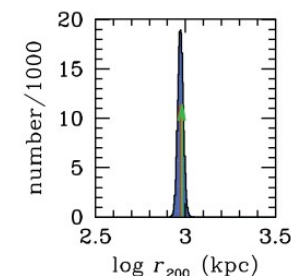
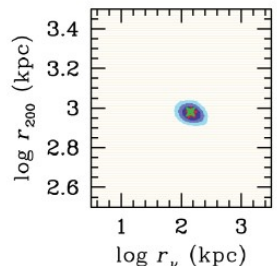
Methods – How to determine the cluster mass distribution

MAMPOSSt tested on numerical simulations (hydrosim and semi-analytic) that include projection effects (interlopers)



Borgani+04 simulation

True value
MAMPOSSt solution
1σ contour



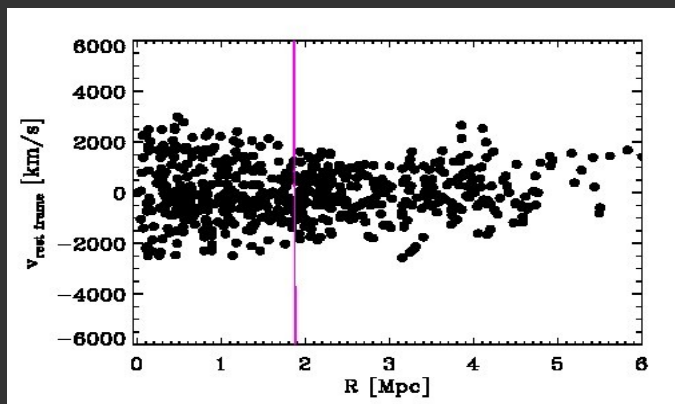
MAMPOSSt $M(r)$ NFW model solution to true $M(r)$ for 100 clusters x 3 projection axes: using red galaxies as tracers allows an accurate $M(r)$ determination (Aguirre Tagliaferro, AB + 21)

500 particle cluster-sized halo, NFW model with 4 free parameters (Mamon, AB, Boué 13)

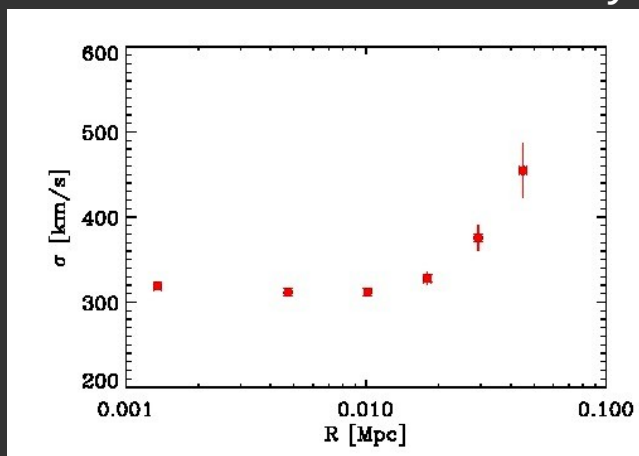
Methods – How to determine the cluster mass distribution

MAMPOSSt+: extension of MAMPOSSt to take into account simultaneously the constraints from the spatial and velocity distribution of the cluster galaxies and the BCG stars (*Sartoris, AB+ 20*)

Joint Maximum Likelihood fit to the projected phase-space distribution of cluster members:



and to the l.o.s. BCG velocity dispersion profile:



Constrain the best-fit parameters of the cluster mass profile $M(r)$ parameterized as a sum of:

- DM mass profile
- + BCG stellar mass profile
- + Intra-Cluster gas mass profile
- + stellar mass profile of all other galaxies

$$M(r) = M_{\text{gNFW}} + M_{\text{Jaffe}} + M_{\text{ICM}} + M_{\text{gal}}$$

Diagram illustrating the components of the cluster mass profile $M(r)$:

- M_{gNFW} : DM (Dark Matter)
- M_{Jaffe} : BCG stellar mass
- M_{ICM} : Intra-cluster gas
- M_{gal} : galaxies stellar mass

Methods – How to determine the cluster mass distribution

We run MAMPOSSt assuming spherical symmetry, and constrain the best-fit parameters of the different components of the total mass profile

$$M_{\text{tot}} = M_{\text{DM}} + M_{\text{BCG}} + M_{\text{ICM}} + M_{\text{galaxies}}$$

(gNFW) (Jaffe)

4 free parameters for $M_{\text{tot}}(r)$:

- 1 for the $M_{\text{BCG}}(r)$: (M/L)
- 3 for the $M_{\text{DM}}(r)$: r_{200} , r_{ρ} , γ_{DM}

L_{BCG} and r_j derived from fit to observed BCG surface brightness profile

M_{ICM} and M_{galaxies} derived directly from observations, no free parameters (they do not contribute much to the cluster mass in the inner region)

+ 1 (constrained) free parameter for the number density profile of cluster galaxies: r_v

+ ≤ 2 free parameters for the galaxy velocity anisotropy profile:

- Tired model with free outer (β_{∞}) and free or fixed inner (β_0) anisotropy

We also consider ≤ 3 models for the velocity anisotropy profile of the BCG stars:

- a) isotropic, b) moderately radial ($\beta=0.3$), c) increasing with radius (Osipkov-Merritt $r_{\beta}=r_j$)

Data sets – CLASH clusters AS1063 and MACS1206



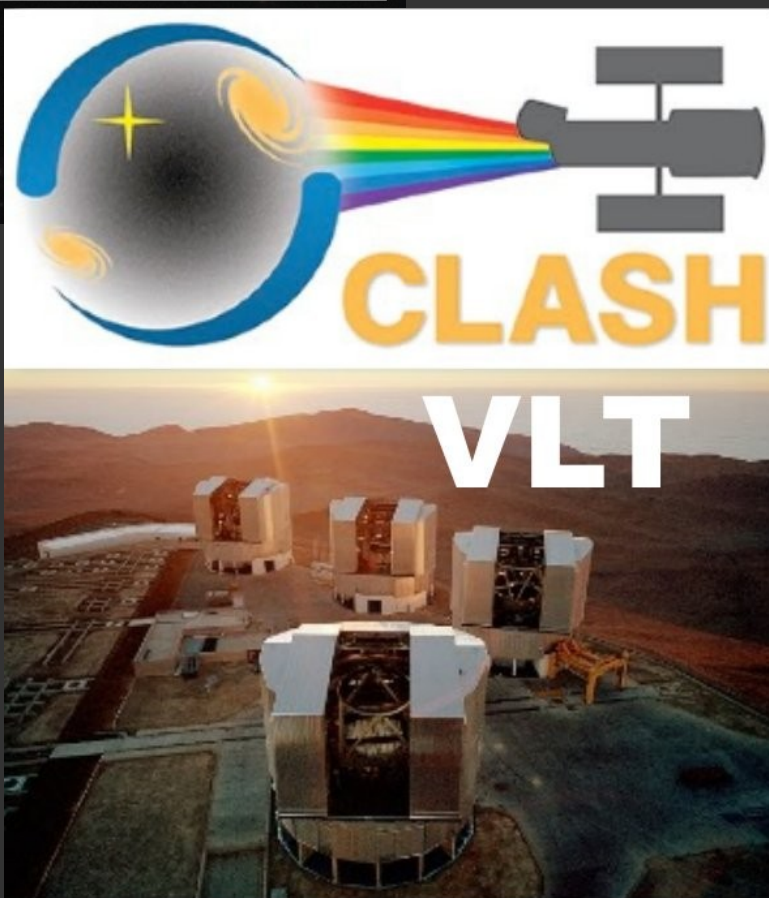
CLASH: CLUSTER LENSING AND SUPERNOVA SURVEY WITH HUBBLE

Postman+12

25 MASSIVE GALAXY CLUSTERS OBSERVED USING
THE HUBBLE SPACE TELESCOPE TO STUDY
DARK MATTER, DISTANT GALAXIES,
CLUSTER GALAXY EVOLUTION,
AND THE GEOMETRY OF THE UNIVERSE.

CLASH-VLT: A VIMOS Large Programme to Map the Dark
Matter Mass Distribution in Galaxy Clusters and Probe
Distant Lensed Galaxies (*Rosati+14*)

VIMOS@VLT: ~ 8000 cluster members with z in 12 clusters
+ MUSE@VLT: velocity dispersion profiles of 7 BCGs



Data sets – CLASH clusters AS1063 and MACS1206

CLASH-VLT data reduction summary



CLASH-VLT: A VIMOS Large Programme to Map the Dark Matter Mass Distribution in Galaxy Clusters and Probe Distant Lensed Galaxies (*Rosati+14*)

VIMOS@VLT: ~ 8000 cluster members with z in 12 clusters + MUSE@VLT: velocity dispersion profiles of 7 BCGs

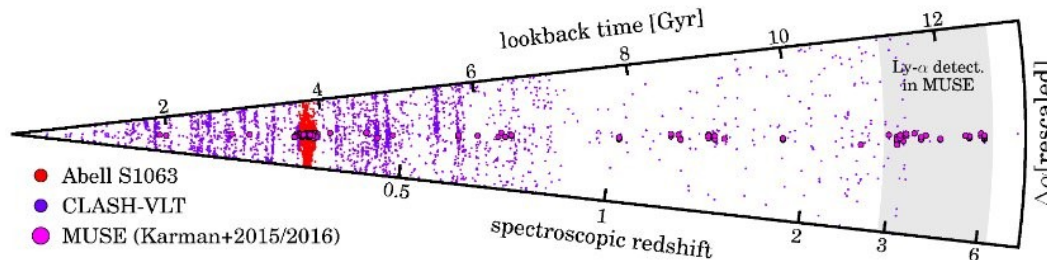
The team:

P. Rosati (PI),
I. Balestra, P. Bergamini, AB,
G. Caminha, S. Ettori, M. Girardi,
C. Grillo, A. Mercurio, **M. Nonino**,
B. Sartoris, K. Umetsu, E. Vanzella
+ L. Pizzuti

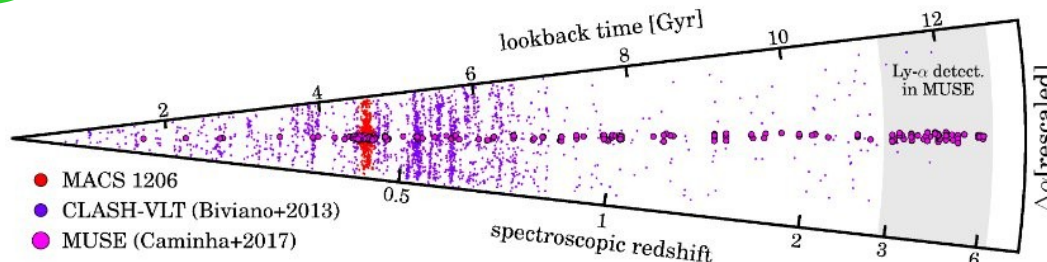


Mario Nonino (1960-2023)

RXJ2248 a.k.a. AS1063

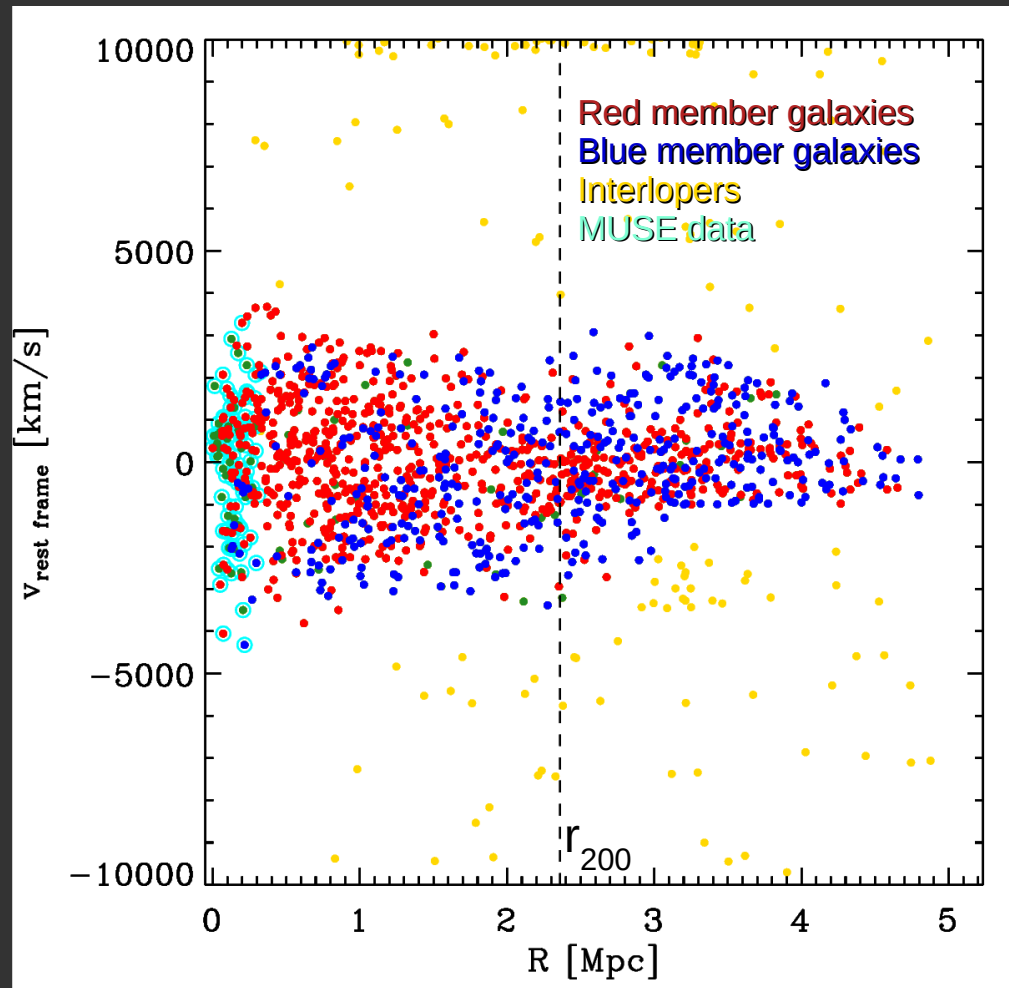


MACS1206

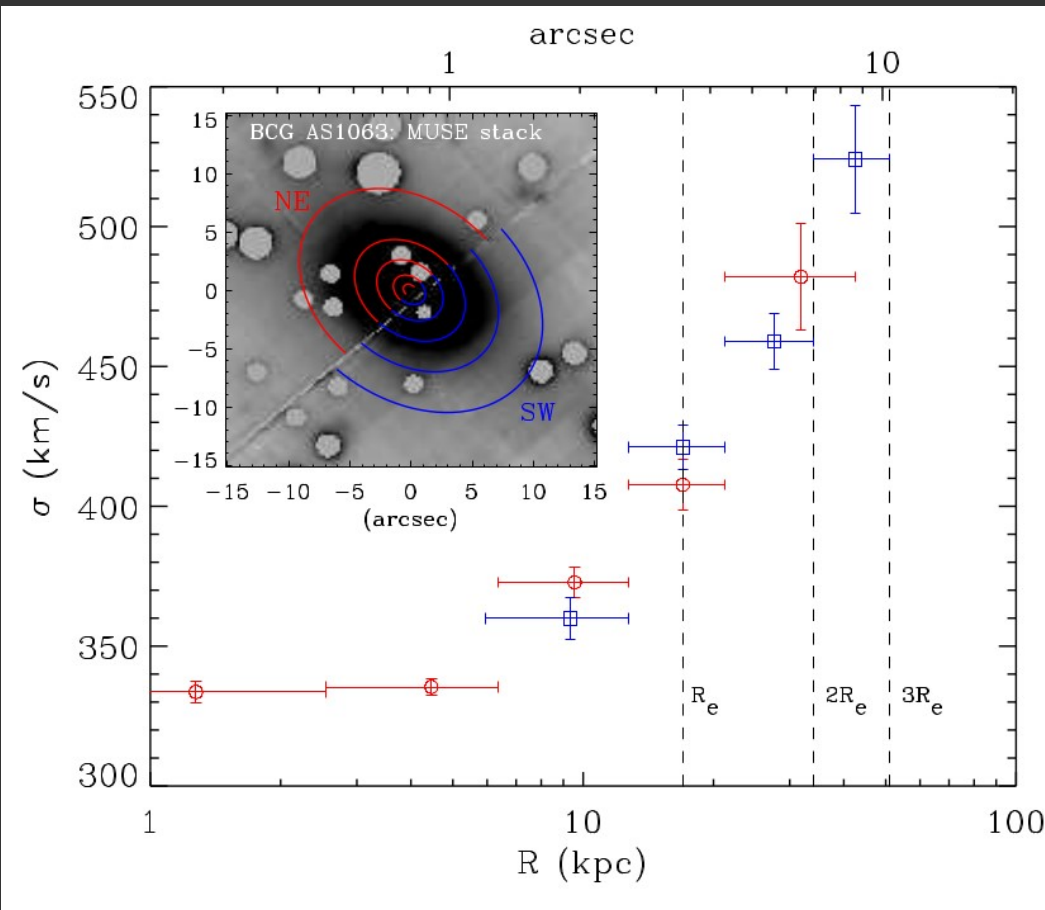


Data sets – CLASH clusters AS1063 and MACS1206

AS1063, $z=0.3458$, $M_{200}=2.8 \cdot 10^{15} M_{\odot}$



Projected phase-space distribution of galaxies;
1234 cluster members, of which
792 with $R \leq r_{200}$ used in our dynamical analysis



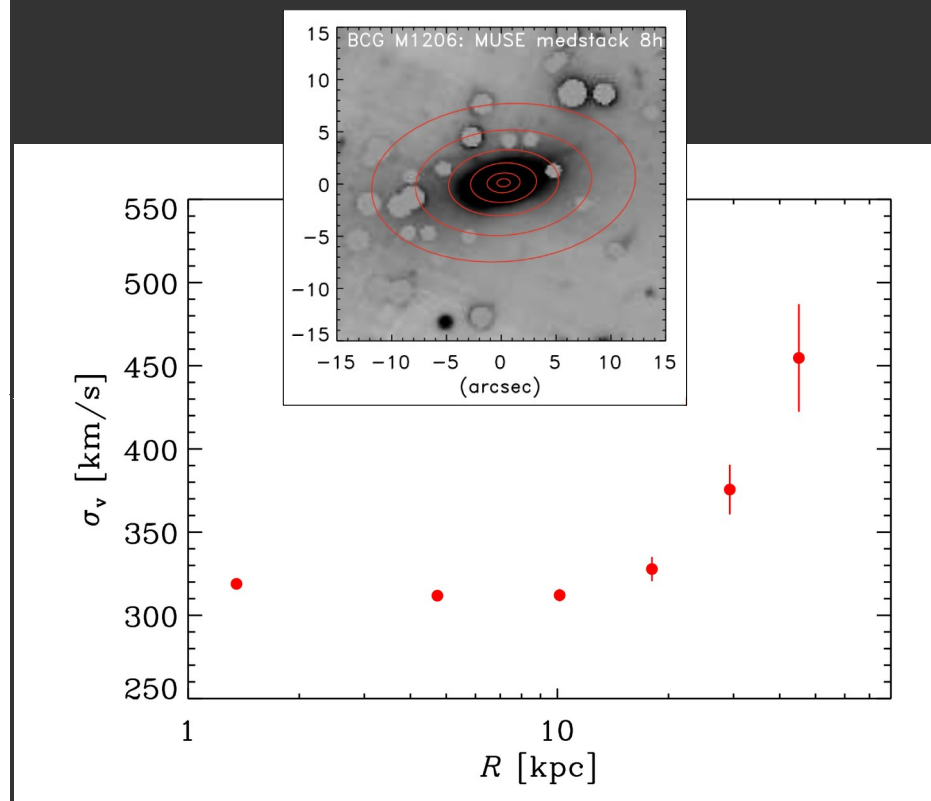
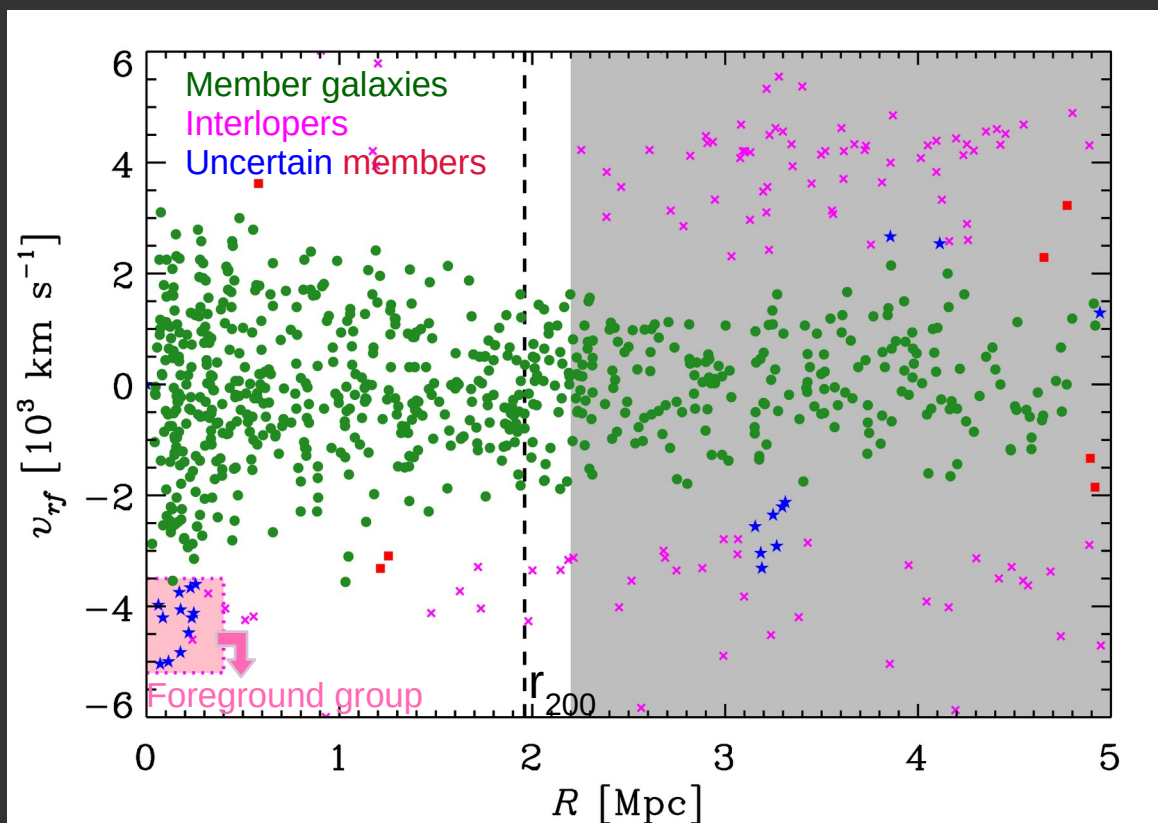
BCG image and velocity dispersion profile

Intra-cluster gas mass profile estimated
from Chandra data

Galaxy stellar masses estimated from
SED fitting to 5-band photometry

Data sets – CLASH clusters AS1063 and MACS1206

MACS1206, $z=0.4398$, $M_{200}=1.4 \cdot 10^{15} M_{\odot}$



Projected phase-space distribution of galaxies;
680 cluster members, of which
476 with $R \leq 1.2 r_{200}$ used in our dynamical analysis

BCG image and velocity dispersion profile

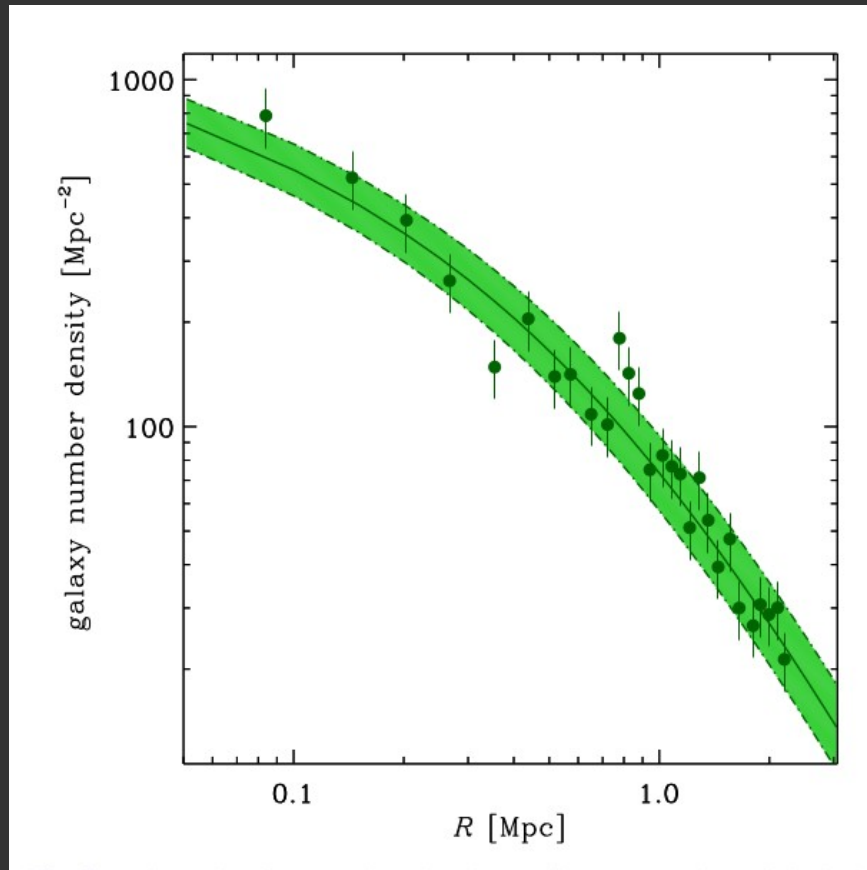
Intra-cluster gas mass profile estimated
from Chandra data

Galaxy stellar masses estimated from
SED fitting to 6-band photometry

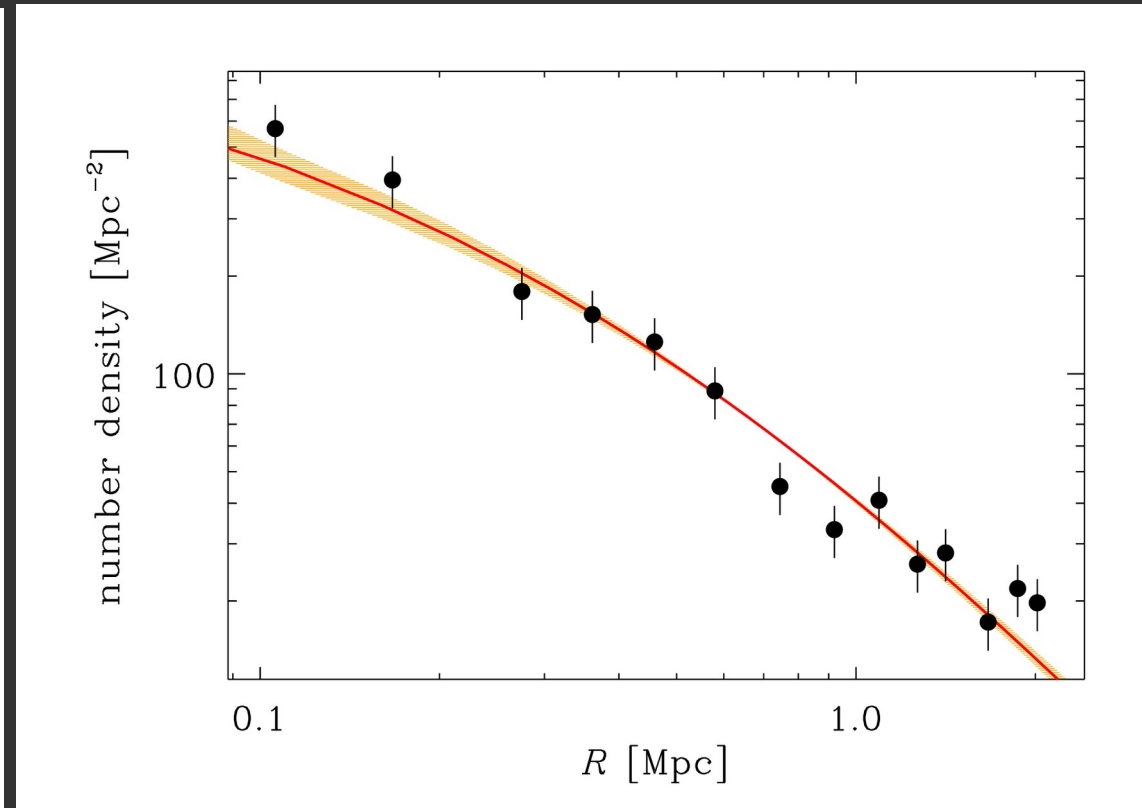
Results – the spatial distribution of cluster galaxies

The galaxy number density profile is a direct observable; it can be fit outside the dynamical analysis of MAMPOSSt.

We use a projected-NFW model, and then de-project it assuming spherical symmetry (Abel inversion) \Rightarrow scale radius of the galaxy distribution r_v



AS1063, $r_v = 0.76 \pm 0.08$ Mpc



MACS1206, $r_v = 0.46 \pm 0.08$ Mpc

Results - MAMPOSSt dynamical analysis: AS1063

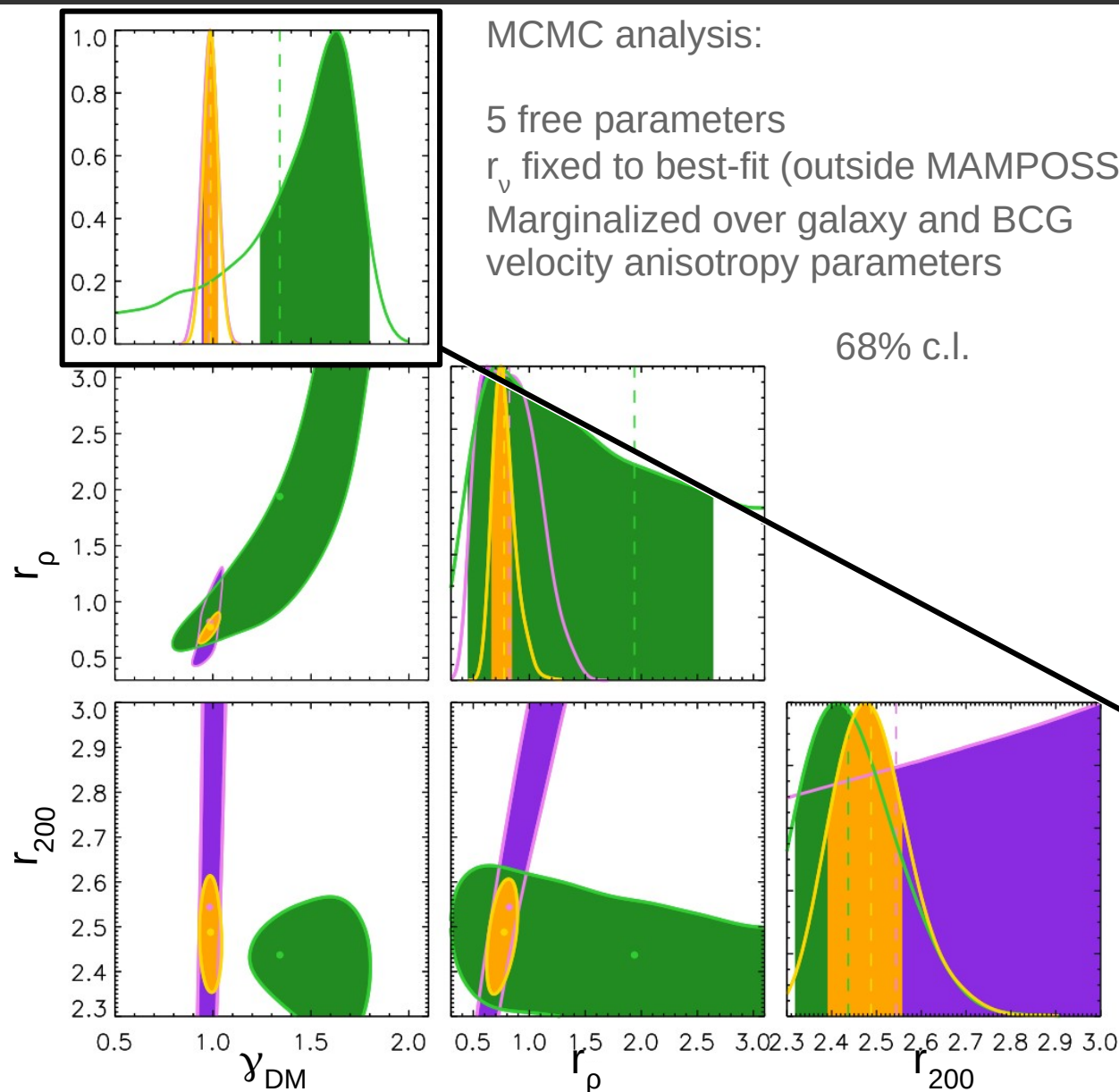
MCMC analysis:

5 free parameters

r_v fixed to best-fit (outside MAMPOSSt)

Marginalized over galaxy and BCG velocity anisotropy parameters

68% c.l.



$$r_{200} = 2.5 \text{ Mpc}$$

$$r_\rho = 0.8 \text{ Mpc}$$

$$M_{BCG} = 1.2 \cdot 10^{12} M_\odot$$

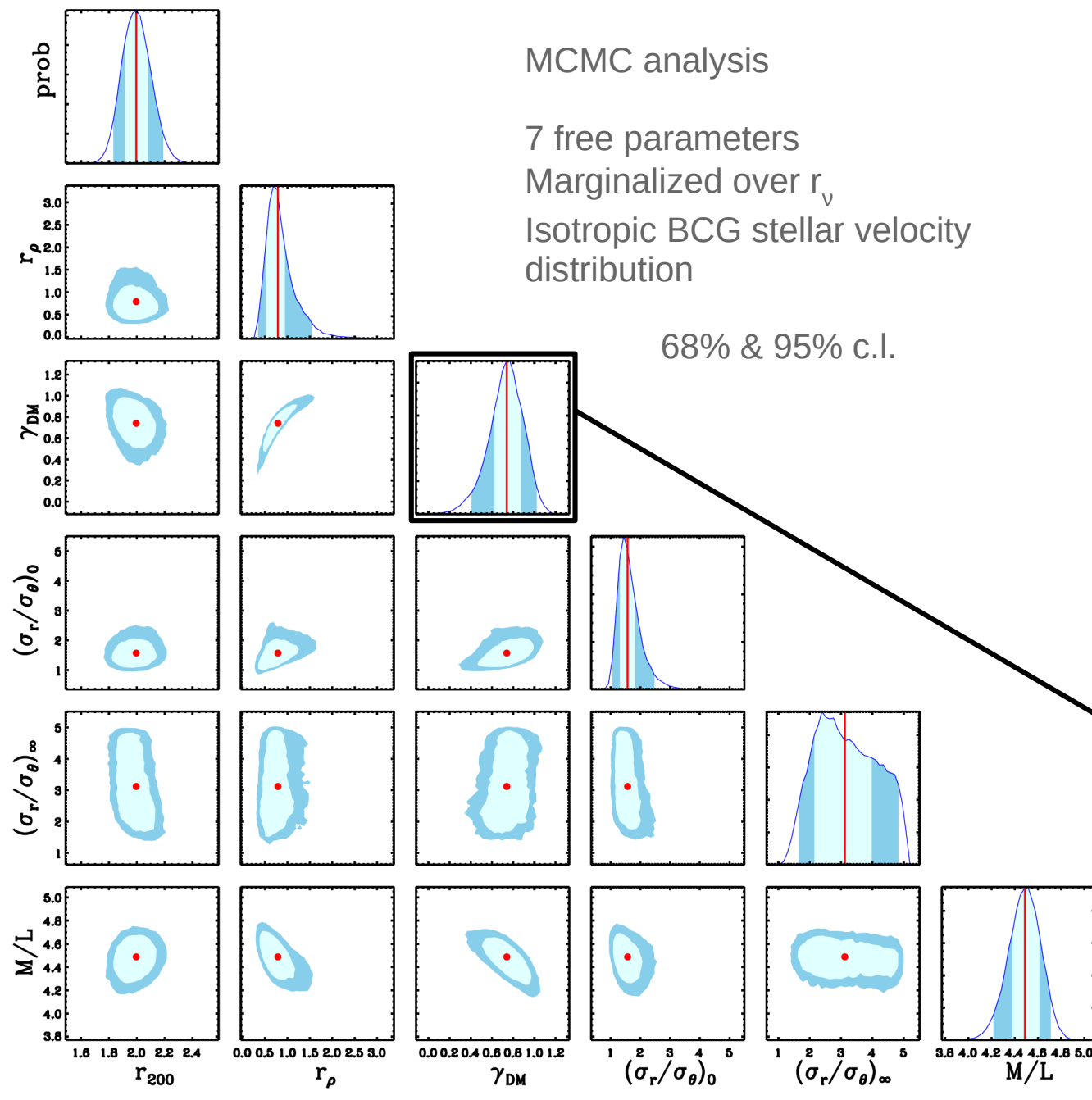
BCG stellar orbits
almost isotropic

Galaxy orbits radially
elongated, increasingly
so at larger radii

$$\gamma_{DM} = 0.99_{-0.04}^{+0.04} (1 \sigma)$$

Constraints from: galaxy velocity distribution, BCG velocity dispersion profile, combined

Results – MAMPOSSt dynamical analysis: MACS1206



$$r_{200} = 2.0 \text{ Mpc}$$

$$r_\rho = 0.9 \text{ Mpc}$$

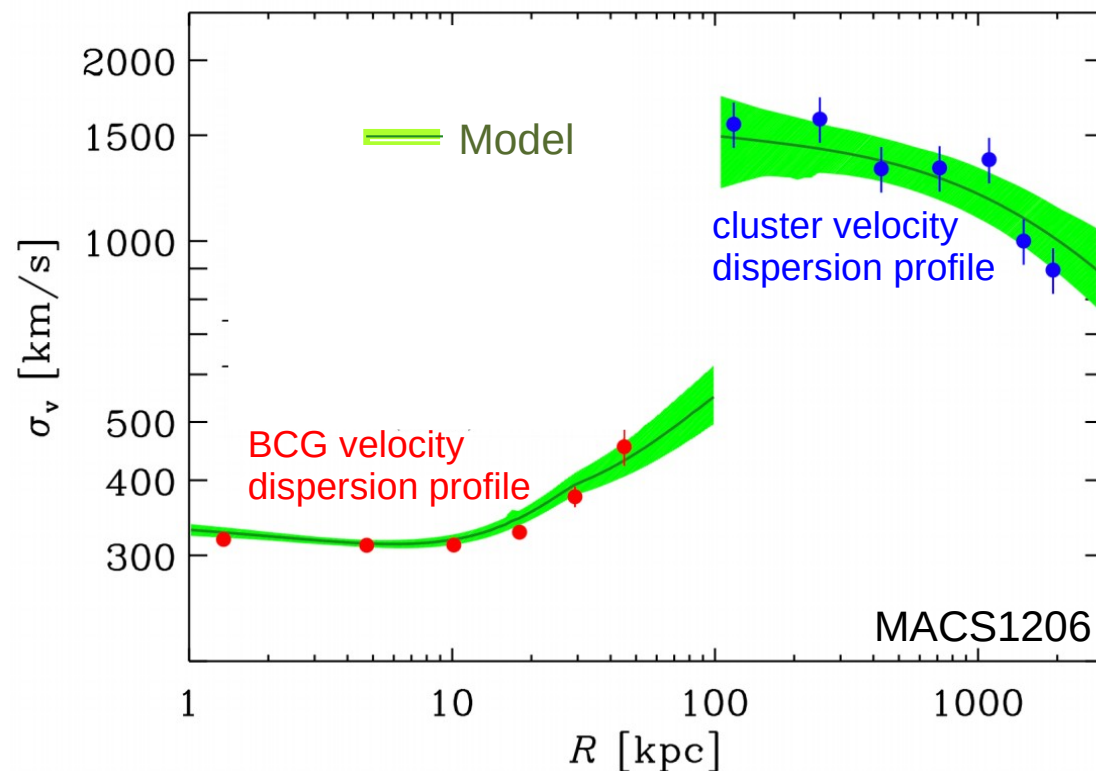
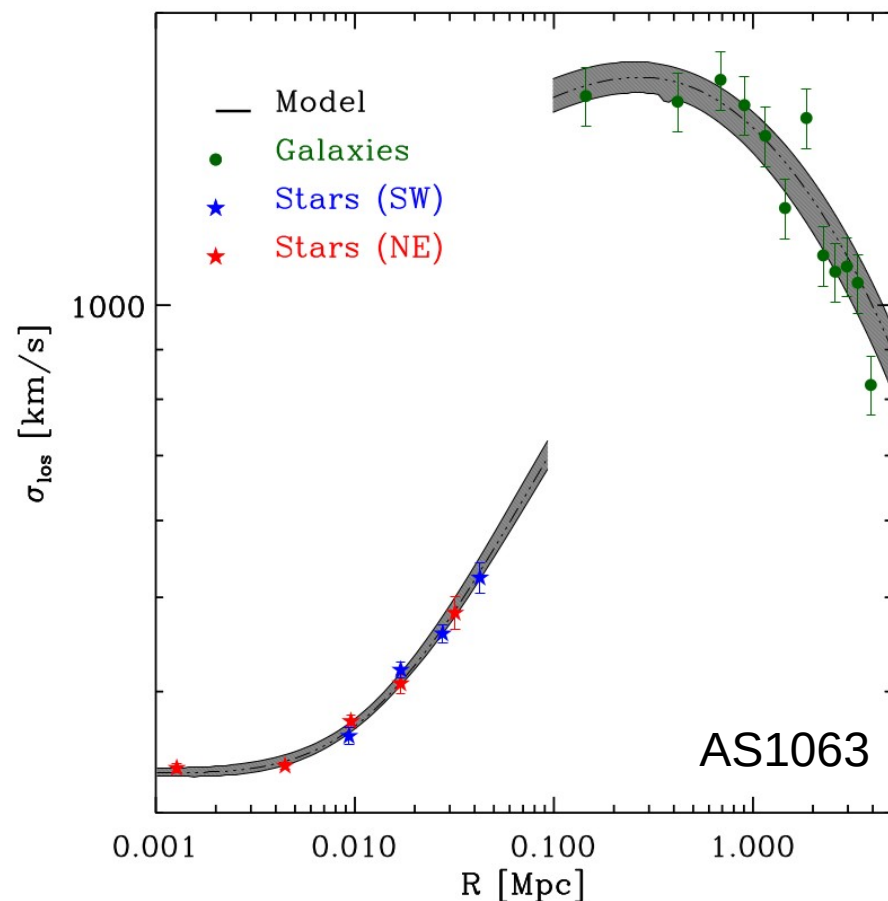
$$M_{BCG} = 2.2 \cdot 10^{12} M_\odot$$

BCG stellar orbits
almost isotropic

Galaxy orbits radially
elongated, increasingly
so at larger radii

$$\gamma_{DM} = 0.73_{-0.14}^{+0.18} (1 \sigma)$$

Results – The velocity dispersion profiles

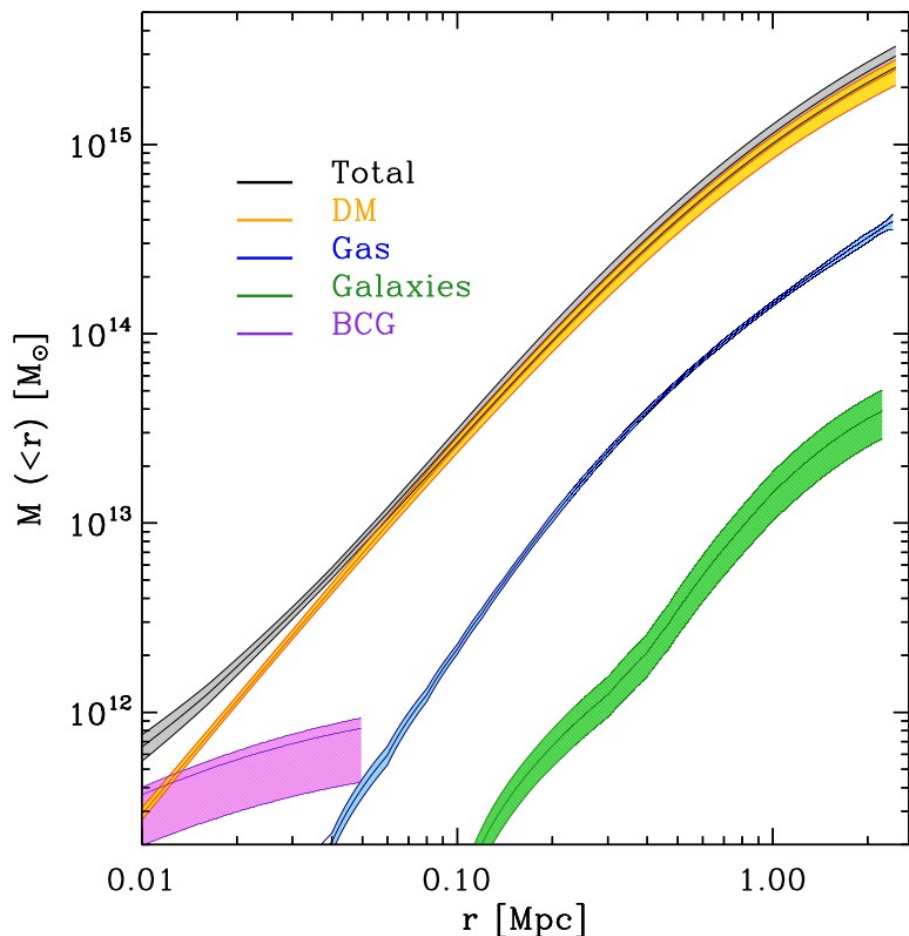


Projecting the best-fit MAMPOSSt solution onto the space of observables:
the velocity dispersion profiles of the BCG and the cluster

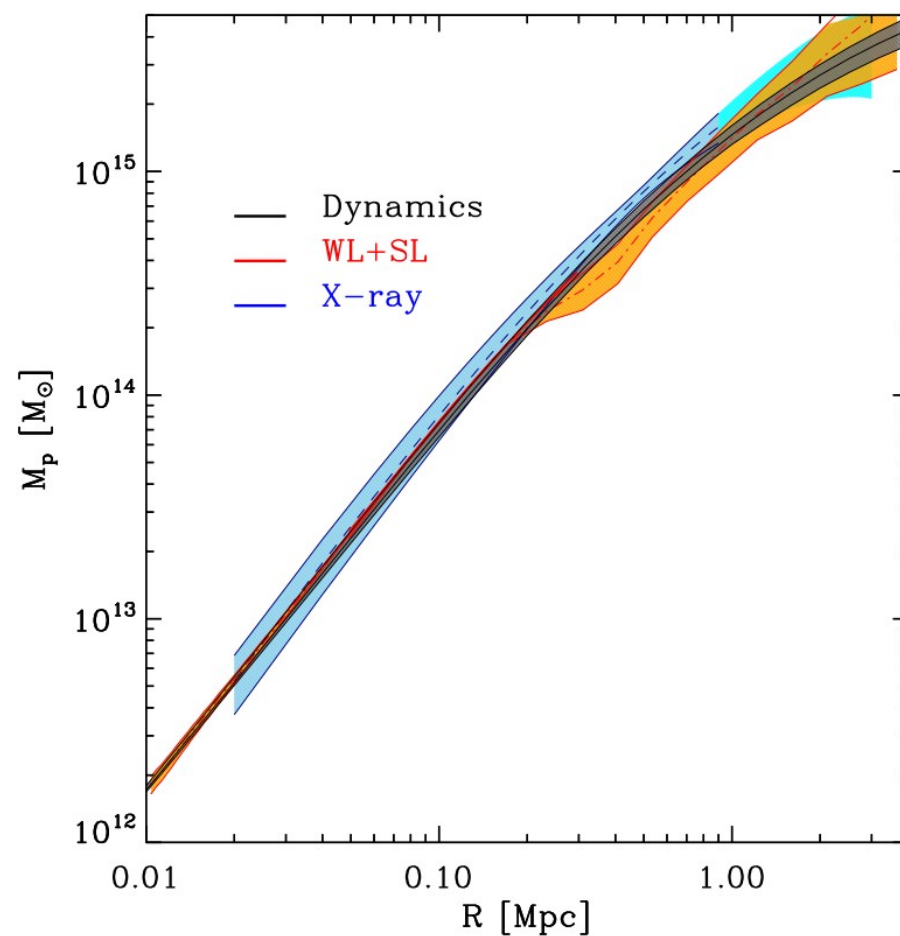
⇒ the MAMPOSSt best fit is a good fit

(Note: the BCG and cluster l.o.s. velocity dispersion profiles do not need to be continuous, since the orbits and density distributions of the BCG stars and the cluster galaxies are \neq)

Results – the mass profiles: AS1063

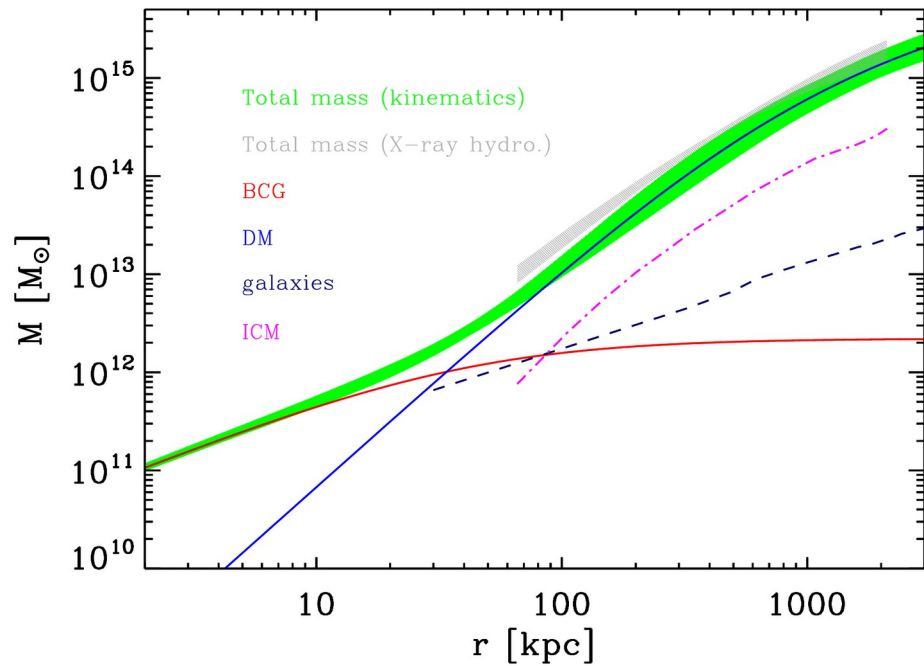


The BCG stellar mass dominates near the center, DM everywhere else

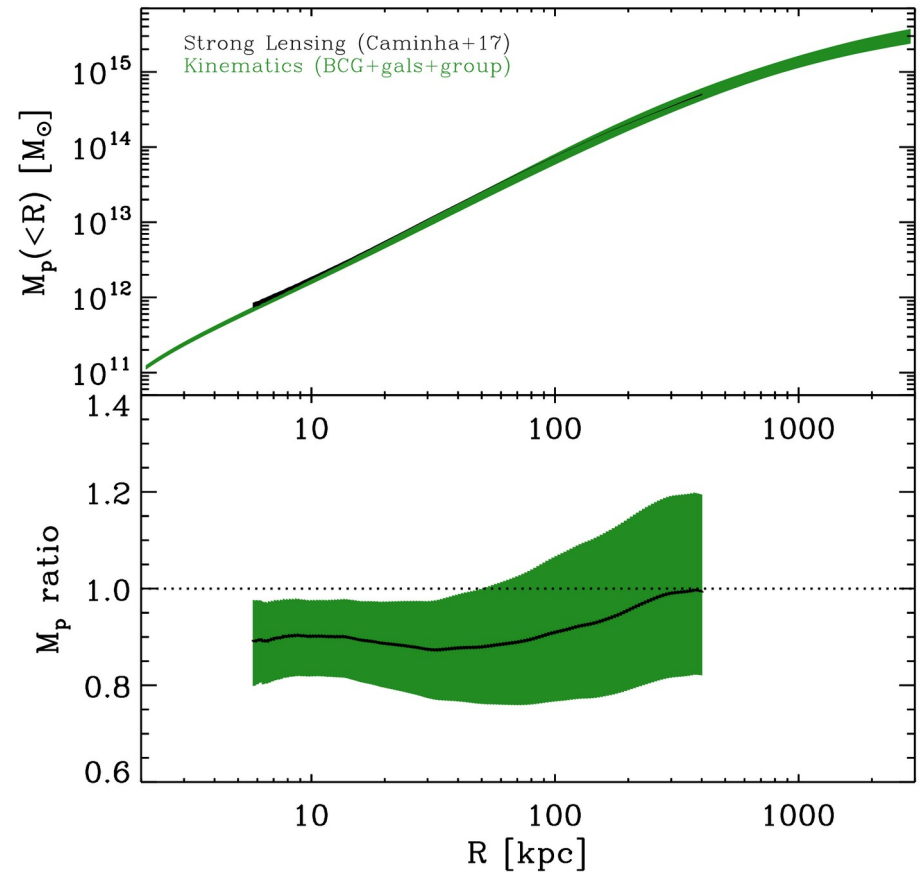


The (projected) total mass profile derived from MAMPOSSt is in good agreement with independent determinations from gravitational lensing and from application of the hydrostatic equilibrium to the intra-cluster plasma

Results – the mass profiles: MACS1206



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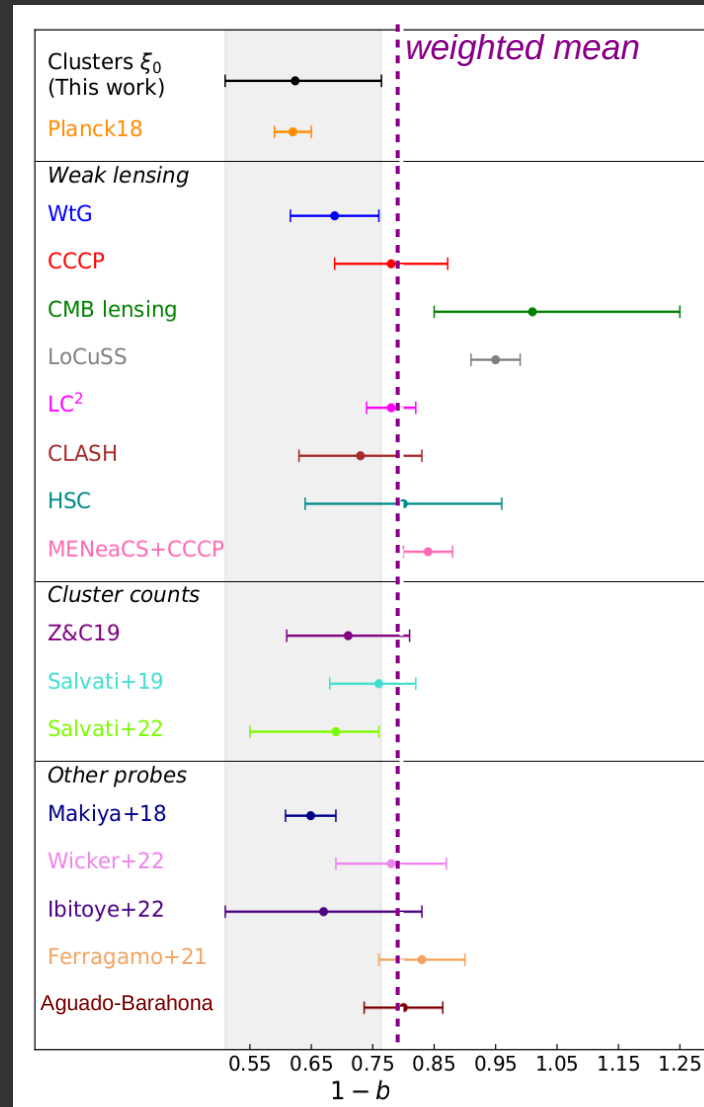
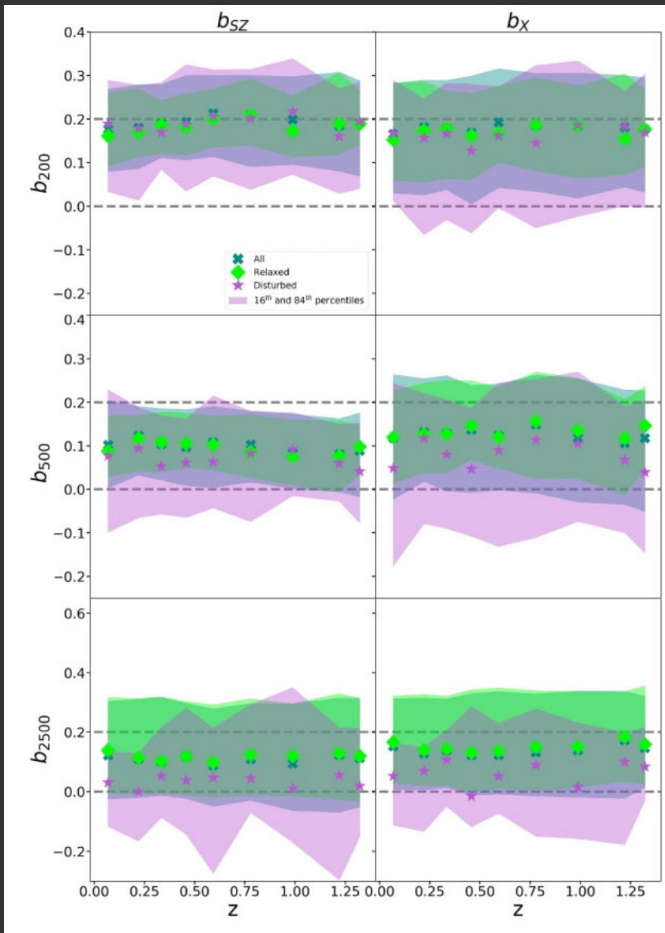


The total mass profile derived from MAMPOSSt is in good agreement with the independent determination from application of the hydrostatic equilibrium to the intra-cluster plasma, and the total (projected) mass profile derived from MAMPOSSt is in good agreement with the independent determination from strong gravitational lensing, once the contribution of a foreground group along the l.o.s. is accounted for

Results – no hydrostatic mass bias?

Inconsistency between Planck base-cosmology and Planck SZ cluster counts cosmology
 ⇒ cluster masses from X-ray data (assuming hydrostatic equilibrium of Intra-Cluster gas)
 must be biased low, $b = 1 - M_X / M_{\text{true}} = 0.38 \pm 0.03$ (Planck coll. 2020, VI)

Simulations (the Three Hundred)
 indicate smaller values $b \approx 0.1-0.2$
 (Gianfagna+23)



Observations indicate
 $\langle b \rangle = 0.22 \pm 0.03$
 (compilation by Lesci+23)

AS1063 and MACS1206:

The good agreement
 between MAMPOSSt $M(r)$
 and $M(r)$ from X-ray data
 (hydrostatic eq. IC gas)
do NOT support $b > 0$



(Ongoing analysis of other
 CLASH-VLT clusters)

Results – the inner slope of the DM density profile

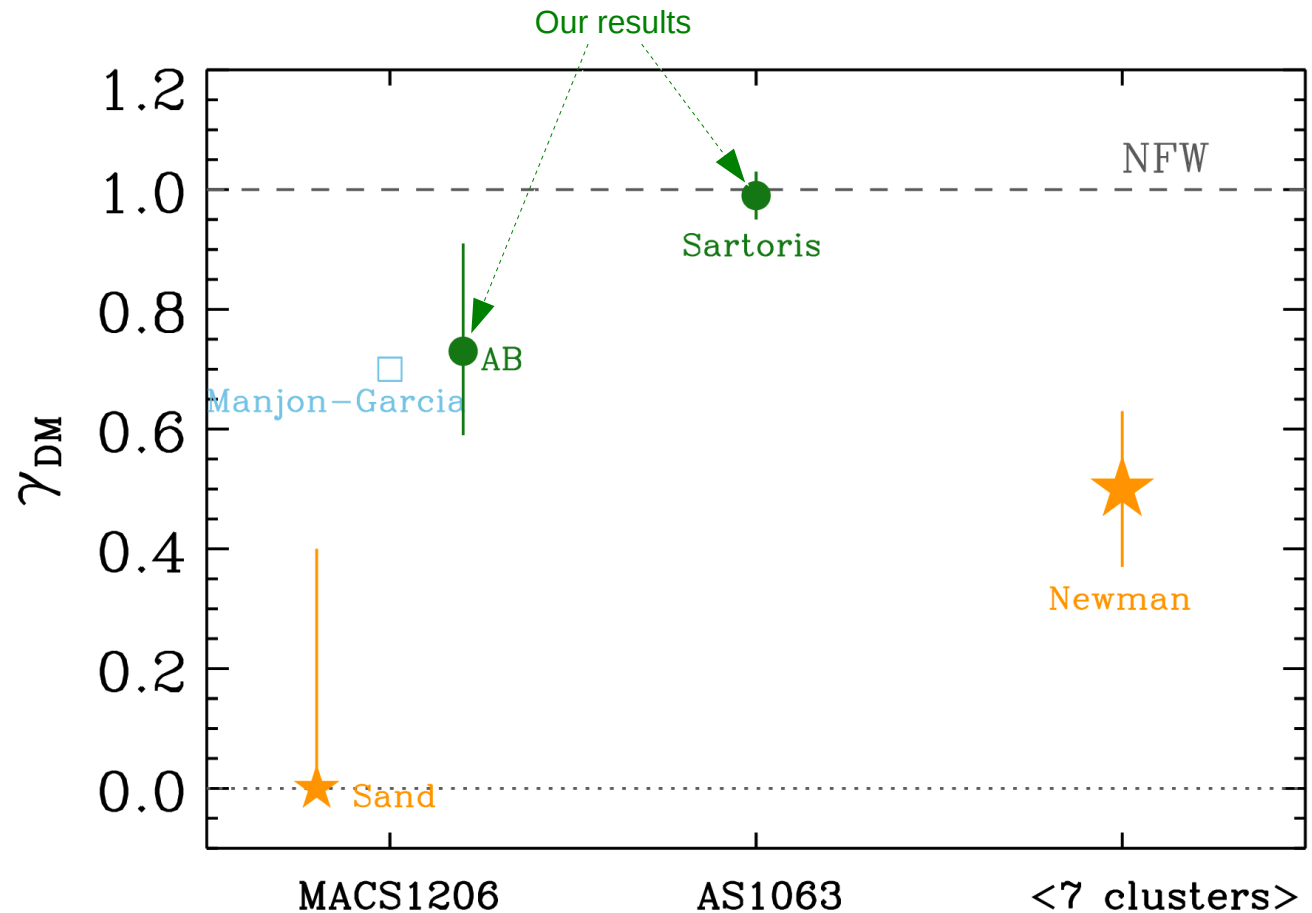
Previous results, based on cluster strong lensing + (in some cases) BCG kinematics:

Newman+13: $\gamma_{\text{DM}} < 1$ for 8 clusters; Sand+04: $\gamma_{\text{DM}} = 0$ for MACS1206 (supported by Limousin+22);

Manjon-Garcia+22: higher γ_{DM} value for MACS1206, but no error estimate given

Kelson+02: inner core in the DM distribution of A2199

Our results, based on BCG and cluster galaxies kinematics, are closer to NFW prediction, $\gamma_{\text{DM}} \approx 1$

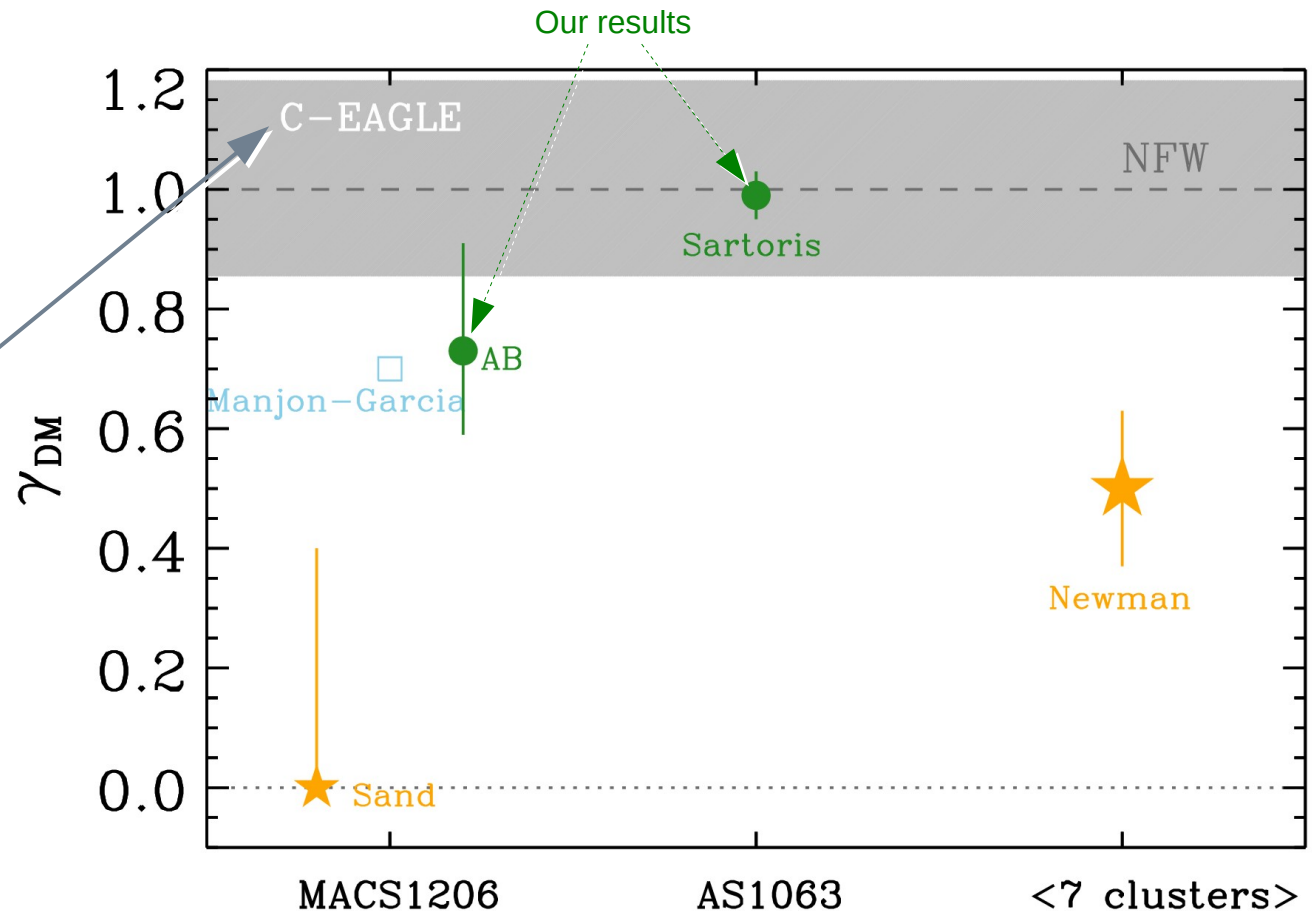


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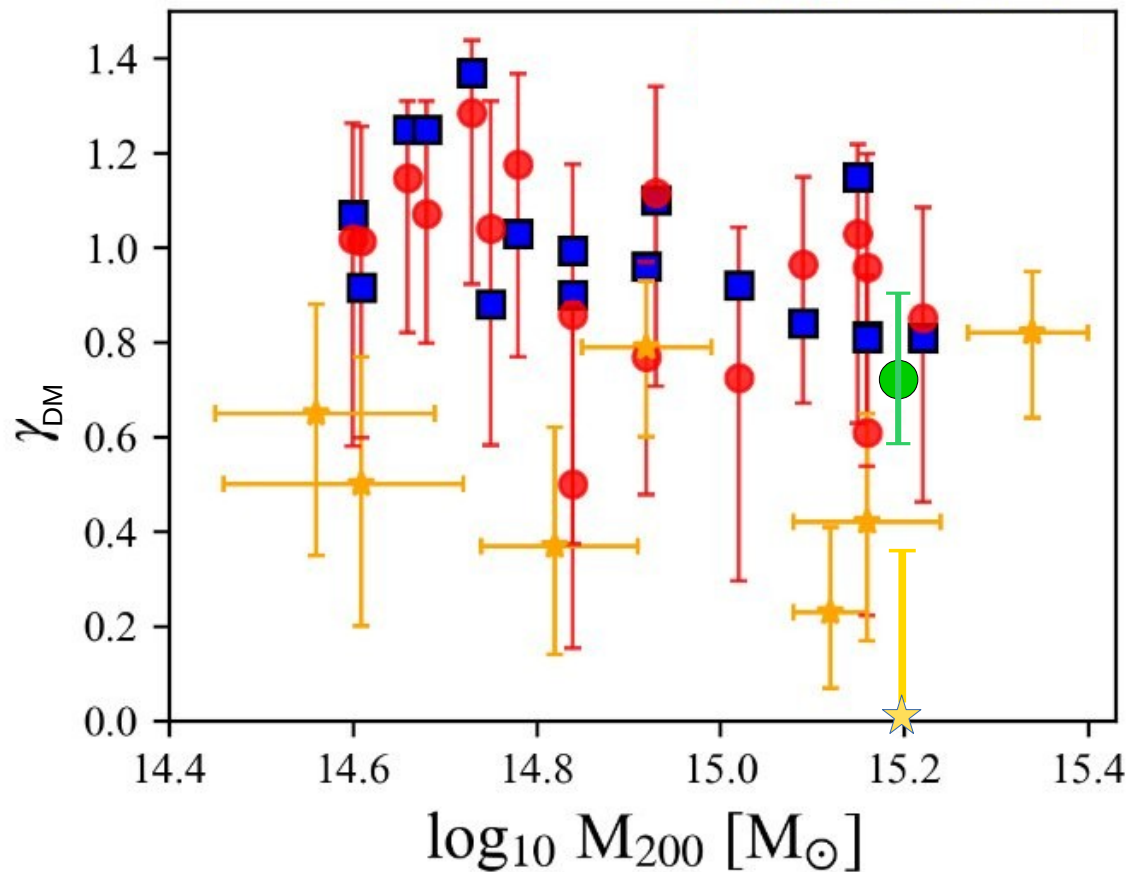
Our results agree with recent predictions from the C-EAGLE hydrodynamical simulations (He+20)



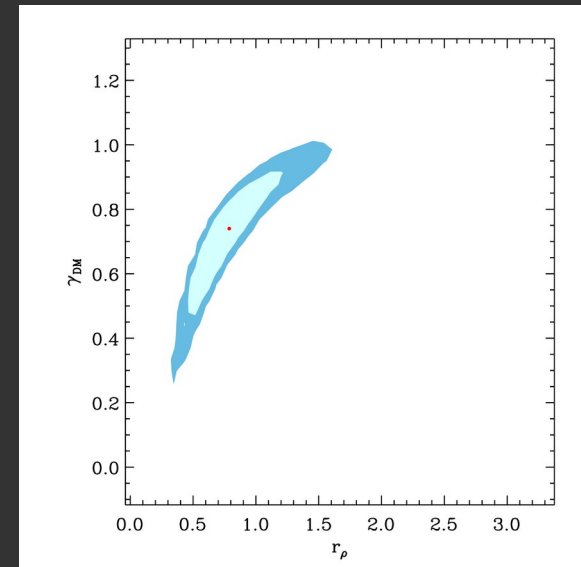
Discussion – the inner slope of the DM density profile

Cmp with C-EAGLE simulations (*He+20*)

A possible problem in SL-based γ_{DM} determinations: to estimate γ_{DM} correctly, one also need a good estimate of the $M(r)$ scale radius, r_ρ . because of covariance:



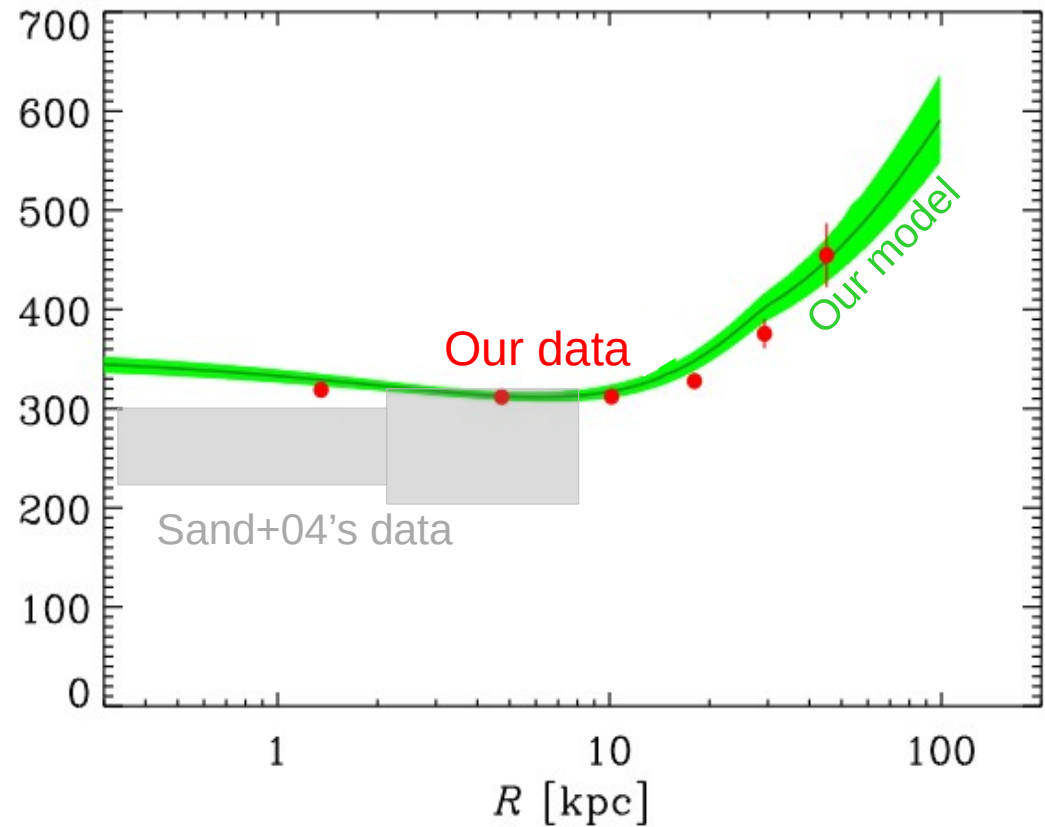
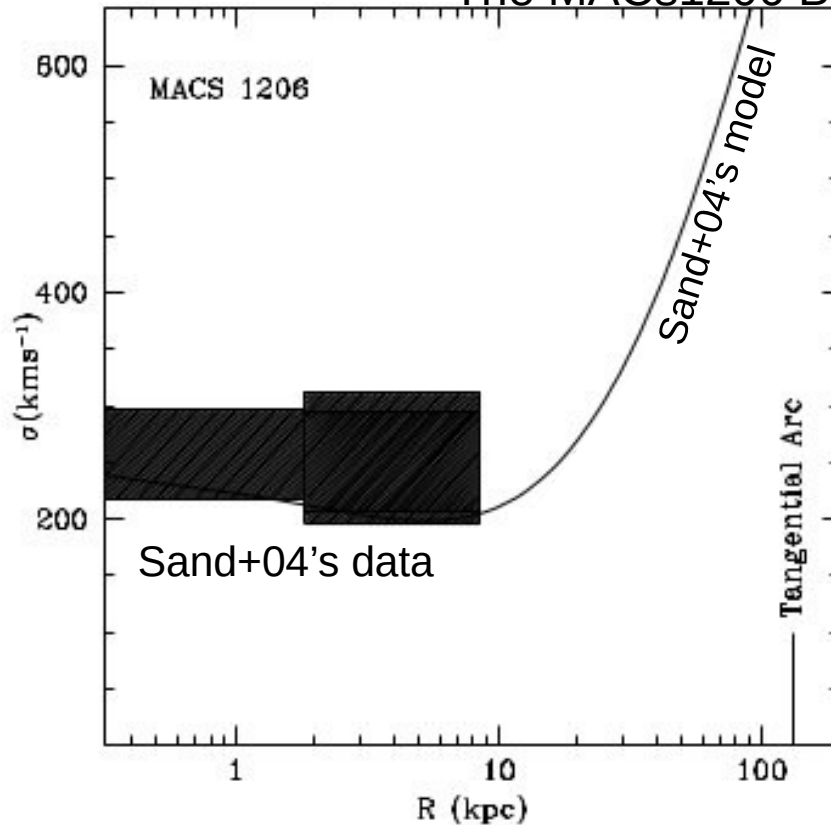
- our results {
- AS1063 (*Sartoris, AB + 20*)
 - MACS 1206.2-0847 (*AB submitted*)
 - simulated unbiased observations
 - intrinsic simulated values
 - ★ previous results (*Newman+13, Sand+04*)



Need to sample the cluster potential at radii well beyond r_ρ ; the kinematic data for cluster galaxies reach well beyond r_ρ , but Strong Lensing data do not

Discussion – the inner slope of the DM density profile

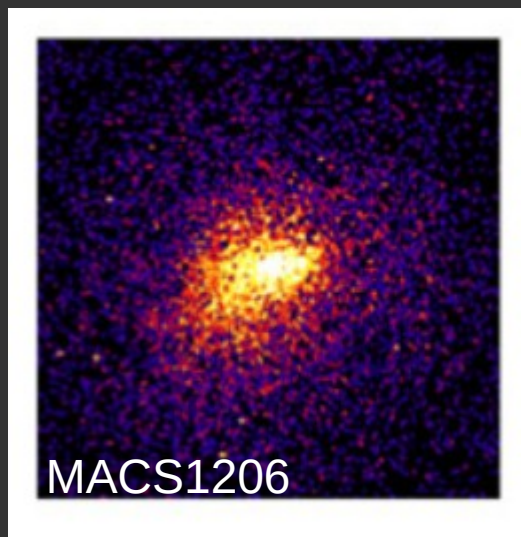
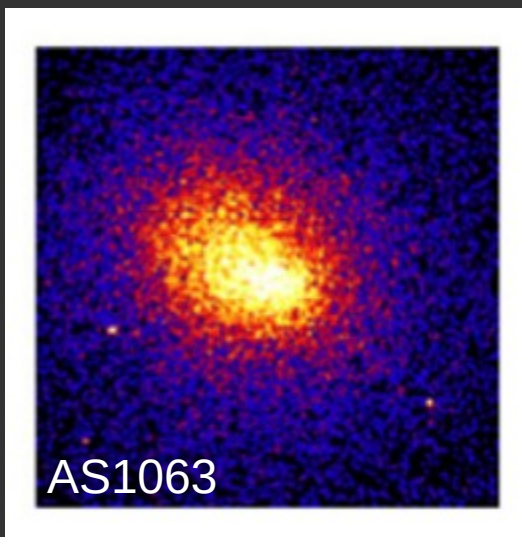
The MACs1206 BCG velocity dispersion profile



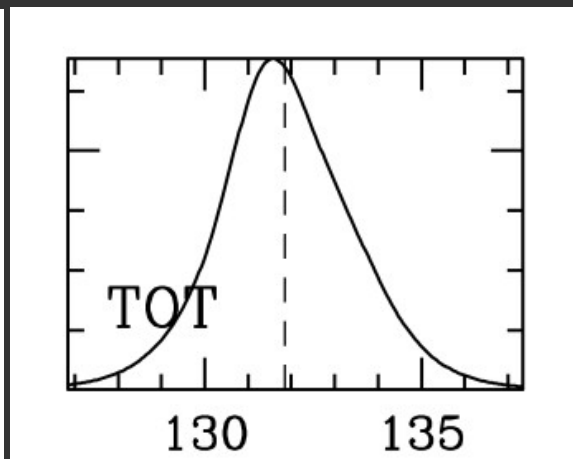
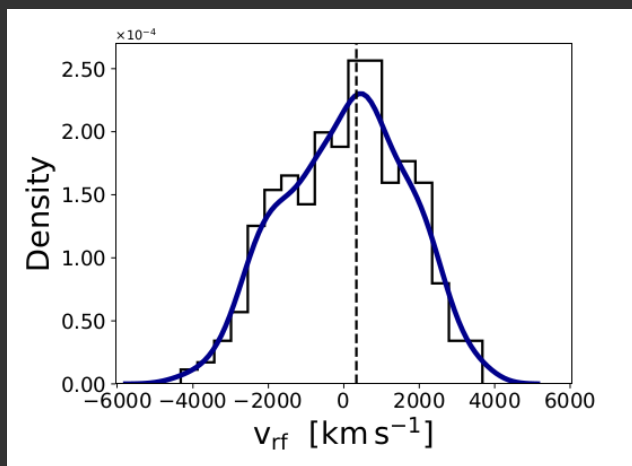
At least part of the reason of the DM difference between Sand+04's result and ours can be ascribed to the different BCG velocity dispersion profile determinations,
better data \Rightarrow better results

Discussion – systematics

We assume dynamical equilibrium for AS1063 and MACS1206 – is this justified?



CLASH clusters originally selected to look “relaxed” in Chandra X-ray images (Postman+12: well defined central surface brightness peak + nearly concentric isophotes) 😊



AS1063: BCG velocity \approx cluster mean, 😊
but velocity distribution is not Gaussian (Mercurio+21) 😞

MACS1206: BCG velocity \approx cluster mean;
Gaussian velocity distribution (Girardi+15)



Good agreement between masses from kinematics and masses from lensing
(the latter do not make any assumption about dynamical relaxation)



Discussion – systematics

We assume spherical symmetry for AS1063 and MACS1206 – is this justified?

Clusters are not spherical. Triaxiality induces a systematic uncertainty.

Combining X-ray, Sunyaev-Zel'dovich, lensing data or modeling strong+weak lensing data
⇒ constrain elongation and orientation of main halo (*e.g. Limousin+13, Chiu+18*)

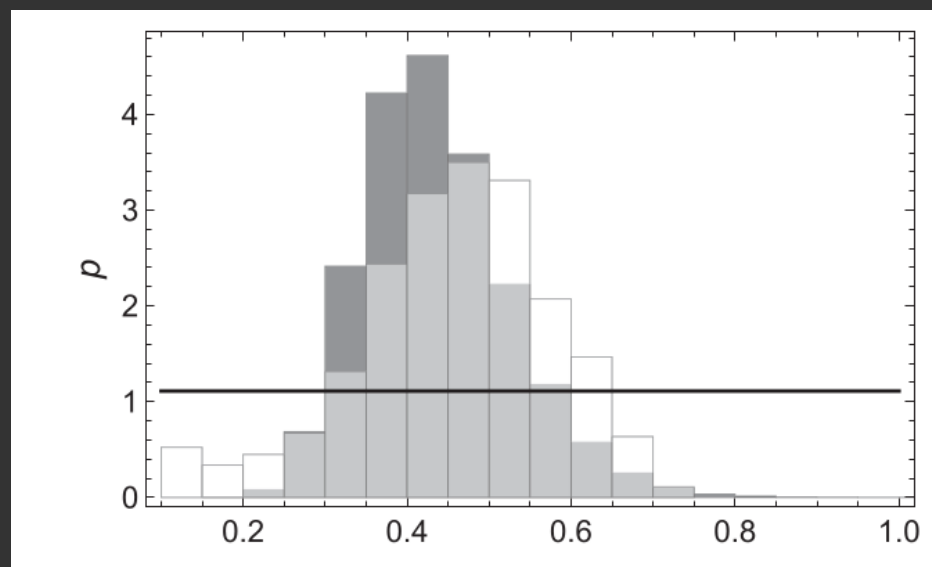
AS1063, from strong+lensing modeling has minor/major axis ratio 0.5 ± 0.2 (*Chiu+18*)

MACS1206, from S+L modeling has $0.6_{-0.1}^{+0.4}$ (*Chiu+18*)

higher than, but consistent with estimate obtained adding X-ray and SZ data (*Sereno+17*)

These are average values for cluster-size halos, and MAMPOSSt has been tested on random sets of cluster-size halos, irrespective of their sphericity 😊

An over-estimate of γ_{DM} could result from an orientation of the cluster major axis along the line-of-sight; but the BCGs and X-ray projected shapes of AS1063 and MACS1206 argue **against** such a geometry 😊



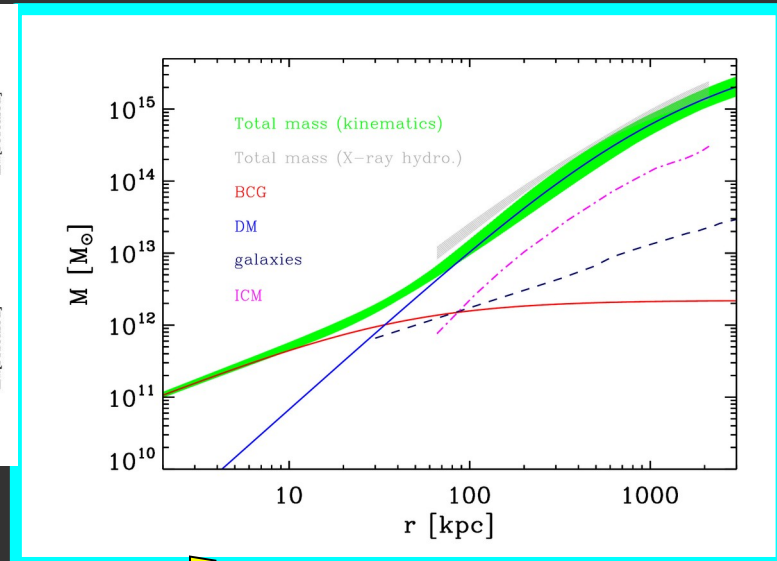
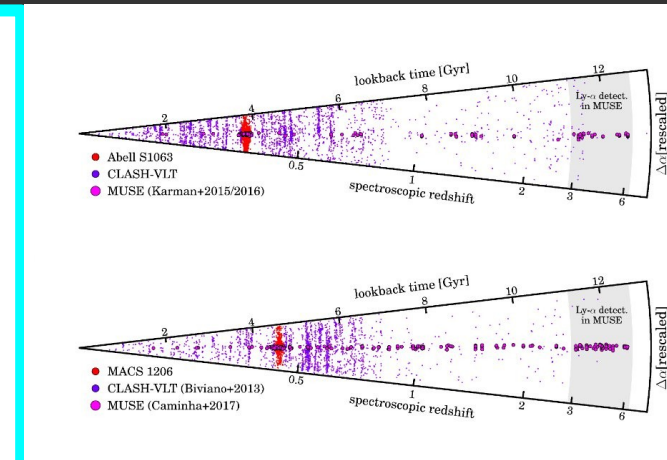
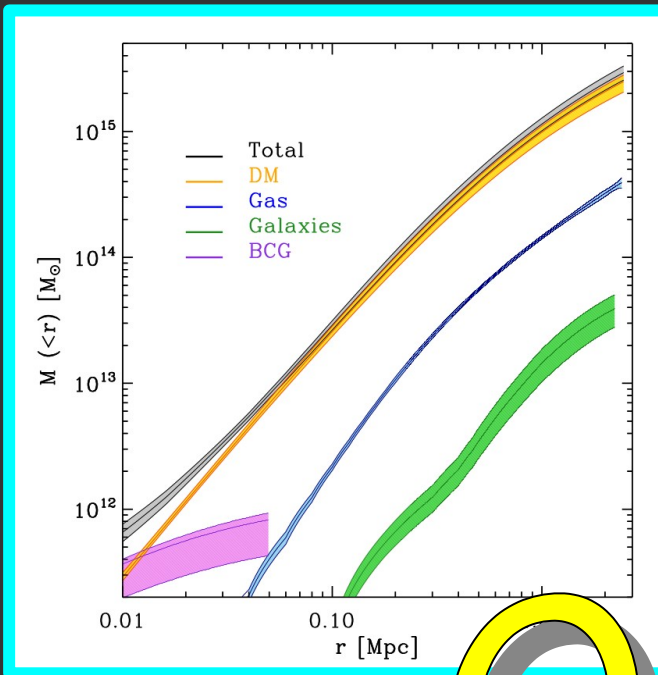
Probability distribution of the
MACS1206 minor-to-major axis ratio
(Sereno+17)

Summary and perspectives

- We combine the kinematics of the Brightest Cluster Galaxy stars and of the cluster galaxies for two massive CLASH-VLT clusters at $z \sim 0.3-0.4$ to determine their DM radial profile
- The total mass profile from kinematics agrees with those inferred from lensing, an indication that the two clusters are in dynamical equilibrium, and with that inferred from applying the hydrostatic equation to the intra-cluster gas, an indication that there is little, if any, “hydrostatic mass bias”
- The DM profiles have inner slopes $\gamma_{\text{DM}} = 0.7-1.0$, consistent with recent results from hydrodynamical Λ CDM simulations (C-EAGLE), rejecting previous claims of significant inconsistency with $\gamma_{\text{DM}}=1$ (NFW) on the cluster scale

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- Extend this analysis to another ~ 5 CLASH-VLT clusters with BCG MUSE data, + data from the literature for more nearby clusters
- Analyse all 12 CLASH-VLT clusters for constraining the X-ray mass hydrostatic bias
- MAMPOSSt constrains $M(r)$ but also the velocity anisotropy $\beta(r)$ (of cluster galaxies and BCG stars): find the mean velocity anisotropy profile of clusters and its variance and constrain the velocity anisotropy of their BCG stars



Obrigado!

