

# Cluster density profiles and orbits of galaxies from dynamical analysis

Andrea Biviano, INAF/Oss.Astr.Trieste

# Collaborators & papers:

## *on the observational side:*

A.B. & M. Girardi 2003,  
P. Katgert, A.B. & A. Mazure 2004,  
A.B. & P. Katgert 2004,  
A.B. & P. Salucci 2006,  
A.B., G. Mamon, T. Ponman in prep.,  
A.B., A. Diaferio, K. Rines in prep.

## *on the numerical side:*

A.B., G. Murante, S. Borgani, A. Diaferio, K. Dolag,  
& M. Girardi 2006 & in prep.

# Aims:

## 1. Constrain $M(r)$ of galaxy systems

- central cusp or core?
- external slope?
- influence of baryons?

## 2. How do galaxies move in their systems?

- evidence of infall?
- relaxation processes?

# Tracers of the grav. potential: *galaxies*

## Observables:

$R_i$  radial distance of i-th galaxy from the cluster center

$V_i$  rest-frame l.o.s. velocity wrt the cluster  $\langle V \rangle$

*Because of poor sampling of single clusters  
and deviation from spherical symmetry...*

→ **Combine many clusters using  $M_{200}$**

$$R_n = R/r_{200} \quad \& \quad V_n = (V - \langle V \rangle) / v_{200}$$

$M_{200}$  from  $\sigma_v$  (virial theorem)

or  $T_x$  (scaling relations) when  $N_{gal}$  small

# *Why using the cluster galaxies to determine the total mass profile?*

- less direct than lensing and X-ray ↓
- sample mass profile to larger radii ↑
- IC gas not fully thermalized (?) ↑  
*(Rasia et al. 2004, Faltenbacher et al. 2005)*
- lensing inefficient for nearby clusters ↑  
*(Natarajan & Kneib 1997)*

...and in any case, 3 is better than 1!

# METHODS



An example of YDS climbing class 1

# M( $<r$ ): methods:

## 1. Jeans analysis

*(e.g. Binney & Tremaine 1987; see also Mamon & Boué 2007)*

- *Works better in central cluster regions*
- *Degeneracy mass profile - velocity anisotropies*

## 2. Caustic method

*(Diaferio & Geller 1997; see also Diaferio 1999)*

- *Works better in external cluster regions*
- *Only mild dependence on velocity anisotropies*

# M(<r) from the Jeans analysis

Assumes dynamical equilibrium of the system

$I(R)$  and  $\sigma_p(R) \leftrightarrow v(r), \sigma_r(r), M(<r)$ , through  $\beta(r)$

or, more generally:  $f_p(R,v) \leftrightarrow \Phi(r) + f(E,L^2)$

Mass – orbits degeneracy:

given  $R,v$  the  $M(<r)$  solution depends on  $\beta(r)$

( $\beta(r) \equiv 1 - \sigma_t^2/\sigma_r^2$ , velocity anisotropy profile)

Our adopted solutions to this problem:

- analysis of the shape of the velocity distribution
- Use  $\geq 2$  independent tracers of the cluster potential

# The Jeans equation

$$M(r) = -\frac{r \langle v_r^2 \rangle}{G} \left( \frac{d \ln v}{d \ln r} + \frac{d \ln \langle v_r^2 \rangle}{d \ln r} + 2\beta \right)$$

*r*, clustercentric radial distance

$\langle v_r^2 \rangle$ , or  $\sigma_r$ , radial component of velocity dispersion

*v*, number density of cluster galaxies

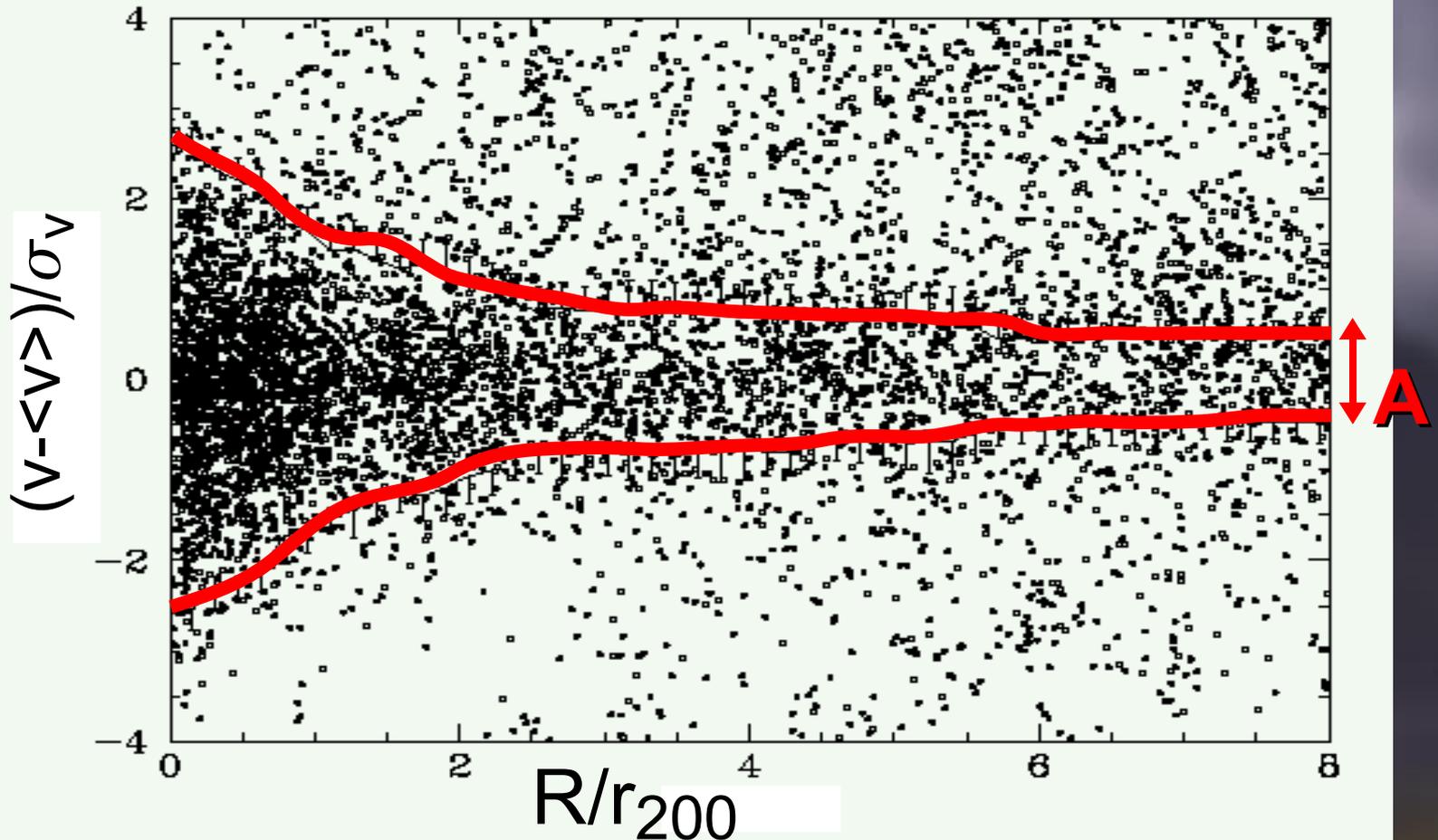
$\beta$ , velocity anisotropy:

$$\beta(r) \equiv 1 - \frac{\langle v_t^2 \rangle}{\langle v_r^2 \rangle}$$

# M(<r) from the caustic method:

*Based on num.sims.: from caustic amplitude  $A(r) \rightarrow \Phi(r)$  through  $F(\Phi, \beta, r) \approx \text{const}$  ...outside the center, independent of dynamical status of the cluster*

*(from Rines et al. 2003)*



# Galaxy orbits: methods:

## 1. Inverse Jeans analysis

*(Binney & Mamon 1982, see also Solanes & Salvador-Solé 1990)*

*Given  $M(r)$ , invert Jeans eq.  $\Rightarrow \beta(r)$*

## 2. Moments of velocity distribution

*(e.g. Merritt 1987, see also van der Marel et al. 2000)*

*Determine 4<sup>th</sup> and 6<sup>th</sup> moments by Gauss-Hermite polynomial decomposition*

# SAMPLES



An example of YDS climbing class 2

# Samples (all at $\langle z \rangle \approx 0$ ):

## 1. ENACS (*Katgert et al. 1996*)

59 clusters,  $\langle \sigma_v \rangle = 699$  km/s,  $\approx 2700$  gal.s within  $r_{200}$

## 2. CIRS (*based on SDSS; Rines & Diaferio 2006*)

65 clusters,  $\langle \sigma_v \rangle = 617$  km/s,  $\approx 3300$  gal.s within  $r_{200}$

## 3. 2dFGRS (*B. & Girardi 2003*)

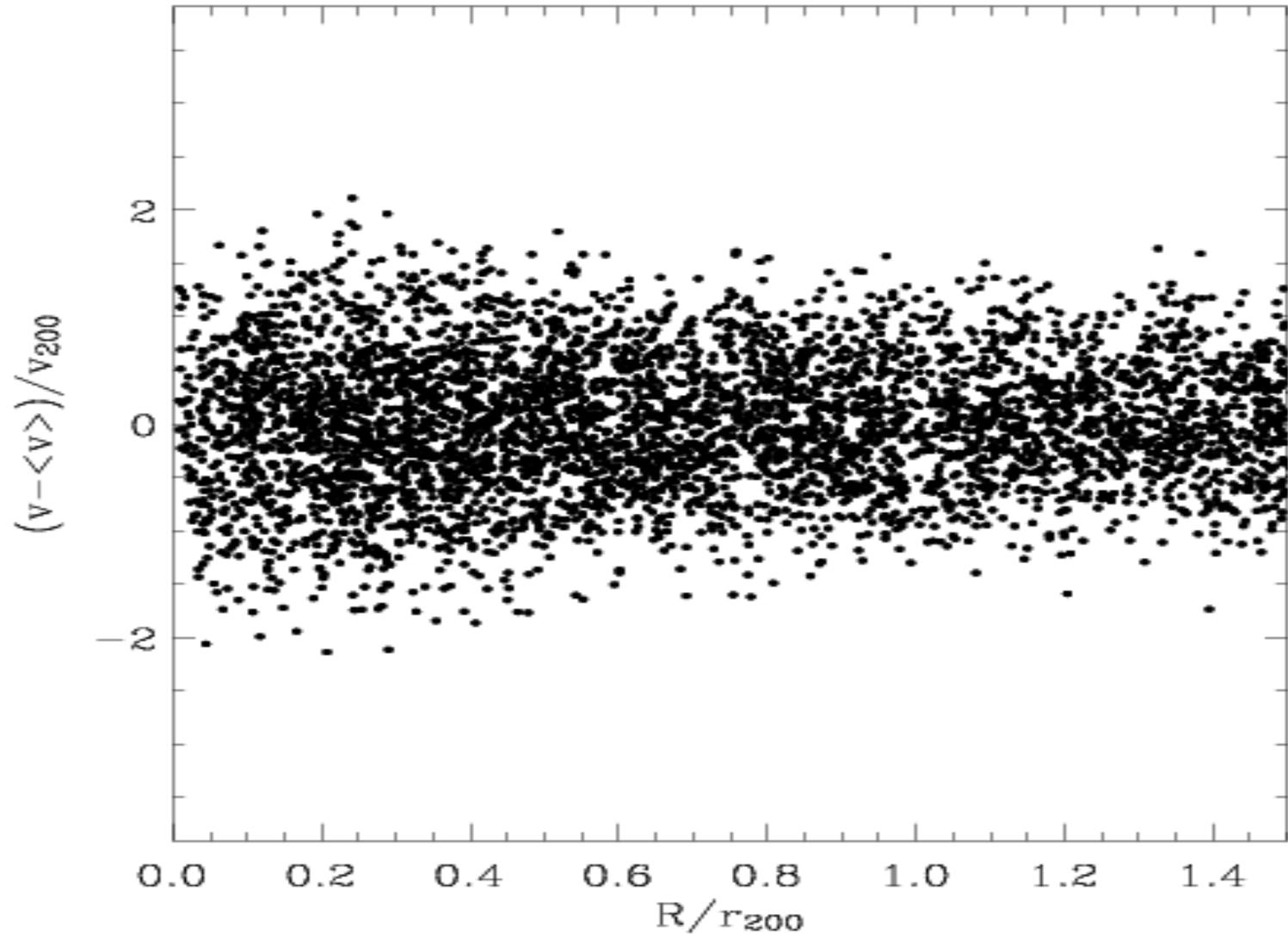
43 clusters,  $\langle \sigma_v \rangle = 490$  km/s,  $\approx 700$  gal.s within  $r_{200}$

## 4. GEMS (*Osmond & Ponman 2002*)

31 groups with measured  $T_x$ ,

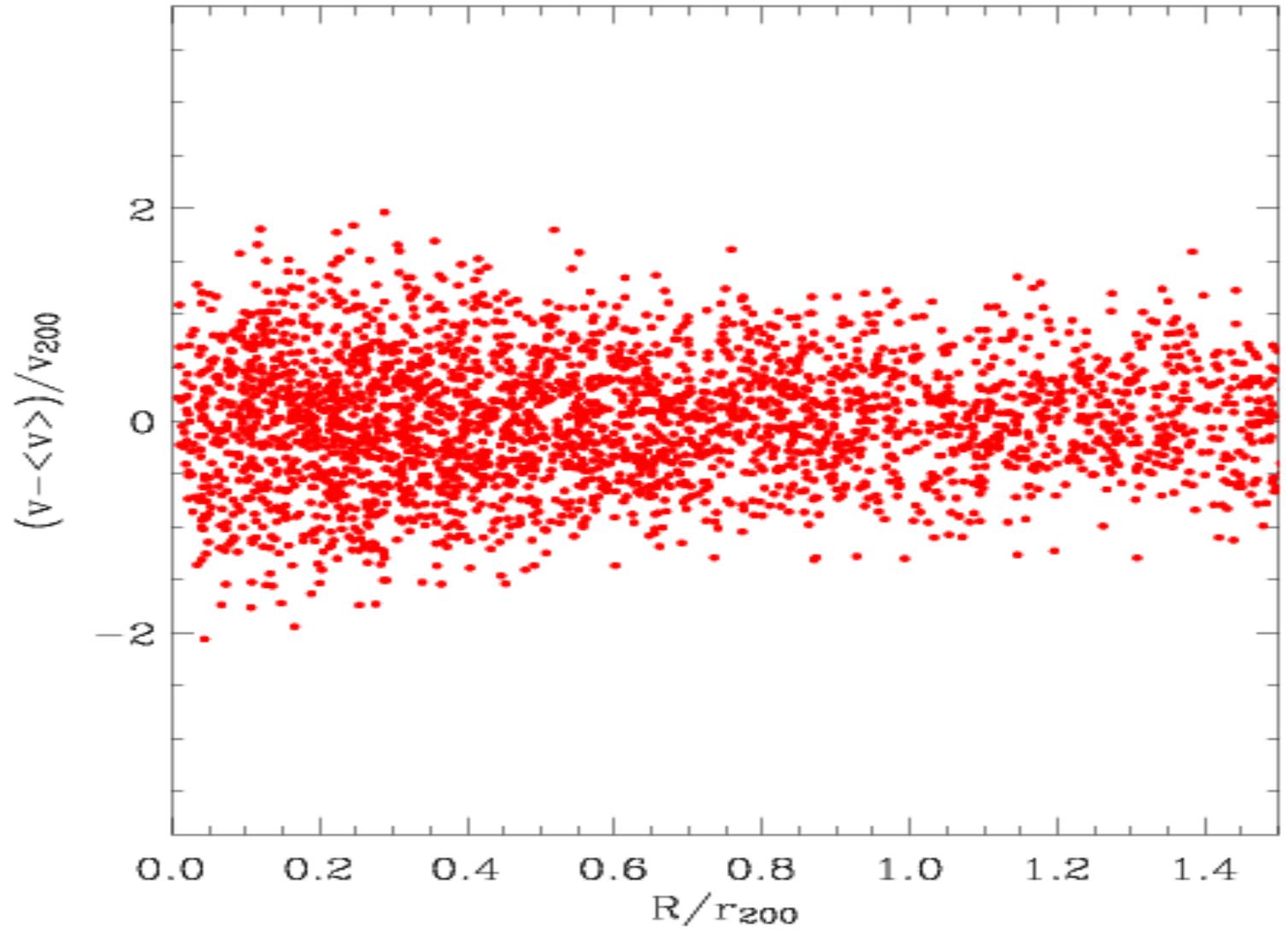
$\langle \sigma_v \rangle = 370$  km/s,  $\approx 700$  gal.s within  $r_{200}$

# Stacked CIRS cluster in $R_n, V_n$ space



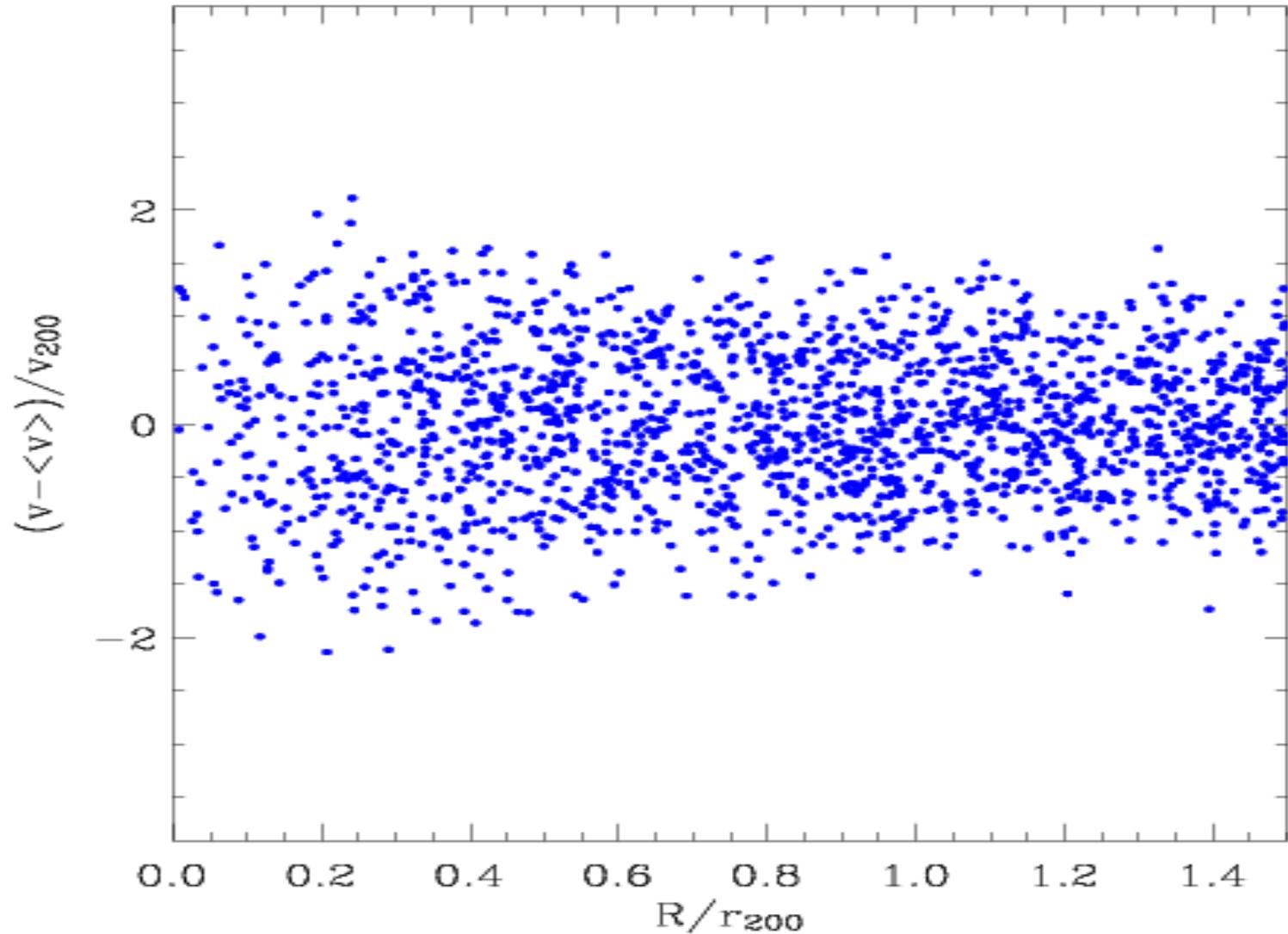
# Stacked CIRS cluster in $R_n, V_n$ space

Red (CM sequence) galaxies only



# Stacked CIRS cluster in $R_n, V_n$ space

Blue galaxies only



# MASS PROFILES

cored or cuspy? external slope?



An example of YDS climbing class 3

# Fit models to the $V_c(r)$ profiles

The **cuspy model of NFW**, motivated by cosmological num. simulations with CDM:

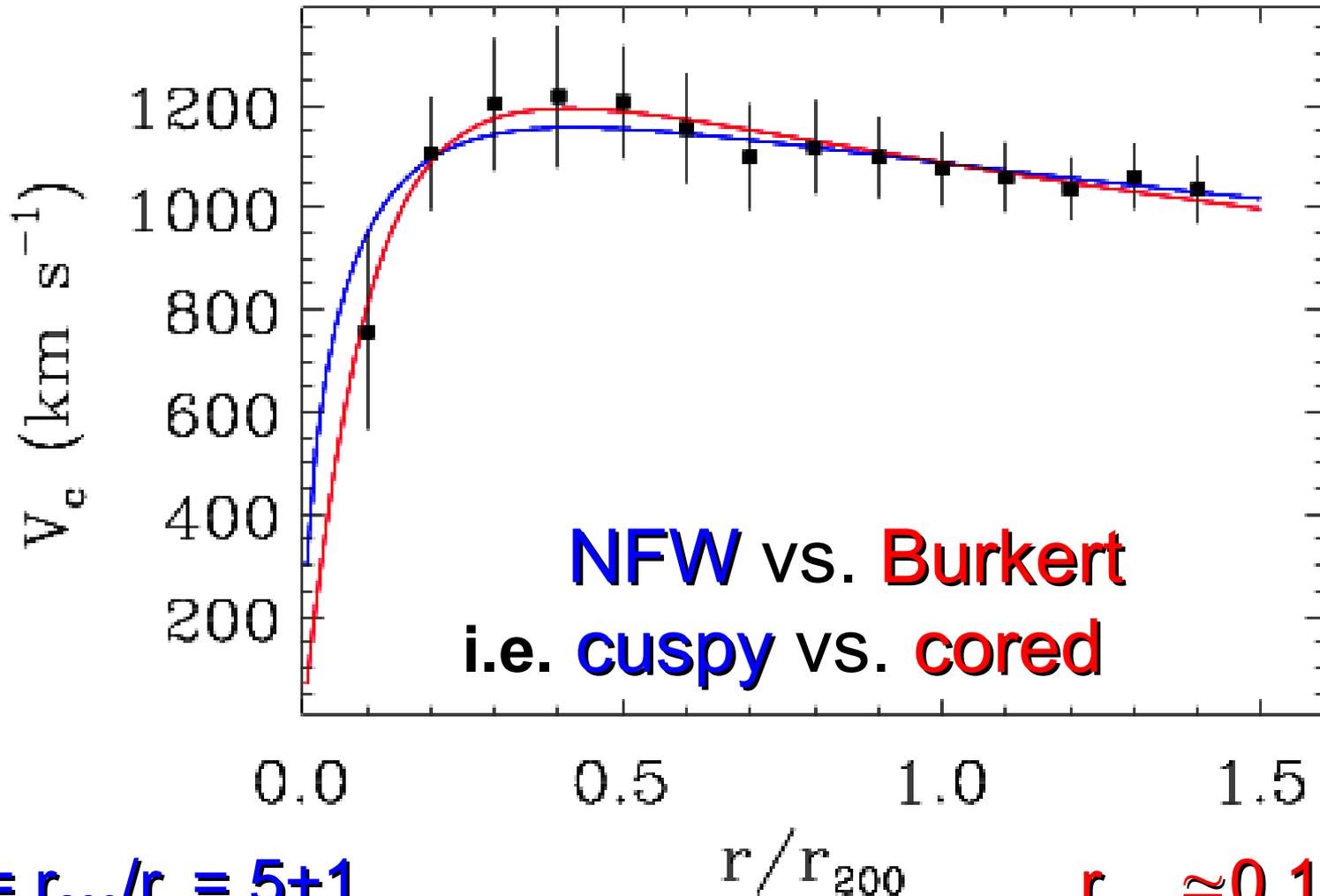
$$\rho_{NFW}(r) = \frac{\rho_0}{(r/r_s)(1 + r/r_s)^2}$$

...vs. the **cored model of Burkert (1995)**, motivated by the problems of NFW on galactic scales (e.g., de Blok et al. 2003, Gentile et al. 2004):

$$\rho_{Burkert}(r) = \frac{\rho_0}{(1 + r/r_0)[1 + (r/r_0)^2]}$$

# ENACS

$$V_c(r) \equiv \sqrt{\frac{G M(r)}{r}}$$

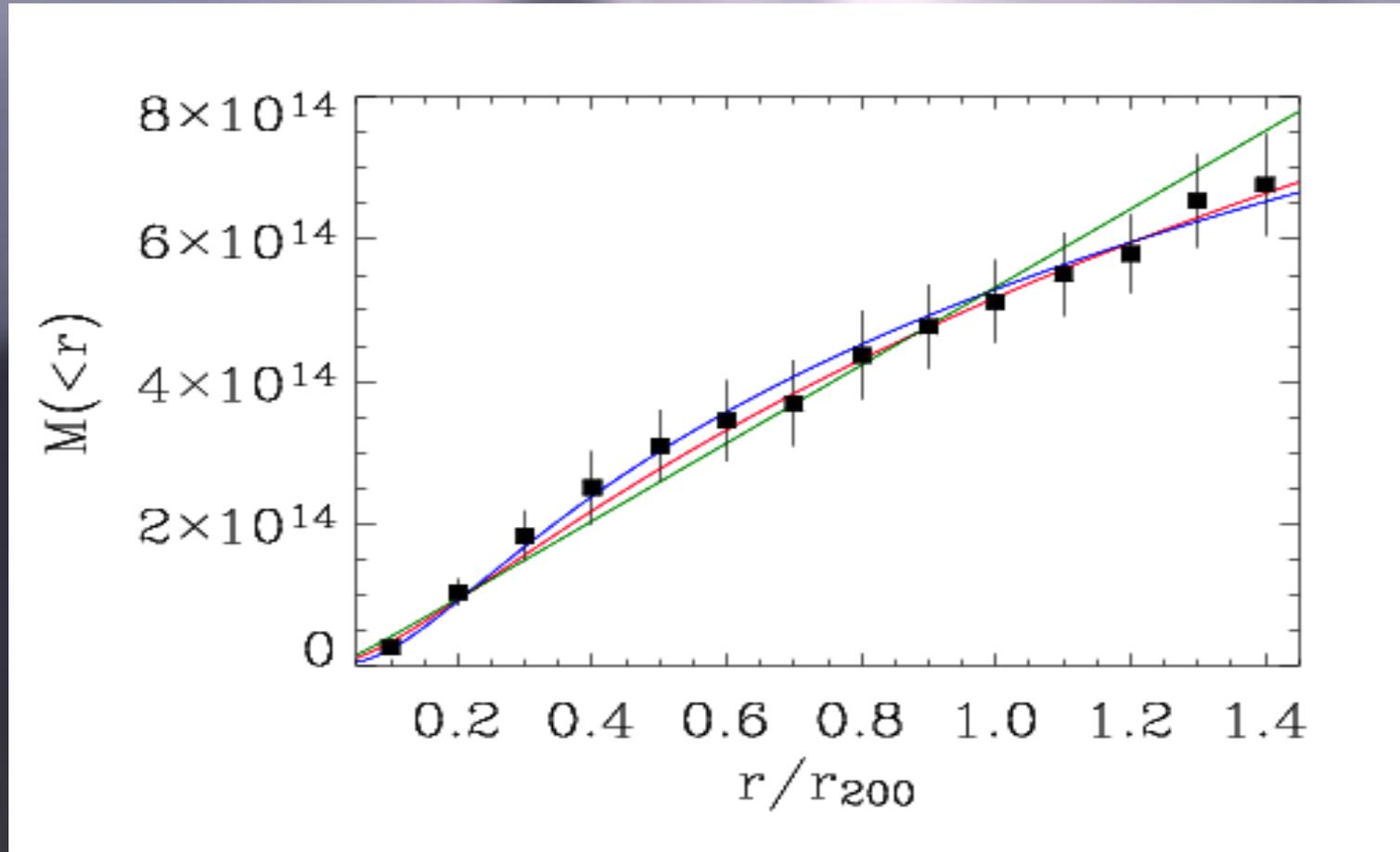


$$c = r_{200}/r_s = 5 \pm 1$$

$$r/r_{200}$$

$$r_{\text{core}} \approx 0.1 r_{200}$$

ENACS:  $\rho(r) \propto r^{-2.4 \pm 0.4}$  at  $r=r_{200}$



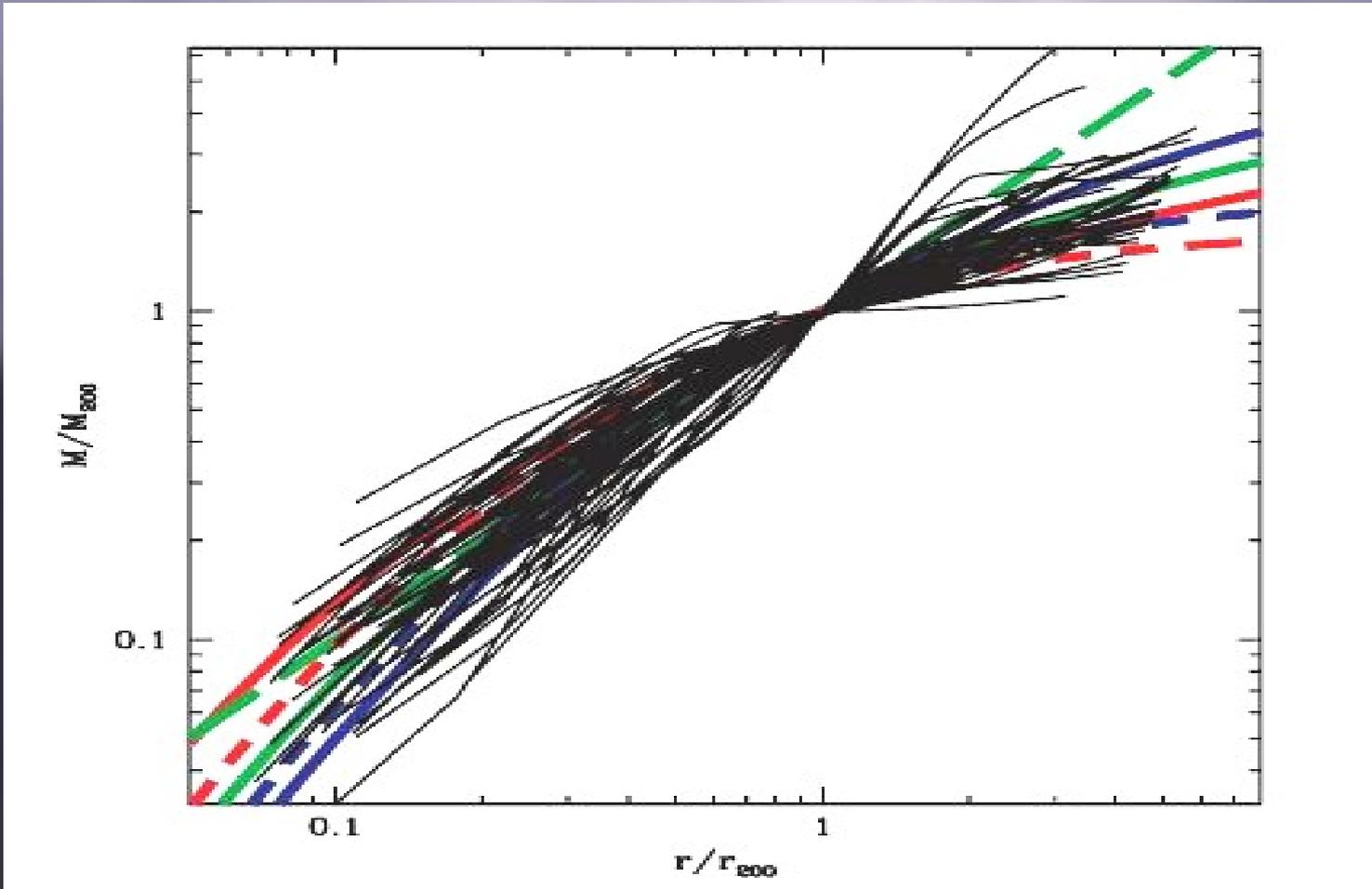
Fitting models: **NFW**

**Burkert 95**

**Isothermal** *gives poor fit*

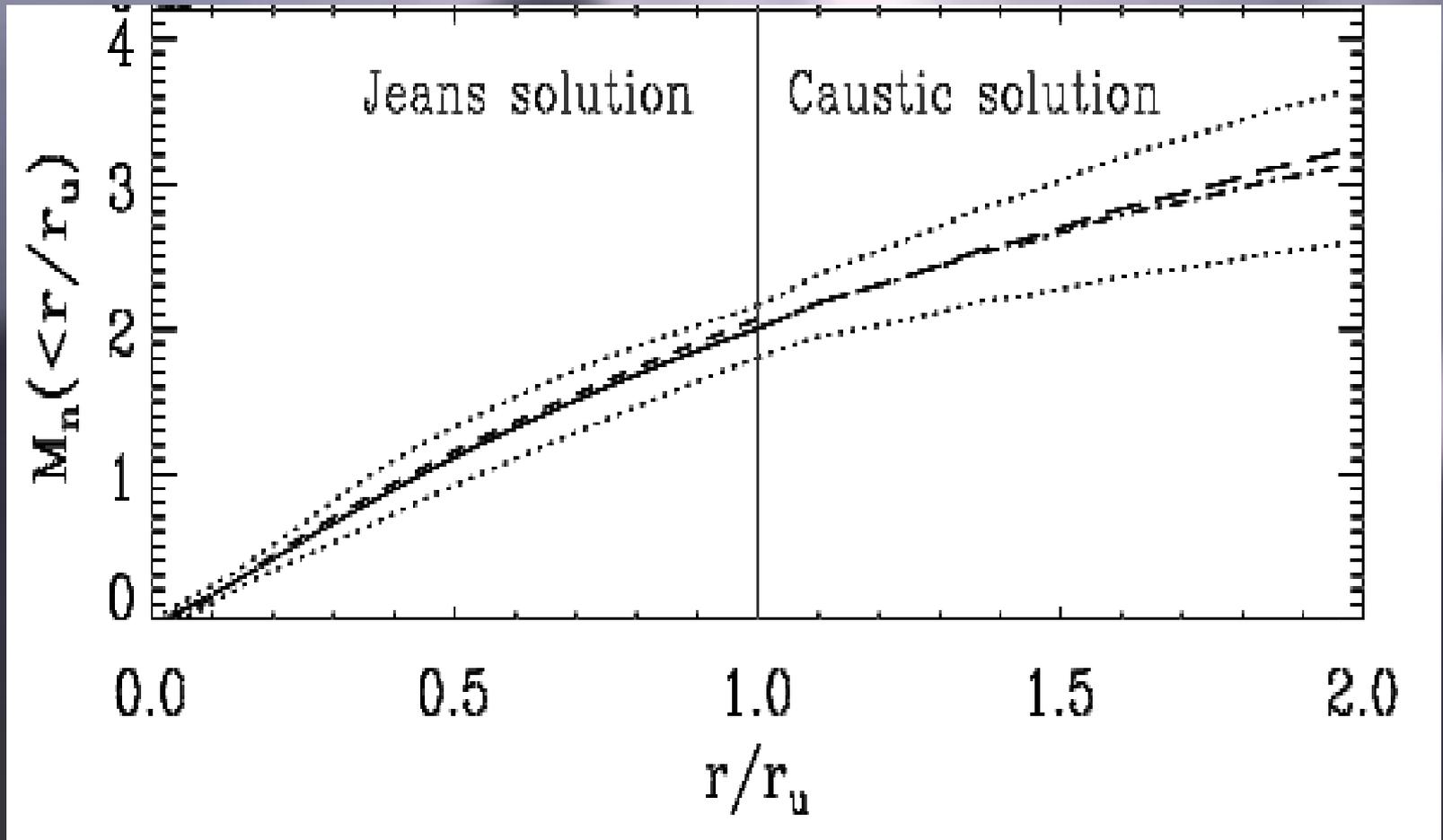
# CIRS: individual cluster mass profiles

From Rines & Diaferio (2006)



Fitting models: Solid lines: NFW  $c=3, 5, 10$   
Short dashed: Hernquist  
Long dashed: SIS

## 2dFGRS: combine the two methods:



The caustic  $M(r)$  nicely continues the  $M(r)$  found with the Jeans solution,  $\rho(r) \sim r^{-3}$  at large  $r$

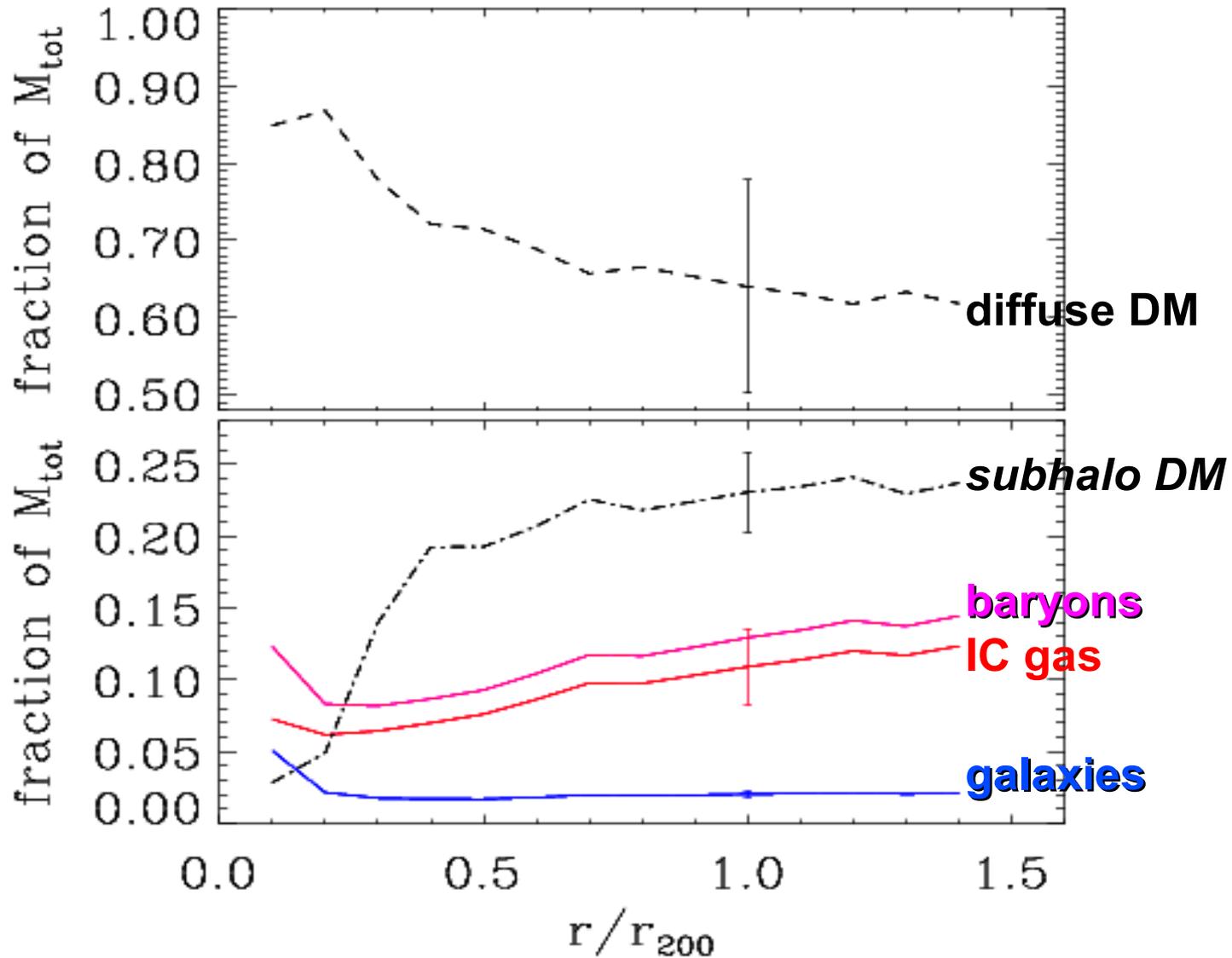
# MASS PROFILES

## the baryonic components

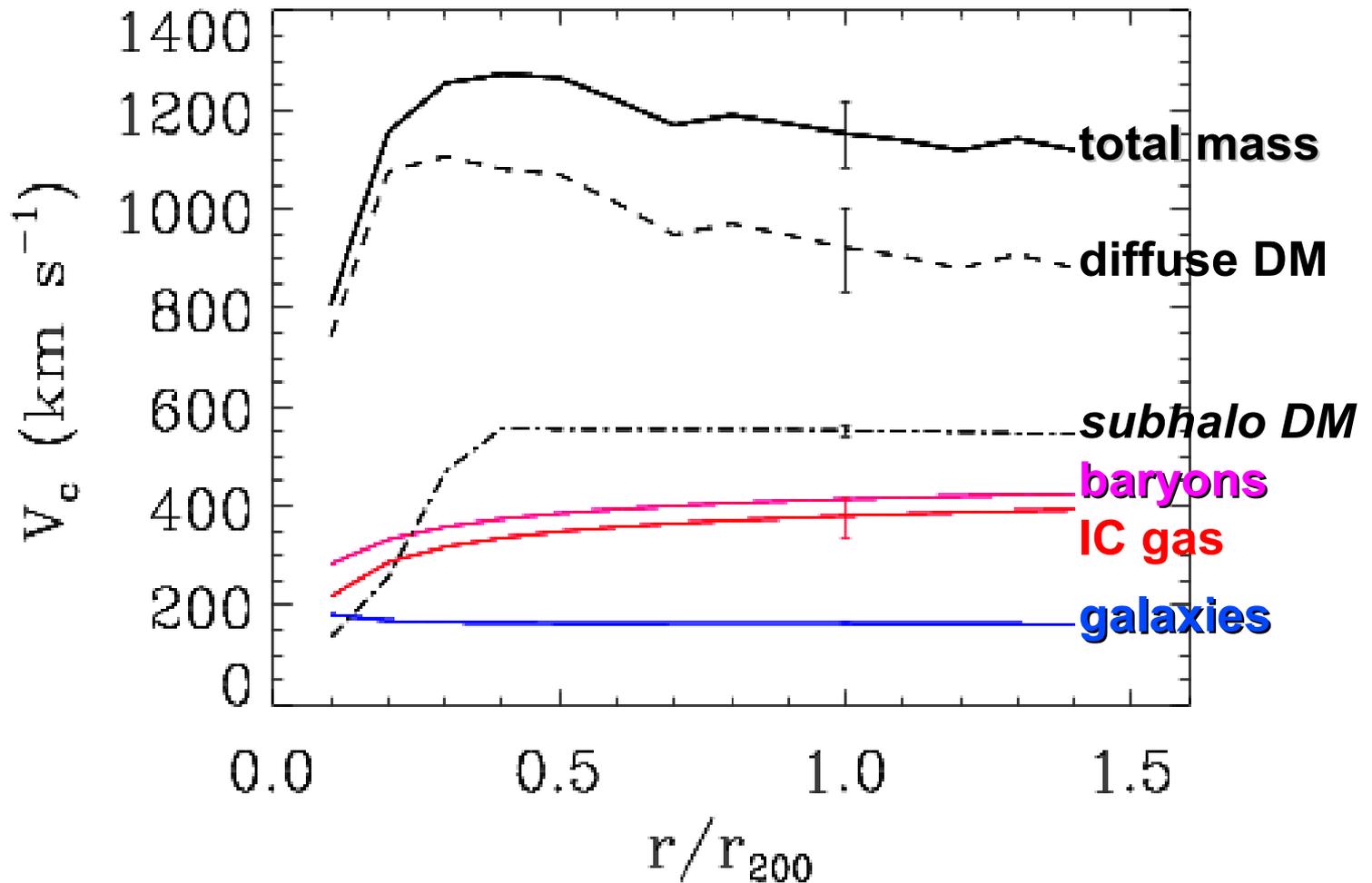


An example of YDS climbing class 4

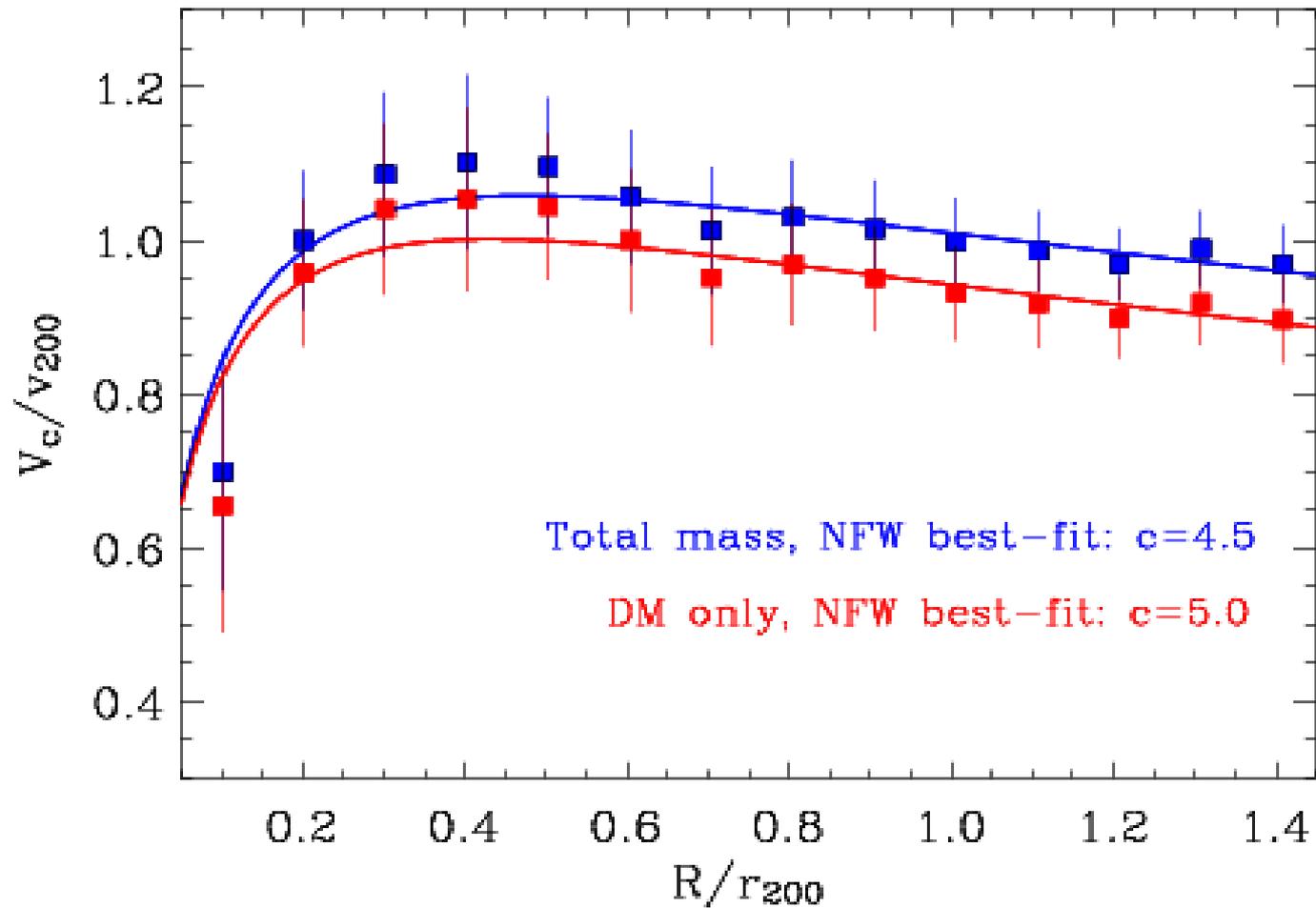
# ENACS: $M(<r)$ subdivided into its components



$c$  for DM only  $>$   $c$  for total  $M(r)$  (*but only slightly*)

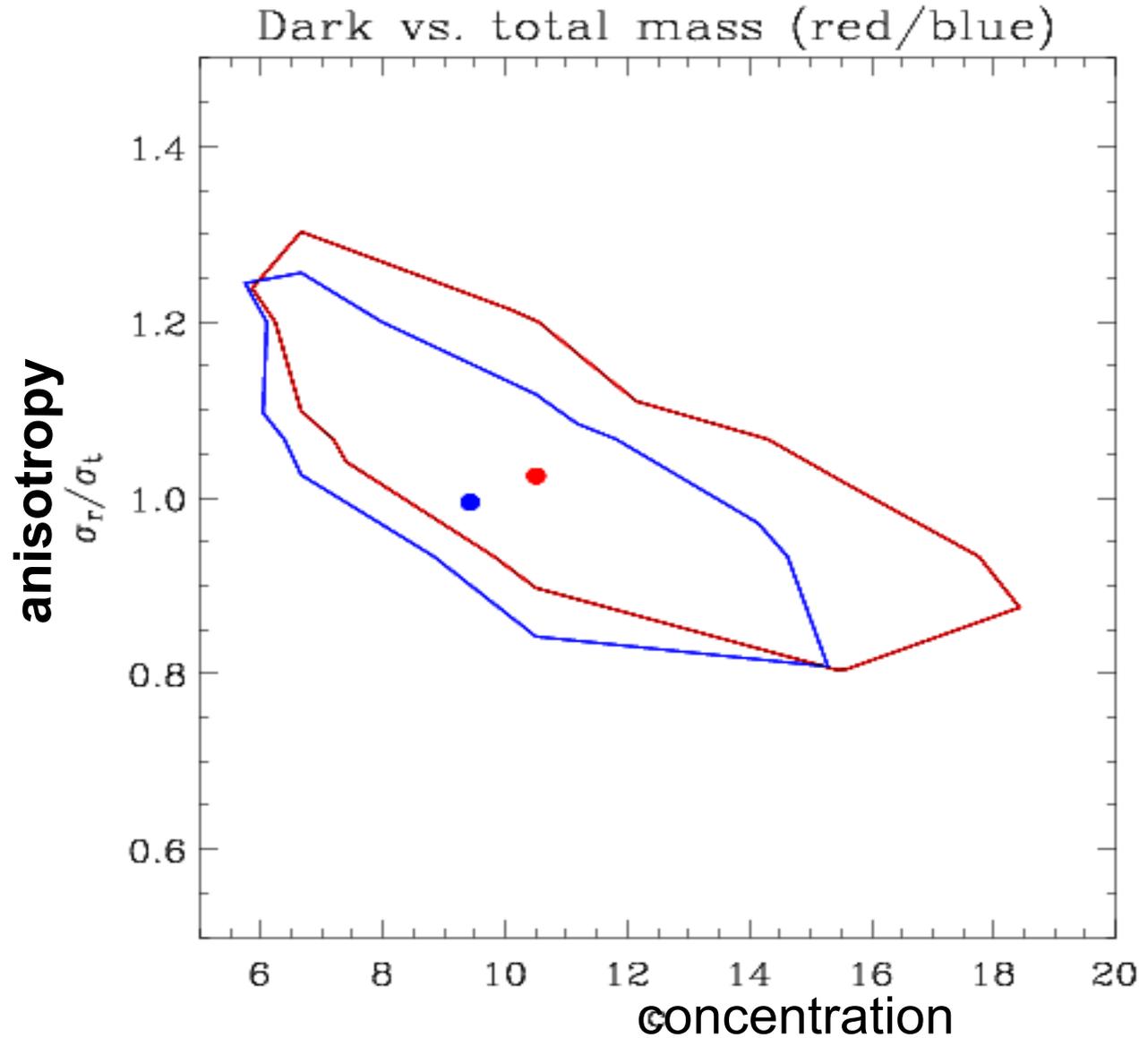


$c$  for DM only  $>$   $c$  for total  $M(r)$  (*but only slightly*)



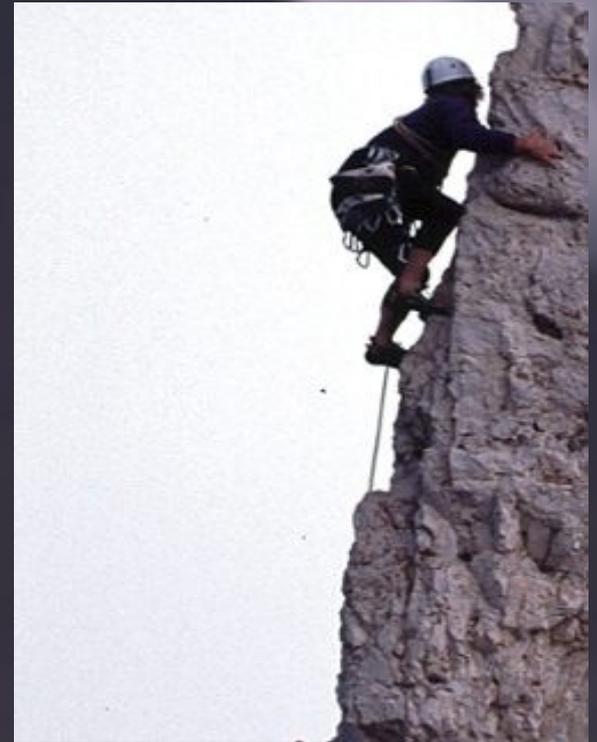
$c$  for DM only  $>$   $c$  for total  $M(r)$  (*but only slightly*)

GEMS



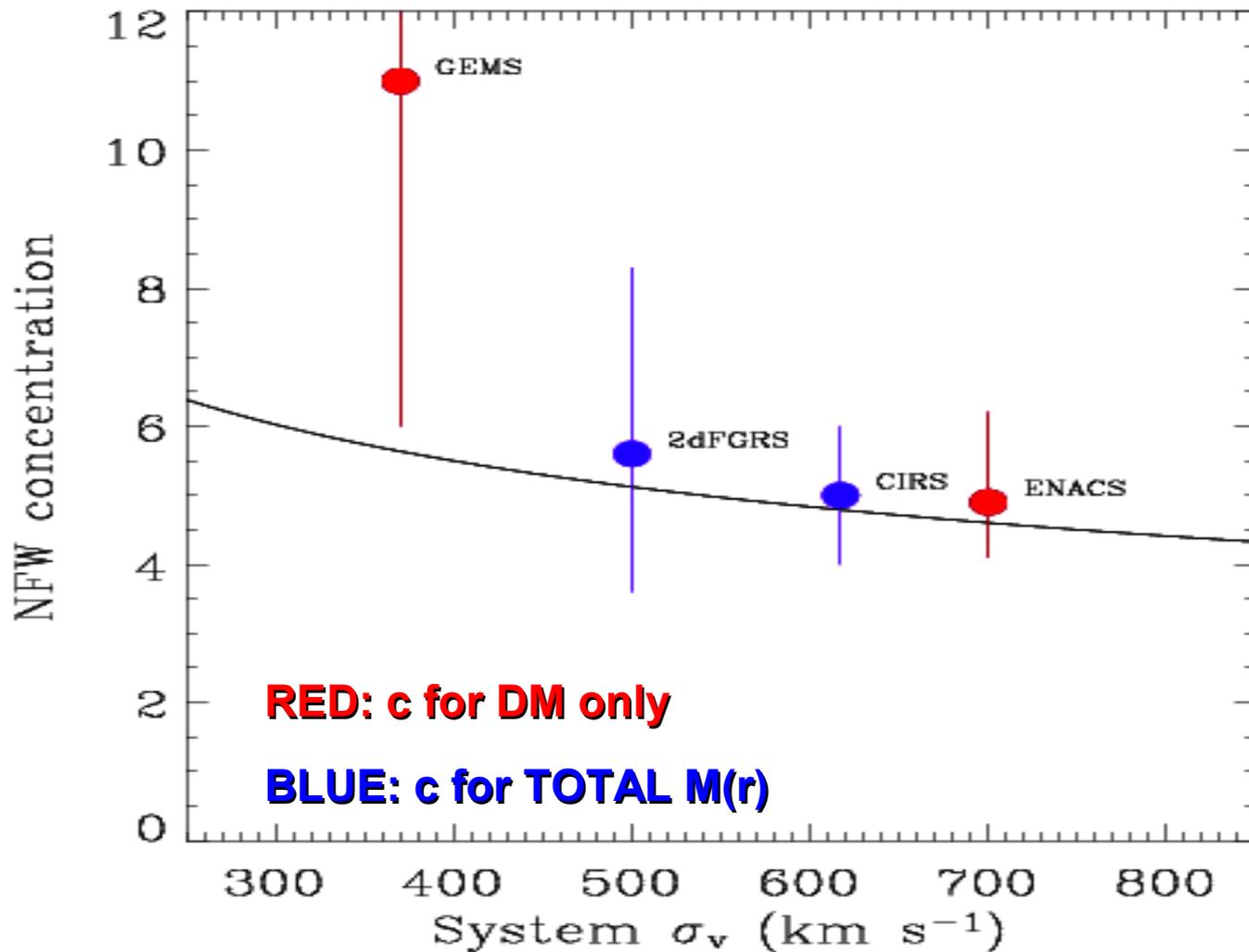
# MASS PROFILES

$$c=c(M)$$



An example of YDS climbing class 5

# NFW $c=c(M)$ : observations vs. theoretical predictions ( $\Lambda$ CDM; Dolag et al. 2004)



# GALAXY ORBITS

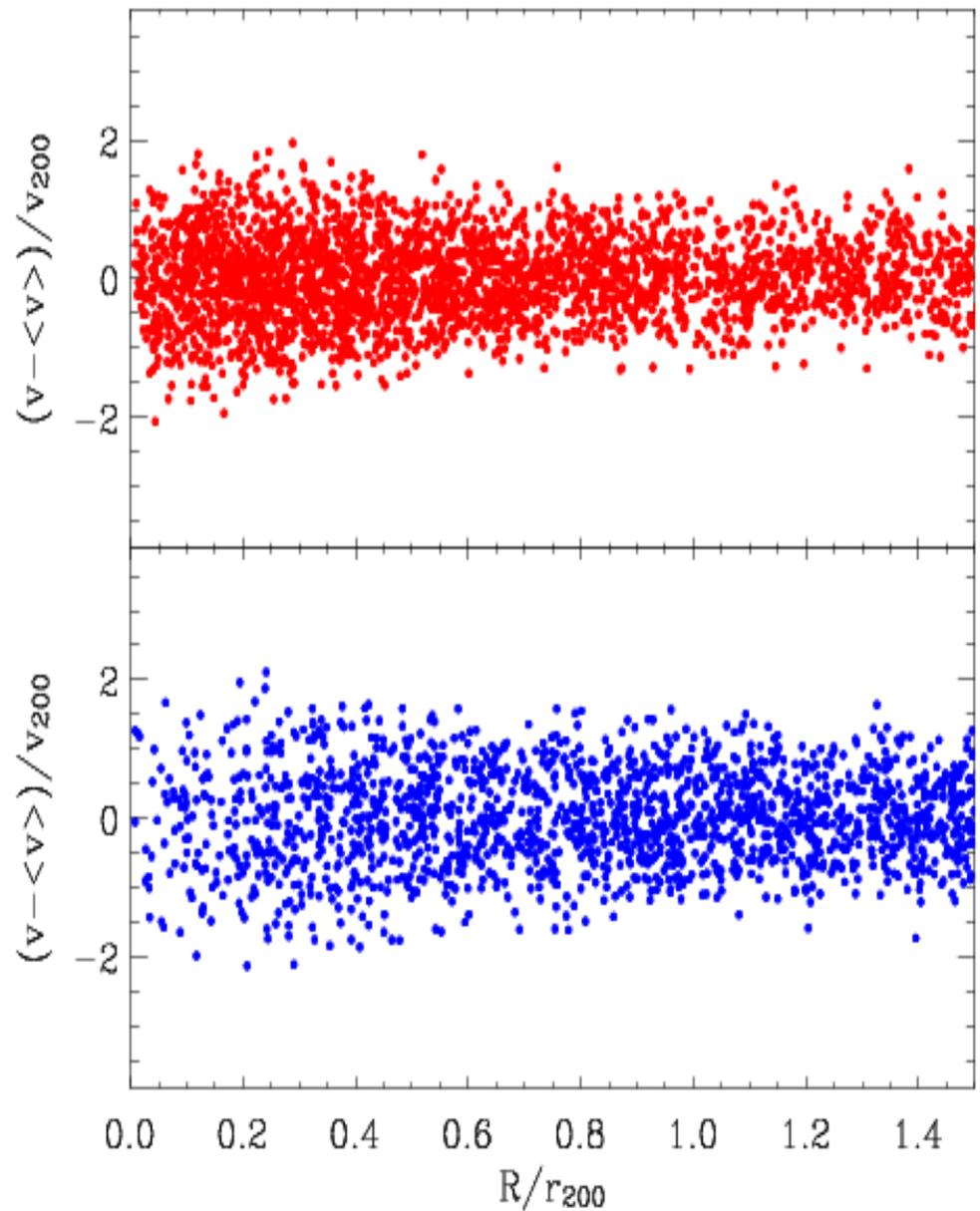
i.e. velocity anisotropy profiles

$$\beta'(r) \equiv \sigma_r(r)/\sigma_t(r)$$



An example of YDS climbing class 5.3

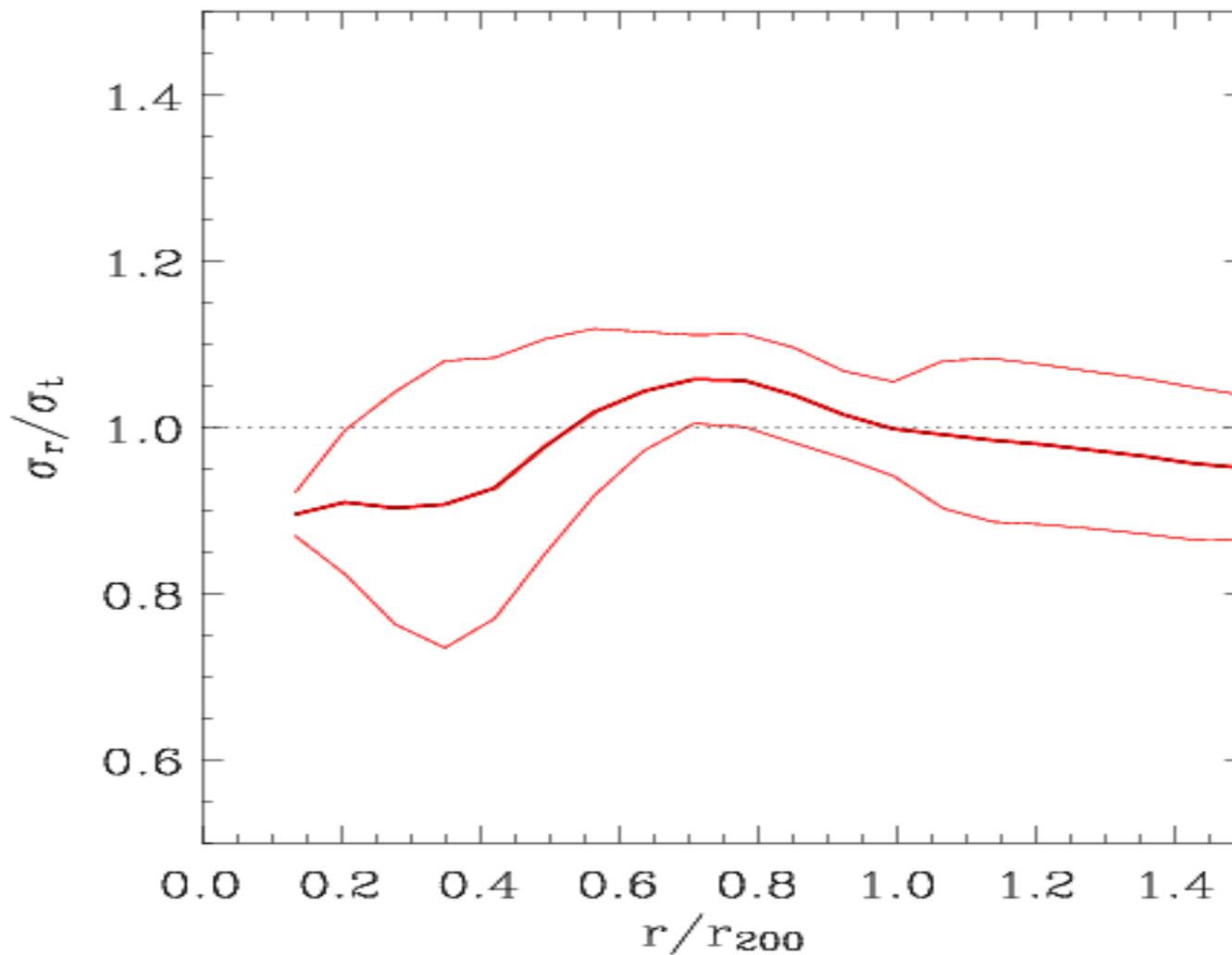
*Must distinguish  
red (early-type)  
from blue (late-type)  
galaxies  
because they have  
different  
 $R_n, V_n$  distributions  
(hence different  
orbits may be  
expected given the  
same mass profile)*



**CIRS**

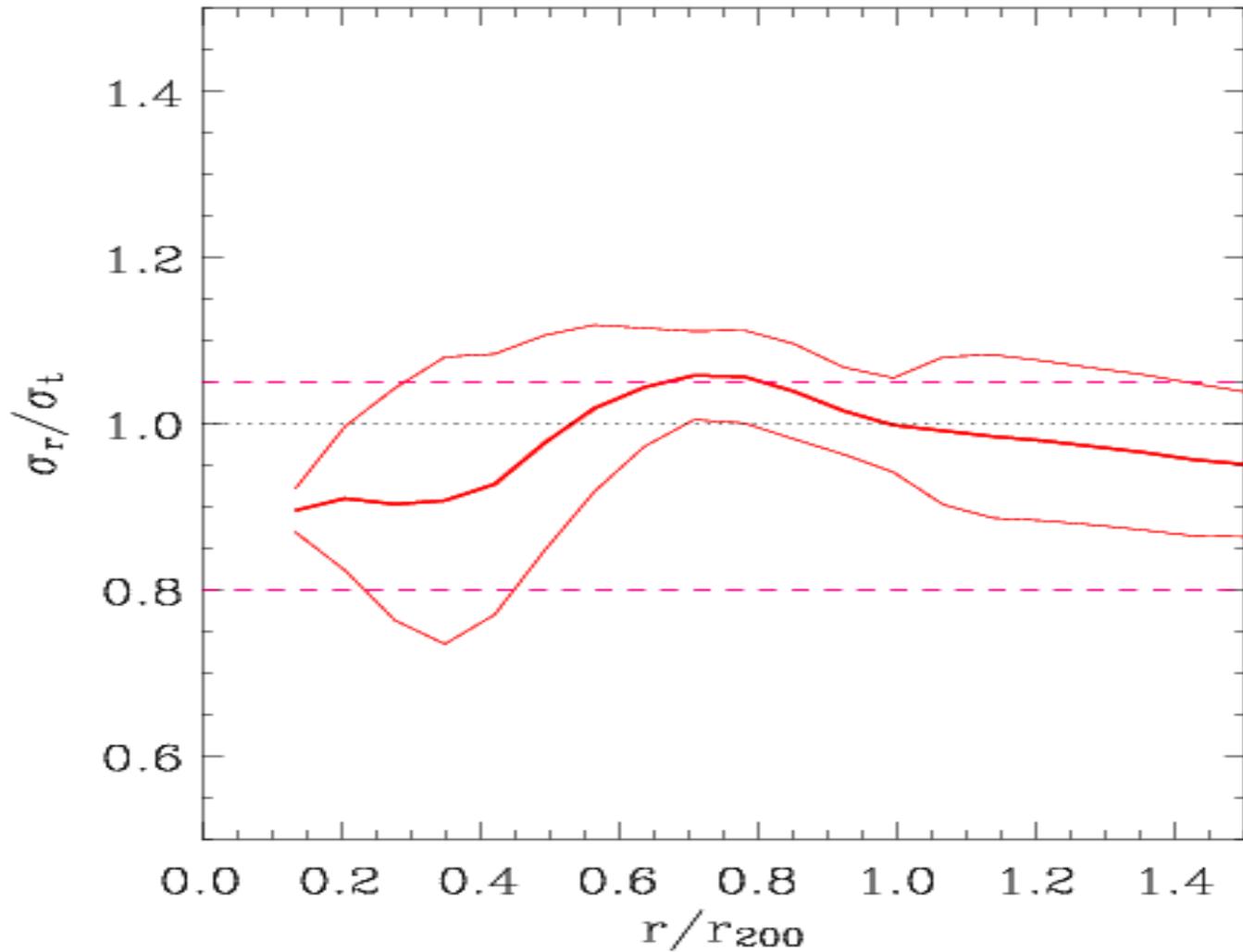
# Red galaxies move on $\approx$ isotropic orbits

CIRS, caustic  $M(r)$  from  
Rines & Diaferio (2006)



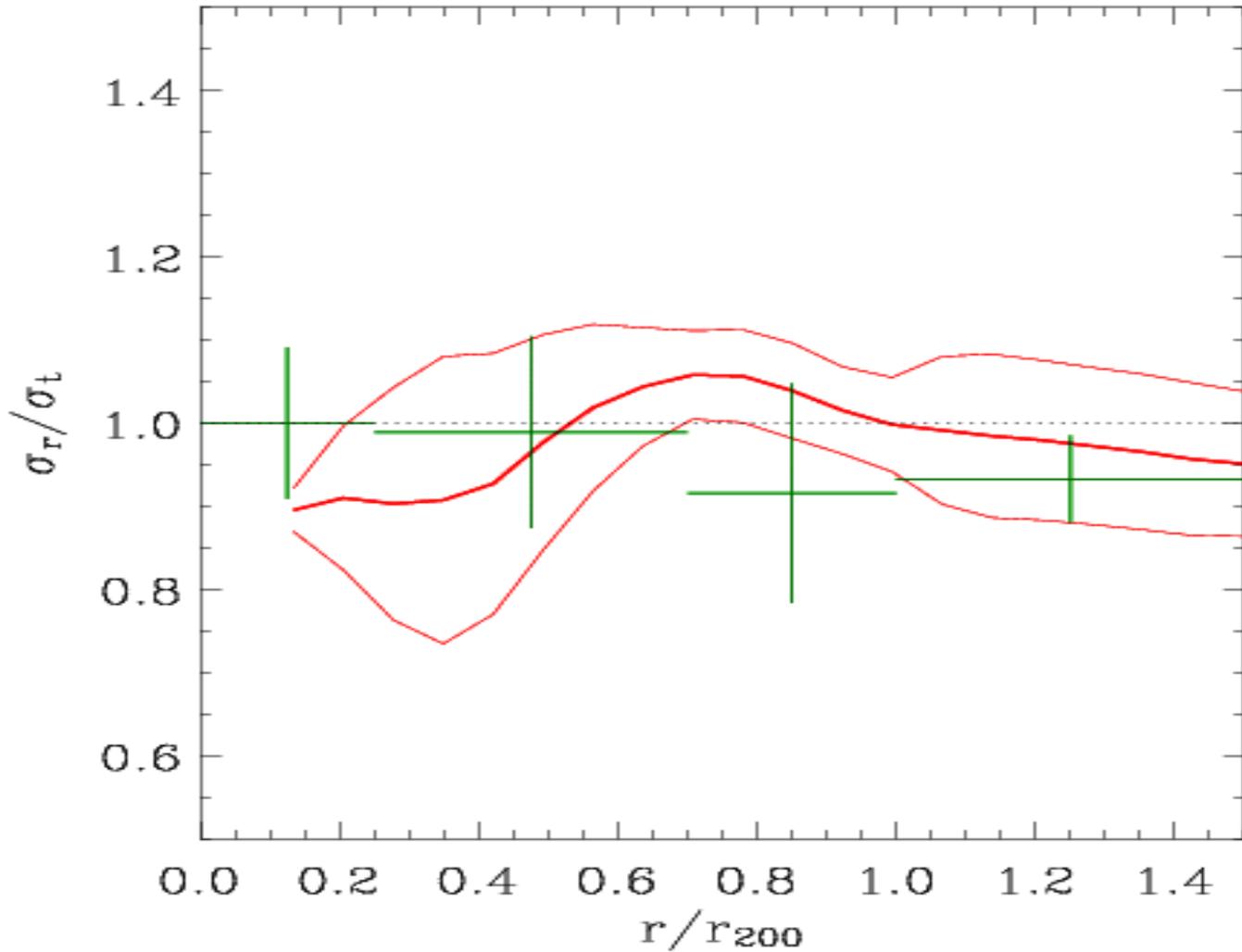
# Isotropic orbits for red gal.s: ≠ samples

CIRS vs. ENACS



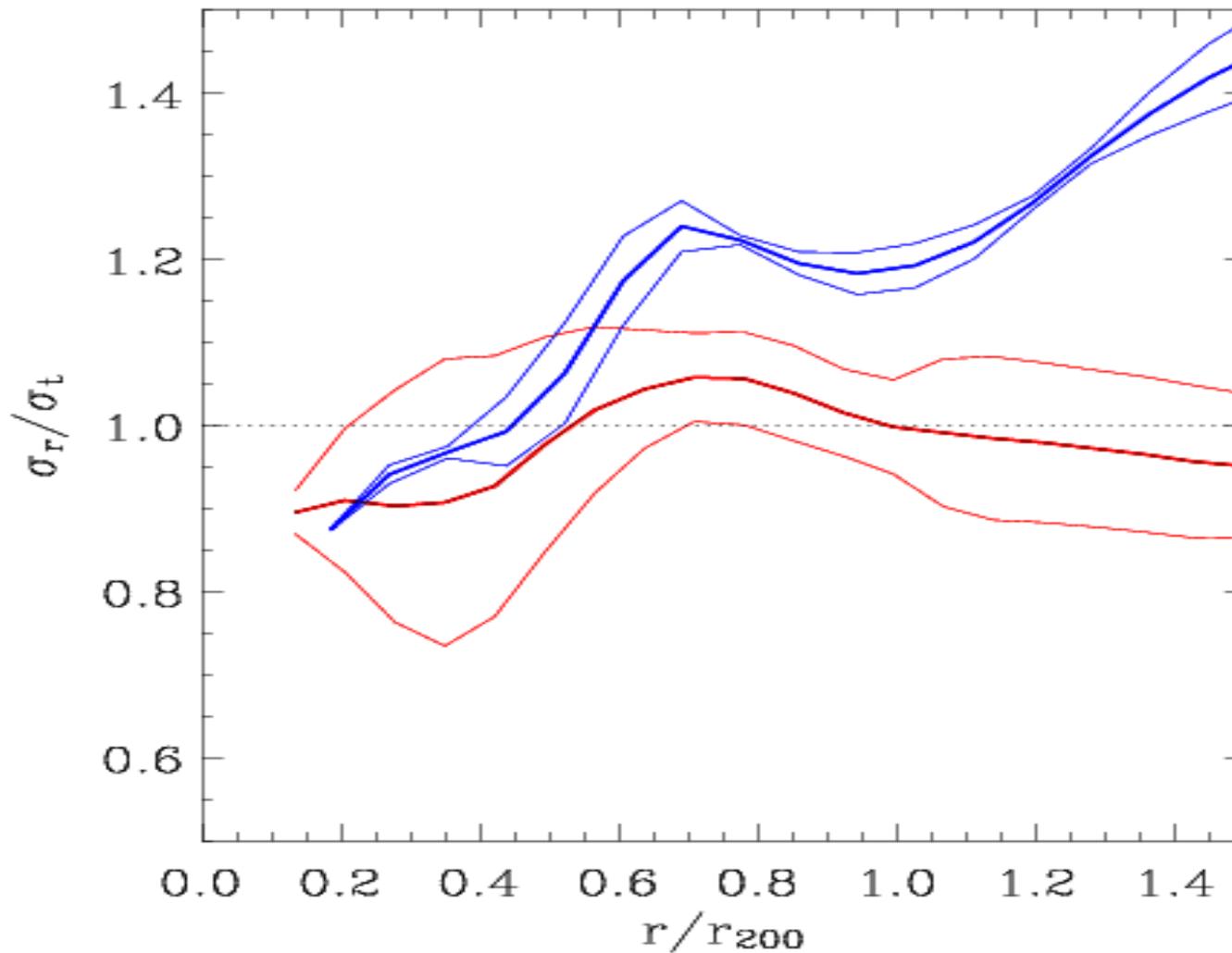
# Isotropic orbits for red gal.s: ≠ methods

CIRS: Jeans vs. Gauss-Hermite



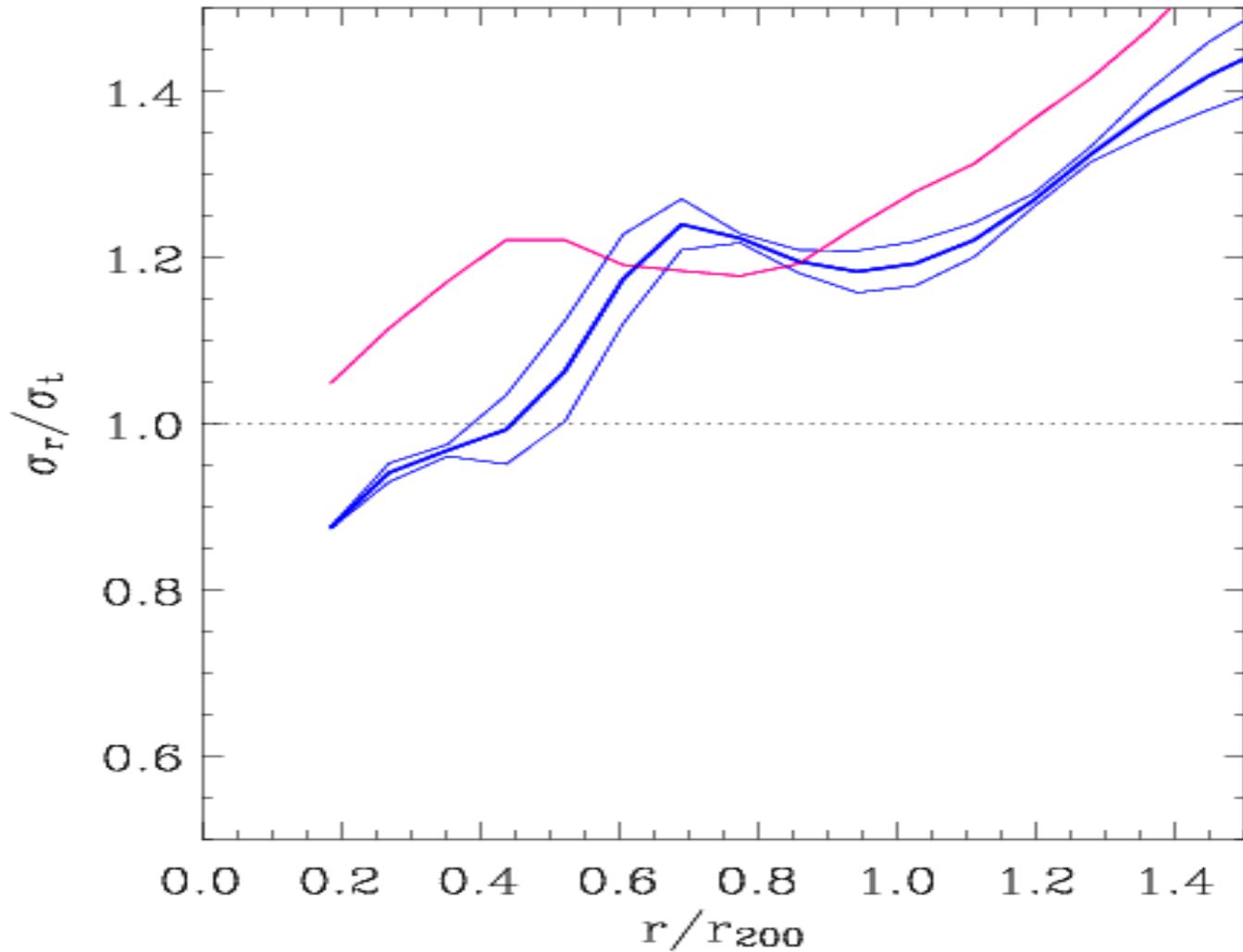
# Blue galaxies move on more radial orbits

CIRS: red vs. blue galaxies



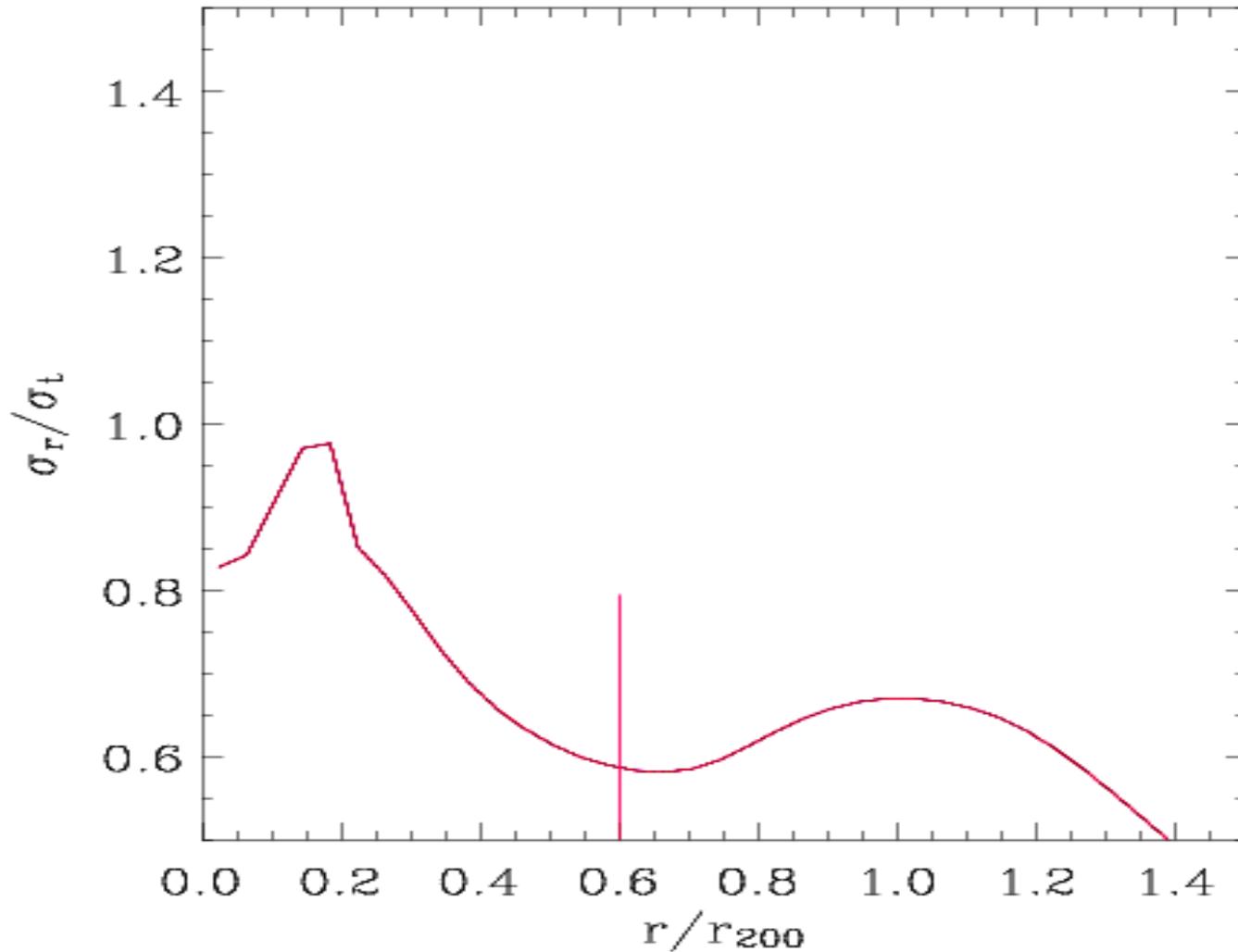
# Radial orbits for blue gal.s: ≠ samples

CIRS vs. ENACS



# Substructures (groups in clusters): *tangential anisotropy*

ENACS

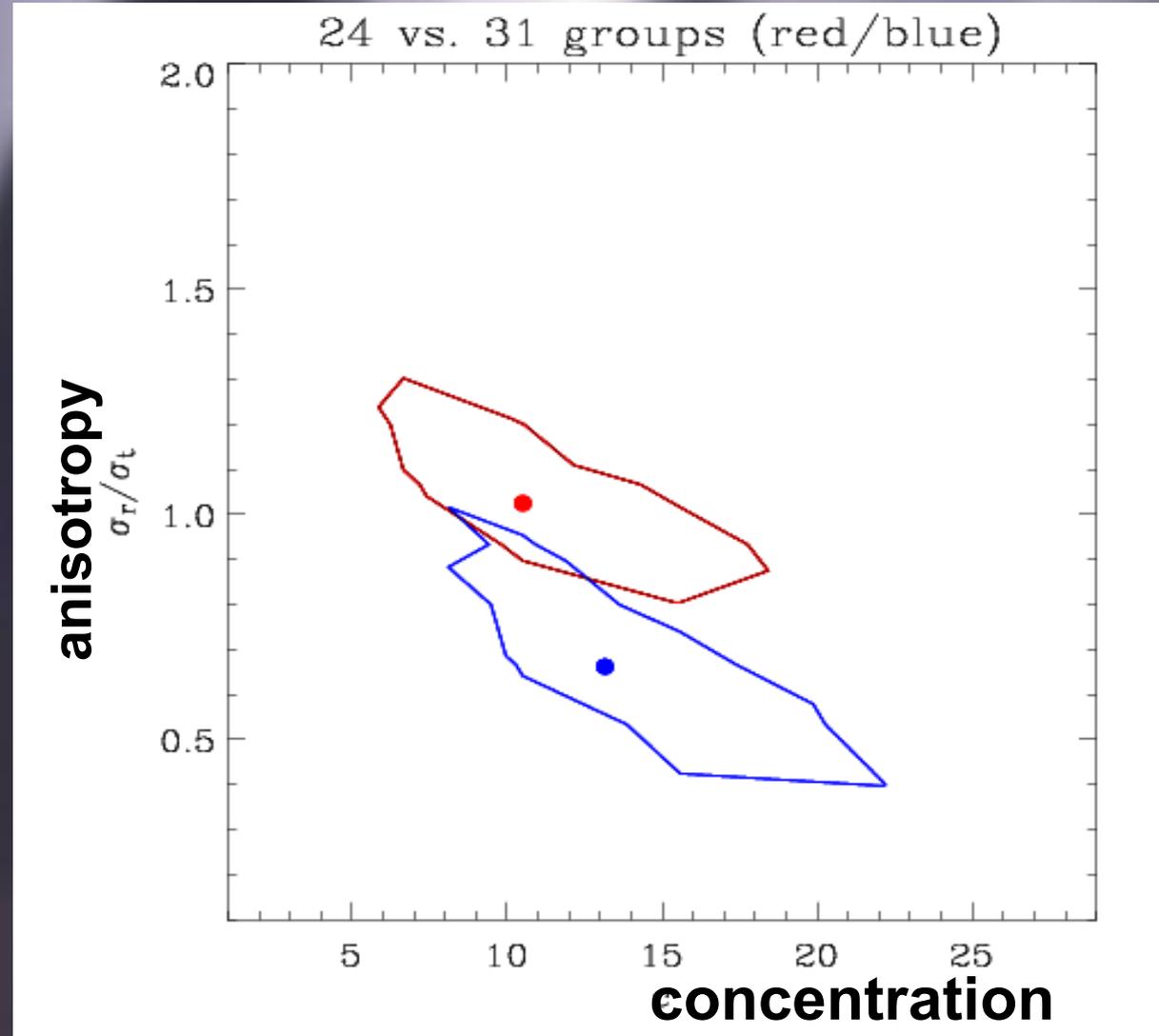


# Gal.s in small $\sigma_v$ groups: energy dissipation?

## GEMS:

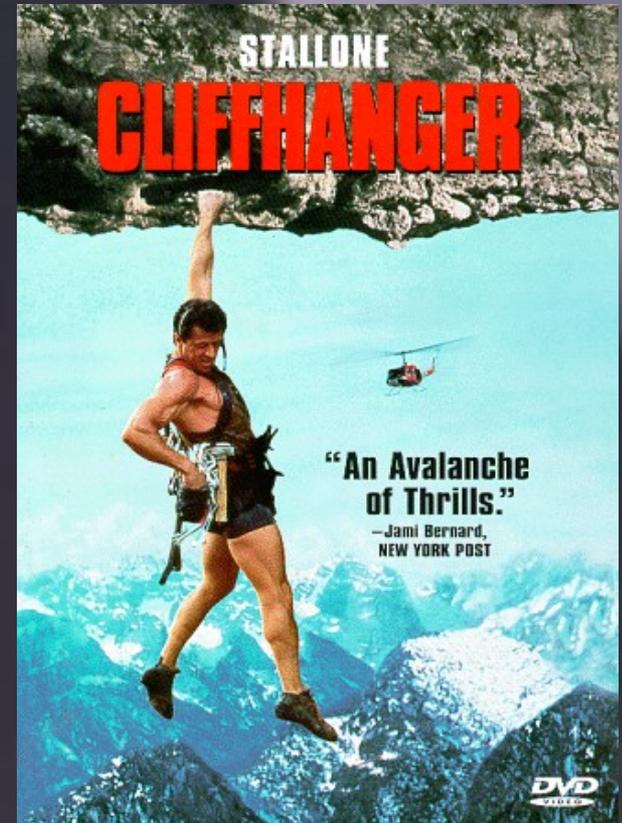
7 out of 31 groups have very small  $\sigma_v$  given their  $T_x$ :

*their galaxies move on slightly tangential orbits*



# SHOULD WE TRUST THESE RESULTS?

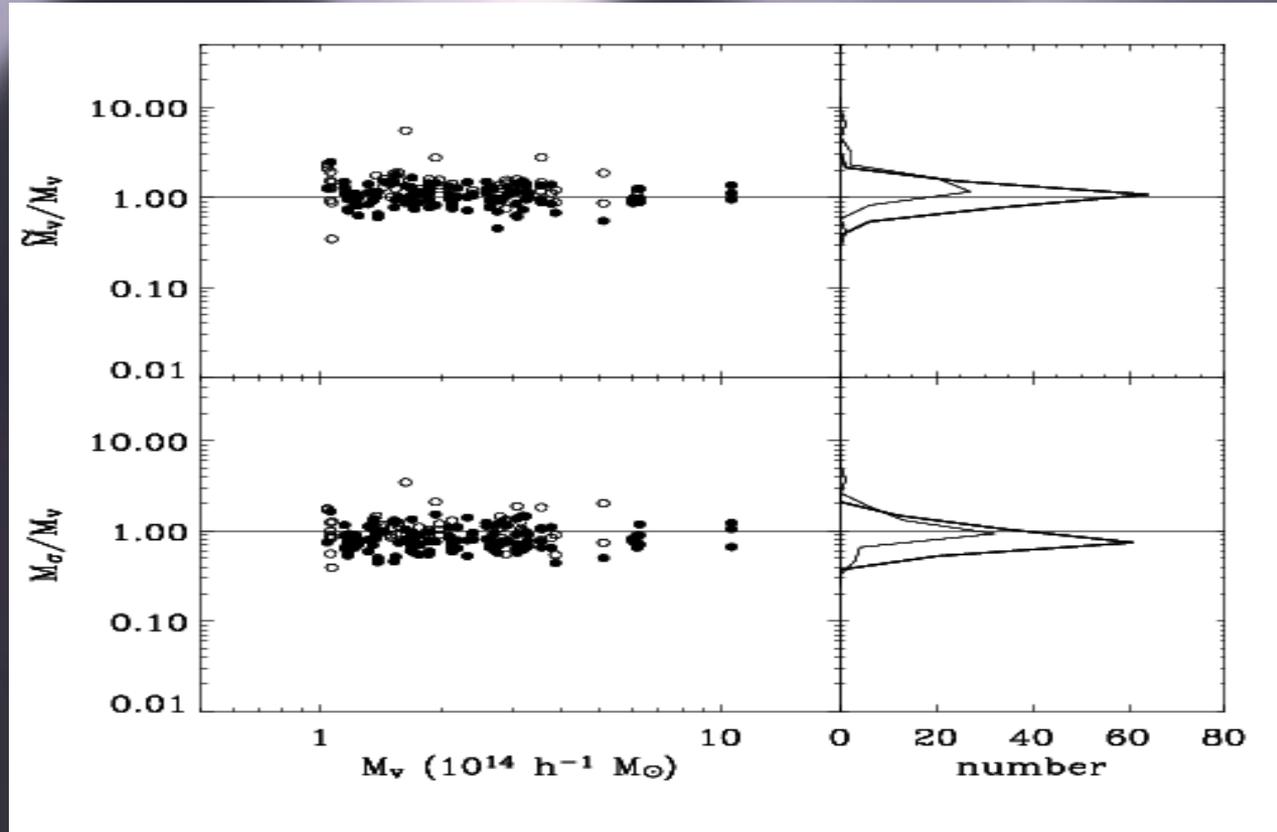
cmp with numerical  
simulations:  
masses and  
mass profiles



An example of YDS climbing class 5.6

⇒ compare to clusters extracted from cosmological simulations (from Borgani et al. 04) and projected

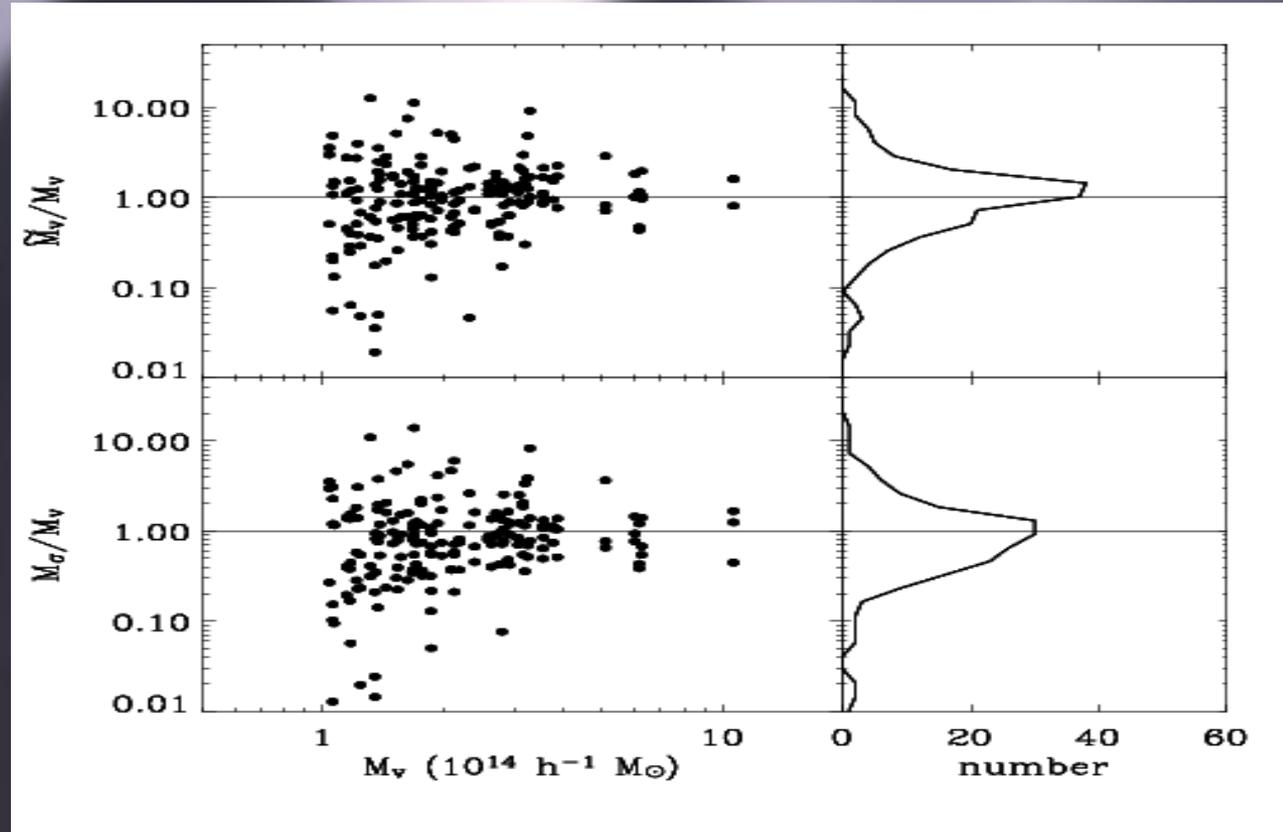
Virial mass estimates  
≈ unbiased  
for  $N_{part} \geq 60$



⇒ compare to clusters extracted from cosmological simulations and projected

Virial mass estimates  
≈ unbiased  
for  $N_{part} \geq 60$

For smaller  $N_{gal}$   
select 'old' (red)  
galaxies

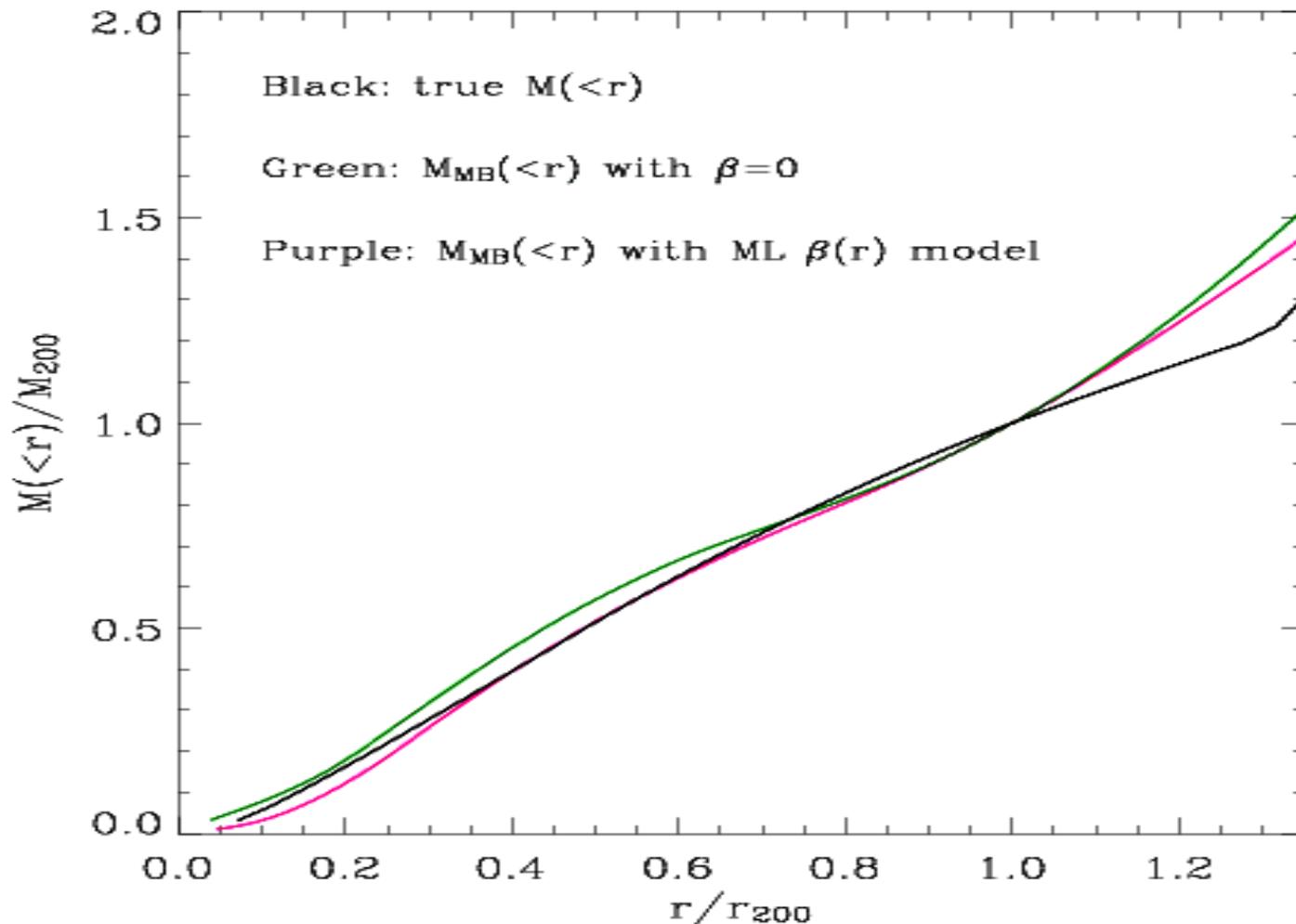


⇒ Global dynamical estimates for clusters are OK:

$M_{200}$  can be used for scaling vel.s and radii

(unless  $N_{gal}$  very small: groups; use  $T_x$ )

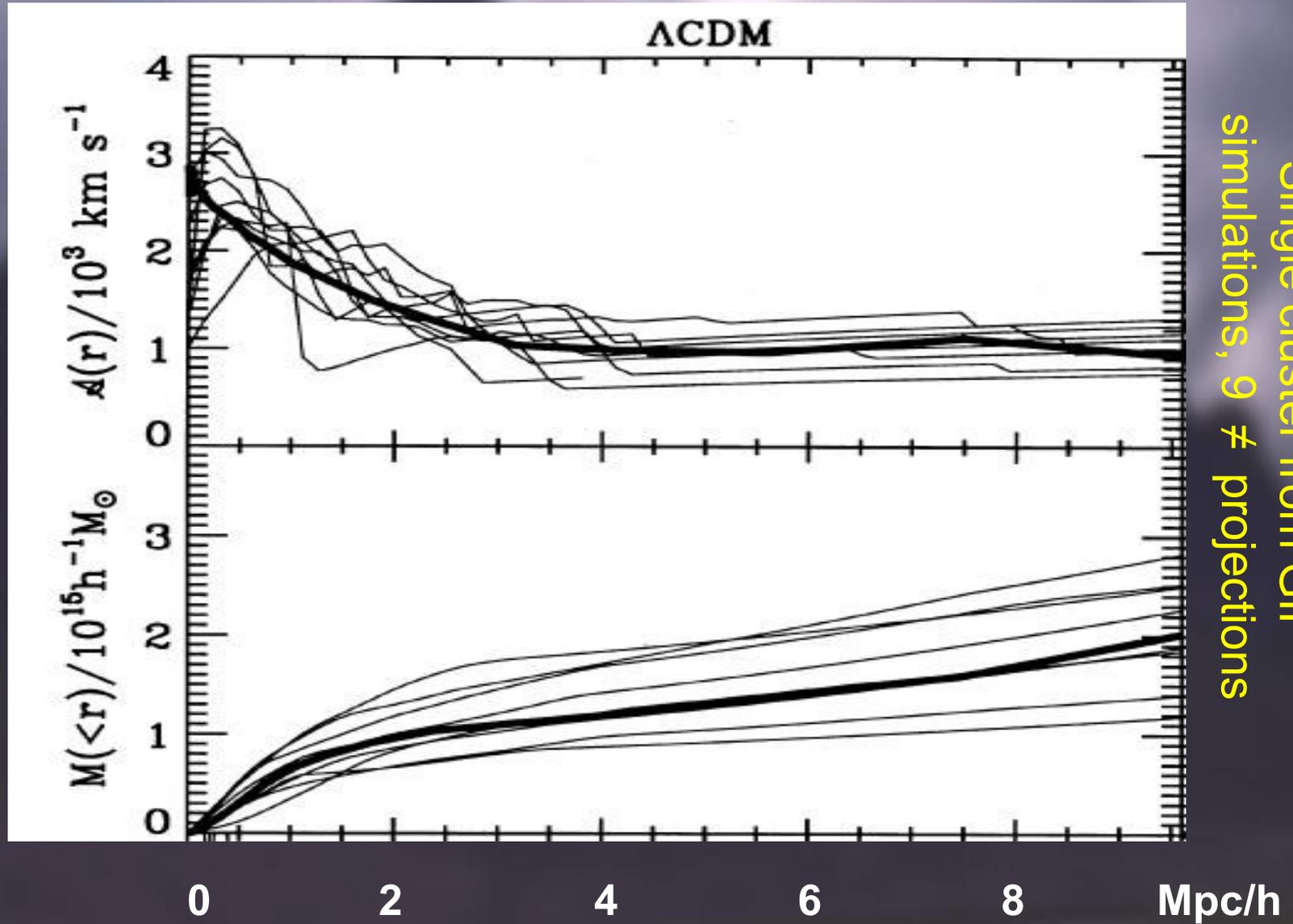
Apply the Jeans method to projected data:  $M(r)$   
( $\beta(r)$  from projected velocity distribution moments)



Stacked cluster from Borgani's  
simulations,  $\approx 4000$  obj's

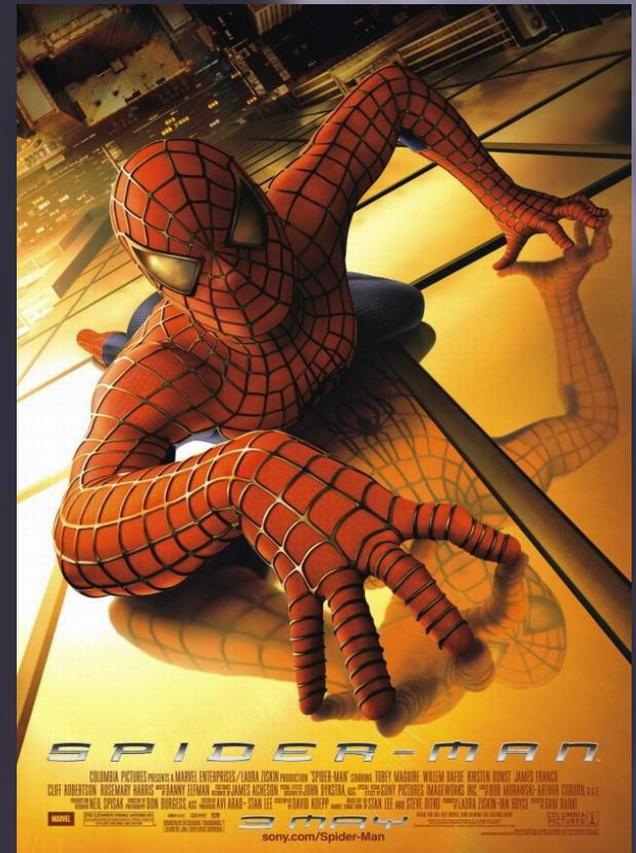
# Determine $M(r)$ with the caustic method:

From Diaferio (1999)



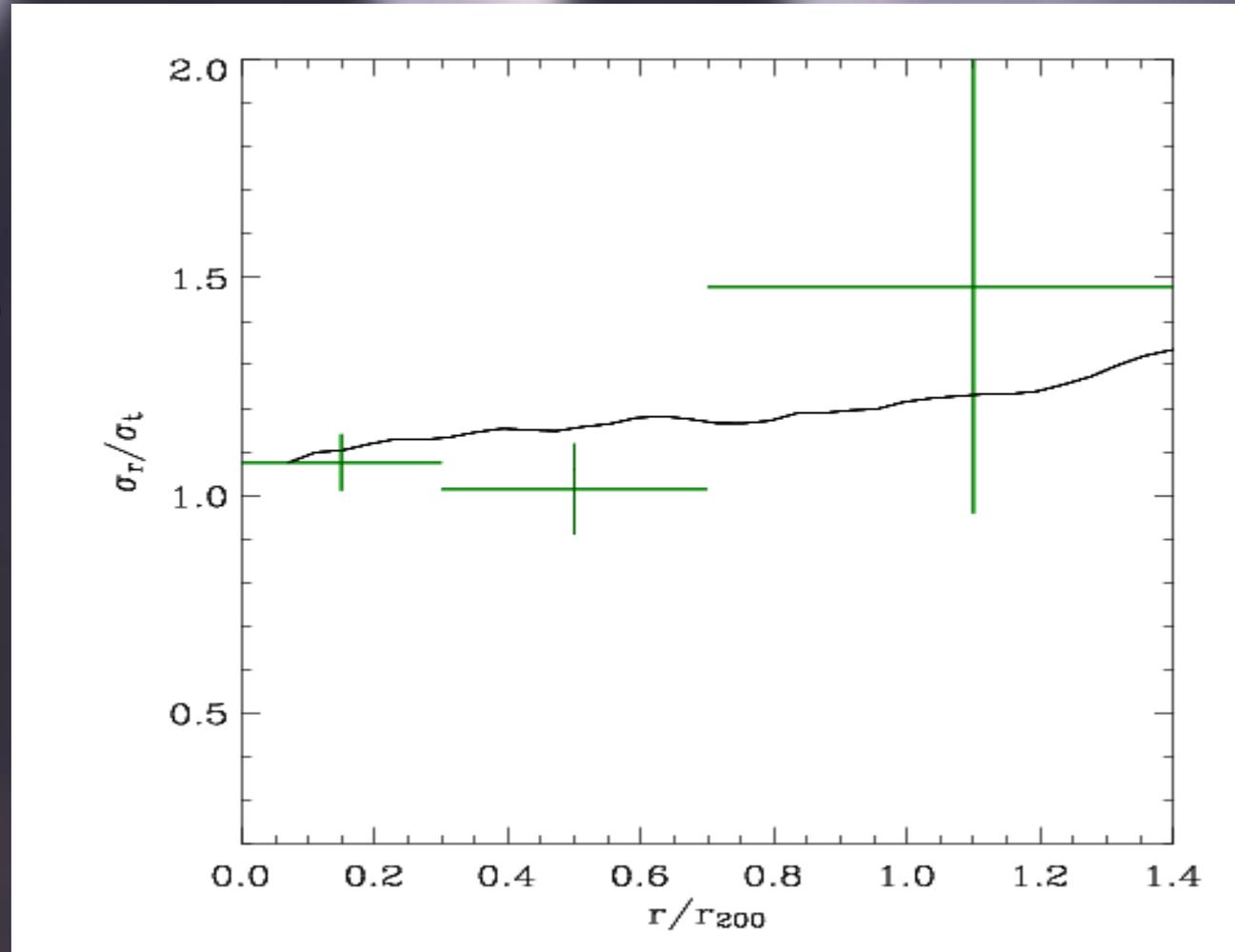
# SHOULD WE TRUST THESE RESULTS?

cmp with numerical  
simulations:  
velocity anisotropy  
profiles (orbits)



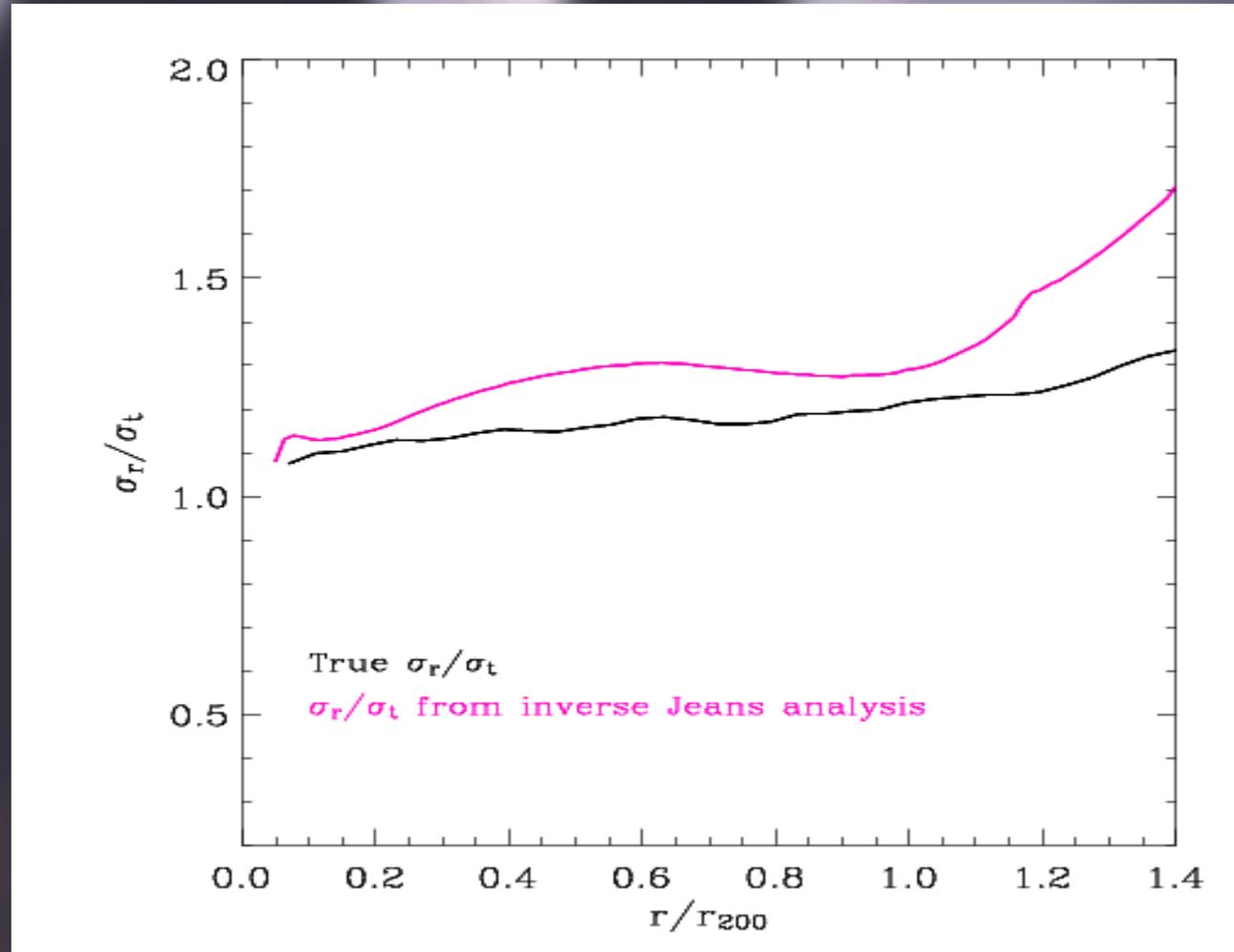
An example of YDS climbing class 5.9

Stacked cluster from Borgani et al.'s simulations: true velocity anisotropy profile compared to profile obtained from the analysis of the velocity moments of projected data (*Gauss-Hermite*)



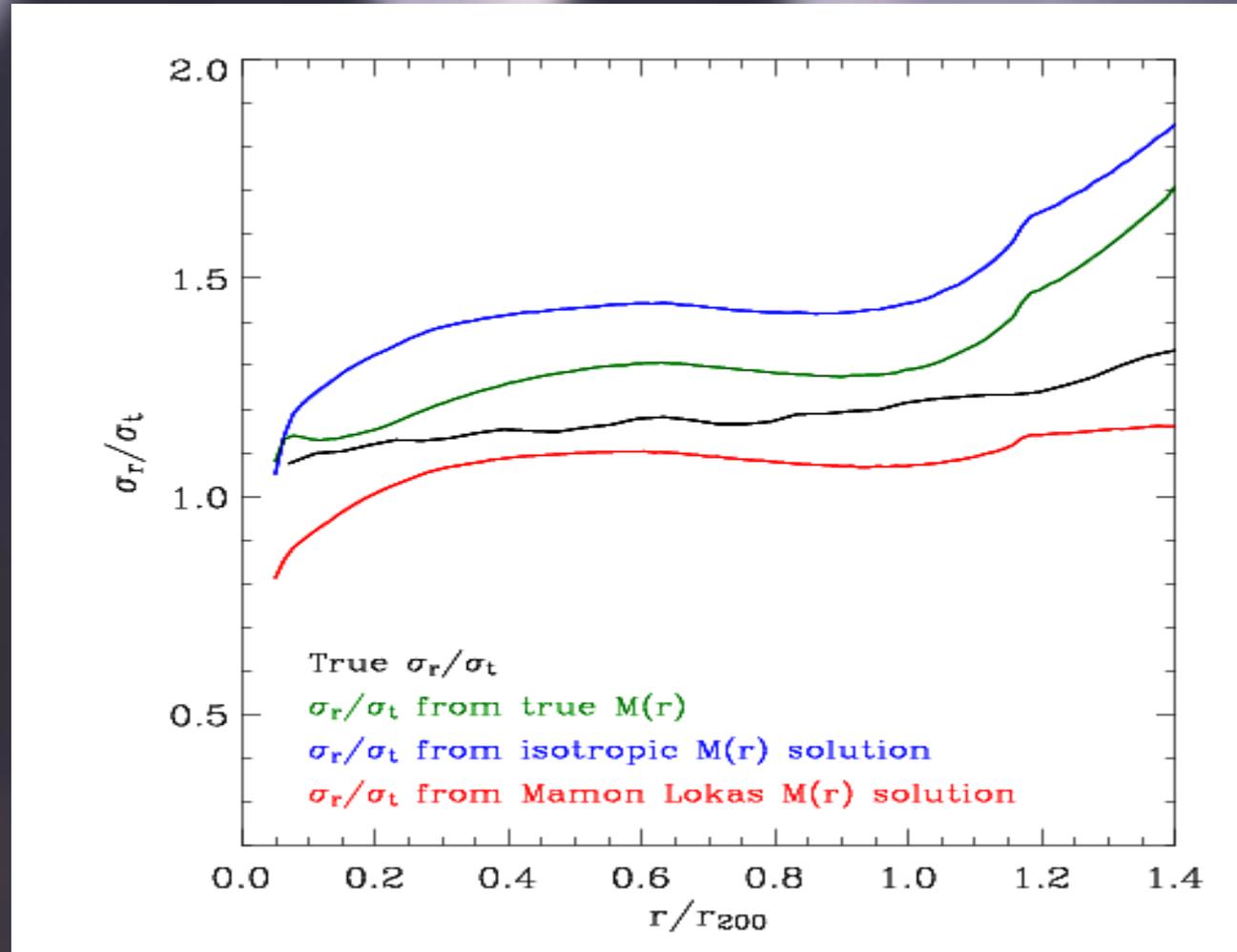
Stacked cluster from Borgani et al.'s simulations: true velocity anisotropy profile compared to profile obtained from Jeans analysis of projected data, given  $M(r)$

*Overestimate probably due to unidentified interlopers in  $(R, v)$  space*



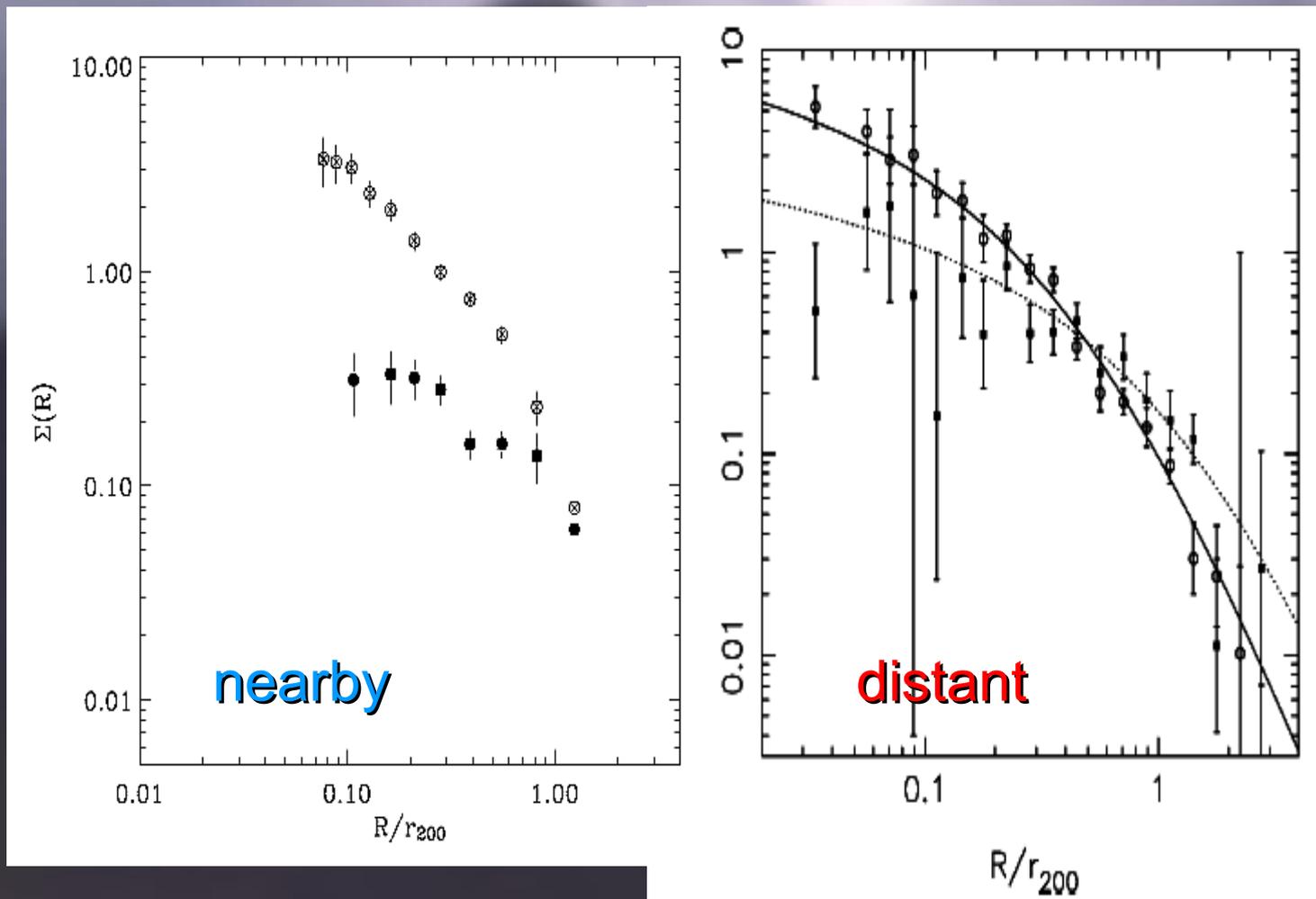
True velocity anisotropy profile *compd to profiles obtained from Jeans analysis, using true M(r), isotropic M(r) Jeans solution, and anisotropic M(r) Jeans solution (as obtained from Gauss-Hermite analysis)*

→ Accurate  $\beta'(r)$  determination requires accurate  $M(r)$  determination



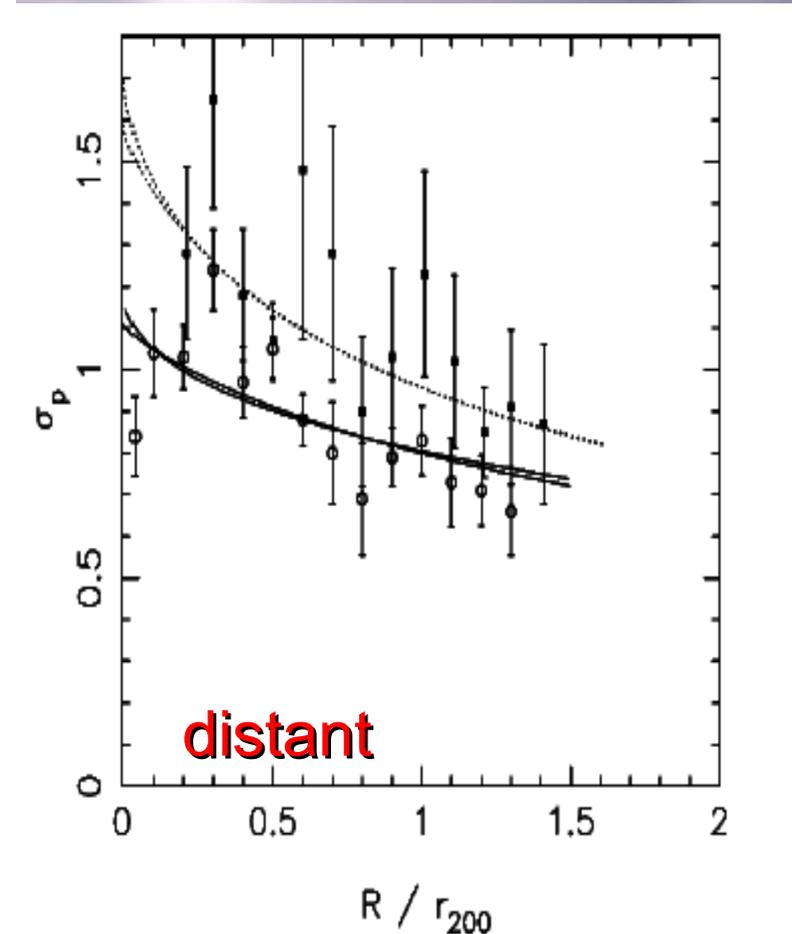
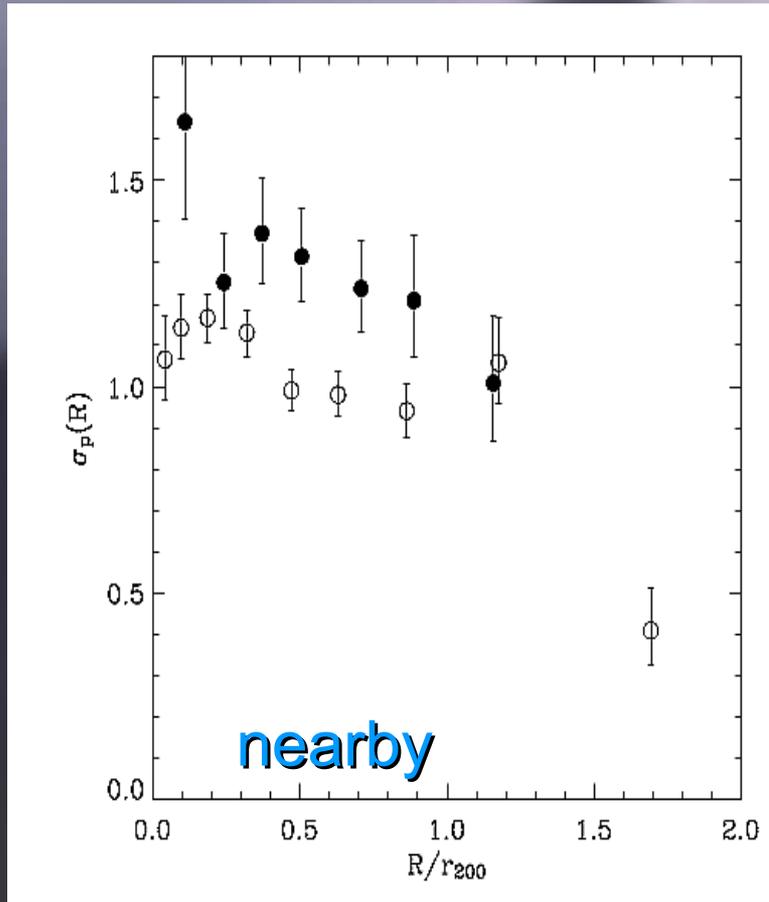
# ORBITS OF GALAXIES IN CLUSTERS: EVOLUTION

# Compare ENACS vs. CNOC



Number density profiles for early- (empty symbols) and late- (filled symbols) cluster galaxies

# Compare ENACS vs. CNOC



$\sigma_p(R)$  profiles for early- (empty symbols) and late- (filled symbols) cluster galaxies

Early-type galaxies at  $z \approx 0$  &  $z \approx 0.3$ : isotropic orbits

*(Katgert, B. & Mazure 04; van der Marel et al. 00)*

Late-type galaxies at  $z \approx 0$ : radial orbits *(B. & Katgert 04)*

No evolution of  $(R, v)$  distributions  
of early- and late-type galaxies from  $z \approx 0$  to  $z \approx 0.3$

*(Carlberg et al. 97 vs. B. & Katgert 04)*

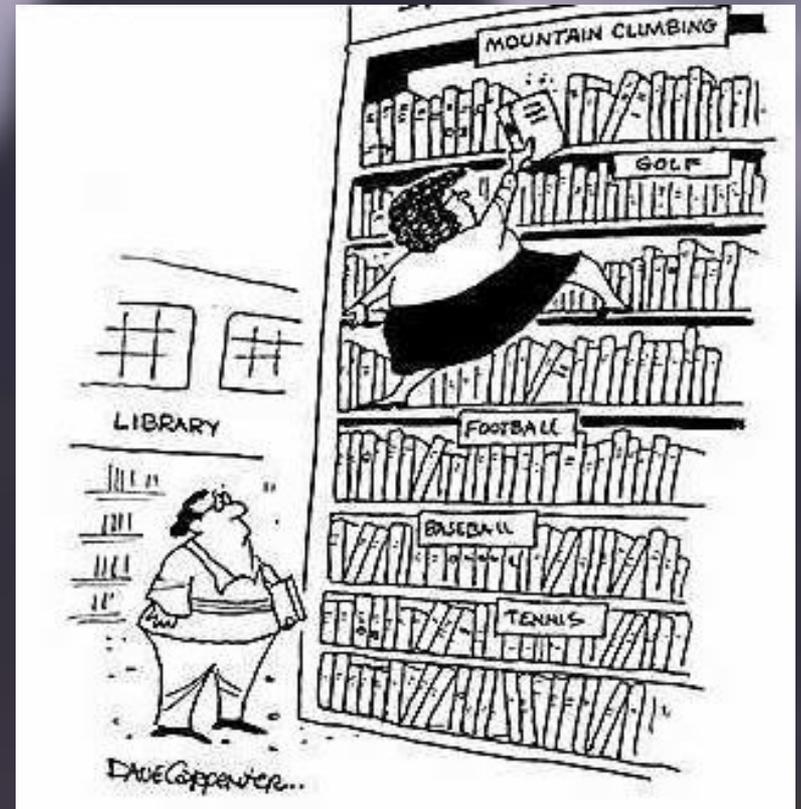
**$\Rightarrow$  late-type galaxies at  $z \approx 0.3$  must also be on radial orbits like late-type galaxies at  $z \approx 0$**

The late-type -galaxy fraction increases with  $z$ ,  
hence more cl. galaxies are on radial orbits at higher  $z$

**$\Rightarrow$  the infall rate increases with  $z$**

*(in agreement with Ellingson et al. 2001)*

# CONCLUSIONS



An example of YDS climbing class 6

Density profiles of clusters are as predicted by  $\Lambda$ CDM models; if cored, core  $\simeq 0.1 r_{200} \sim$  cD size  
( $\rightarrow$  DM particles cross-section)

DM more concentrated than baryons  
( $\rightarrow$  effectiveness of dyn. friction & adiabatic contraction)

Groups: higher concentration than predicted by  $\Lambda$ CDM?  
dissipation processes at work?  
(...TBC: need better statistics)

Red (early-type) galaxies move on isotropic orbits,  
Blue (late-type) galaxies move on slightly radial orbits  
Substructures move on tangential orbits  
( $\rightarrow$  cluster accretion history, galaxy evolution in clusters)

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- The best fitting Burkert core-radius is small,  
0.1  $r_{200}$   $\sim$  size of central cD  
→ DM scattering cross section  $< 2 \text{ cm}^2 \text{ g}^{-1}$   
(By comparison with simulation res. of Meneghetti et al. 2001)

*Much smaller than the  $5 \text{ cm}^2 \text{ g}^{-1}$  needed to fit dwarf galaxy mass density prof., Davé et al. (2000)*

- DM is *more* concentrated than the total matter

*Dynamical friction mechanism ineffective in transferring galaxy energy to DM in clusters or counteracted by adiabatic contraction  
(e.g. Zappacosta et al. 2006)*

# Future work

**Num.simulations:** investigate physics of evolution of orbits of galaxies in clusters and find optimal algorithm for  $M(r)$ ,  $\beta(r)$   
(ongoing collaboration with Borgani, Dolag, Mamon, Murante et al.)

**More data:** Improve current constraints on cluster  $M(r)$  and  $\beta(r)$  by combining existing data-bases and using new ones  
(e.g.: W I N G S, **see A. Cava's poster**, ongoing collaboration with Bettoni, Cava, D'Onofrio, Fasano, Moles, Poggianti, Ramella, Varela)

**Higher z:** Evolution of  $M(r)$  and  $\beta(r)$ , extend the analysis to higher-z cluster samples  
(e.g.: I C B S, possible collaboration with Dressler, Poggianti et al.)

*Thank you for your attention!*



**An example of YDS climbing class 7  
(...my favorite!)**