

Measuring the IGM thermal state with wavelets

Antonella Garzilli



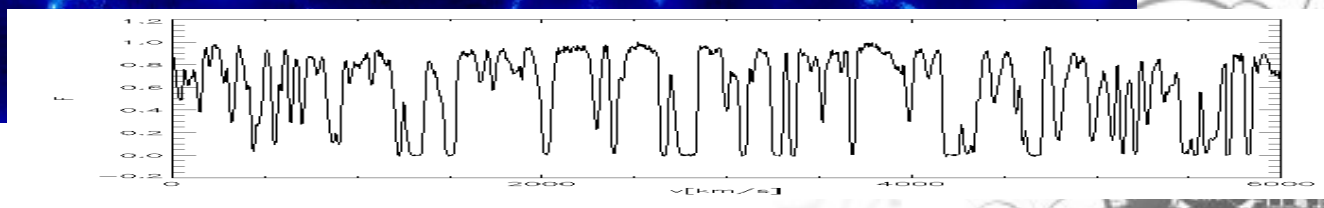
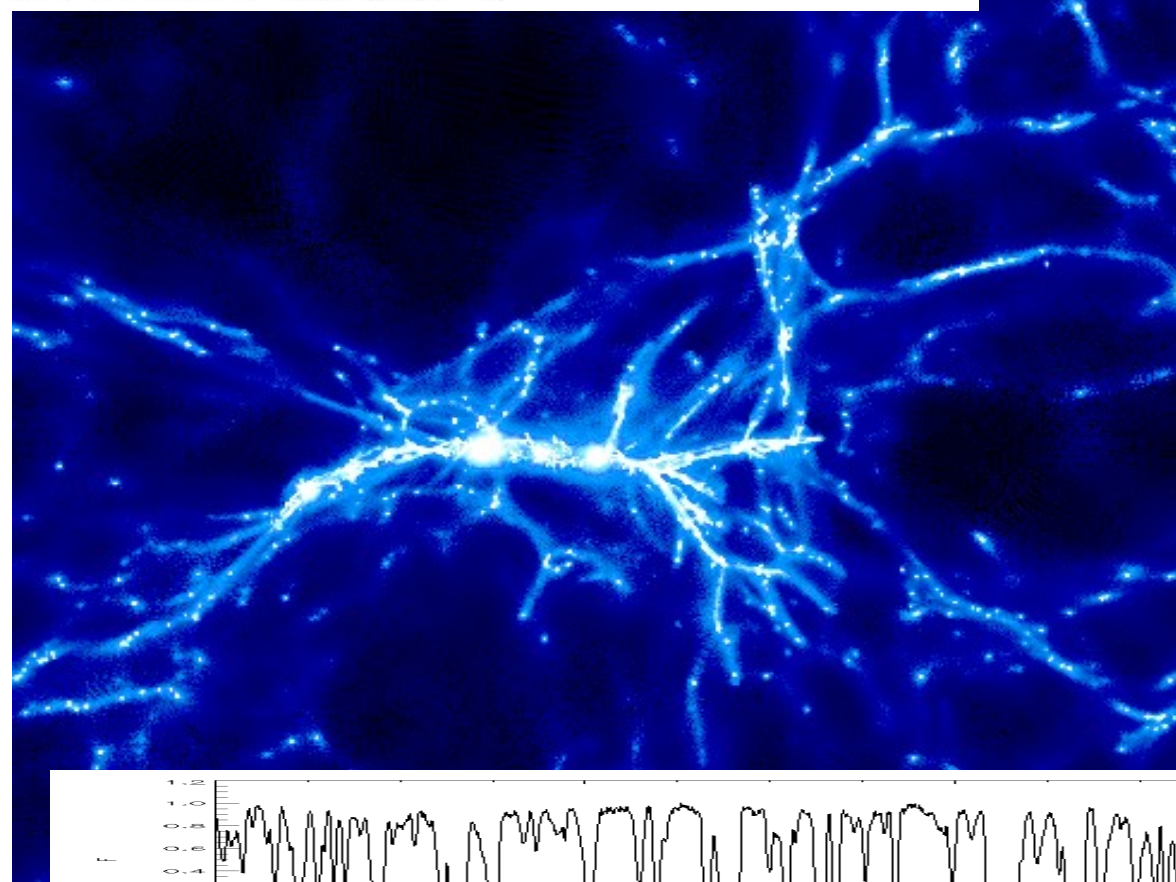
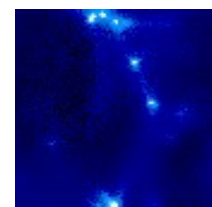
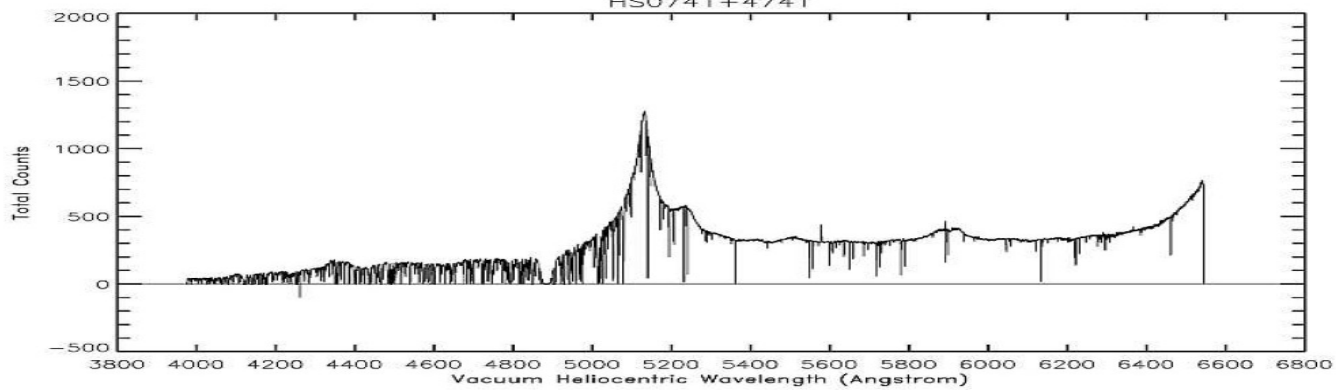
In collaboration with:

Samuel Leach, Matteo Viel and James Bolton

ArXiv:1202.3577, accepted for publication on MNRAS

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HS0741+4741




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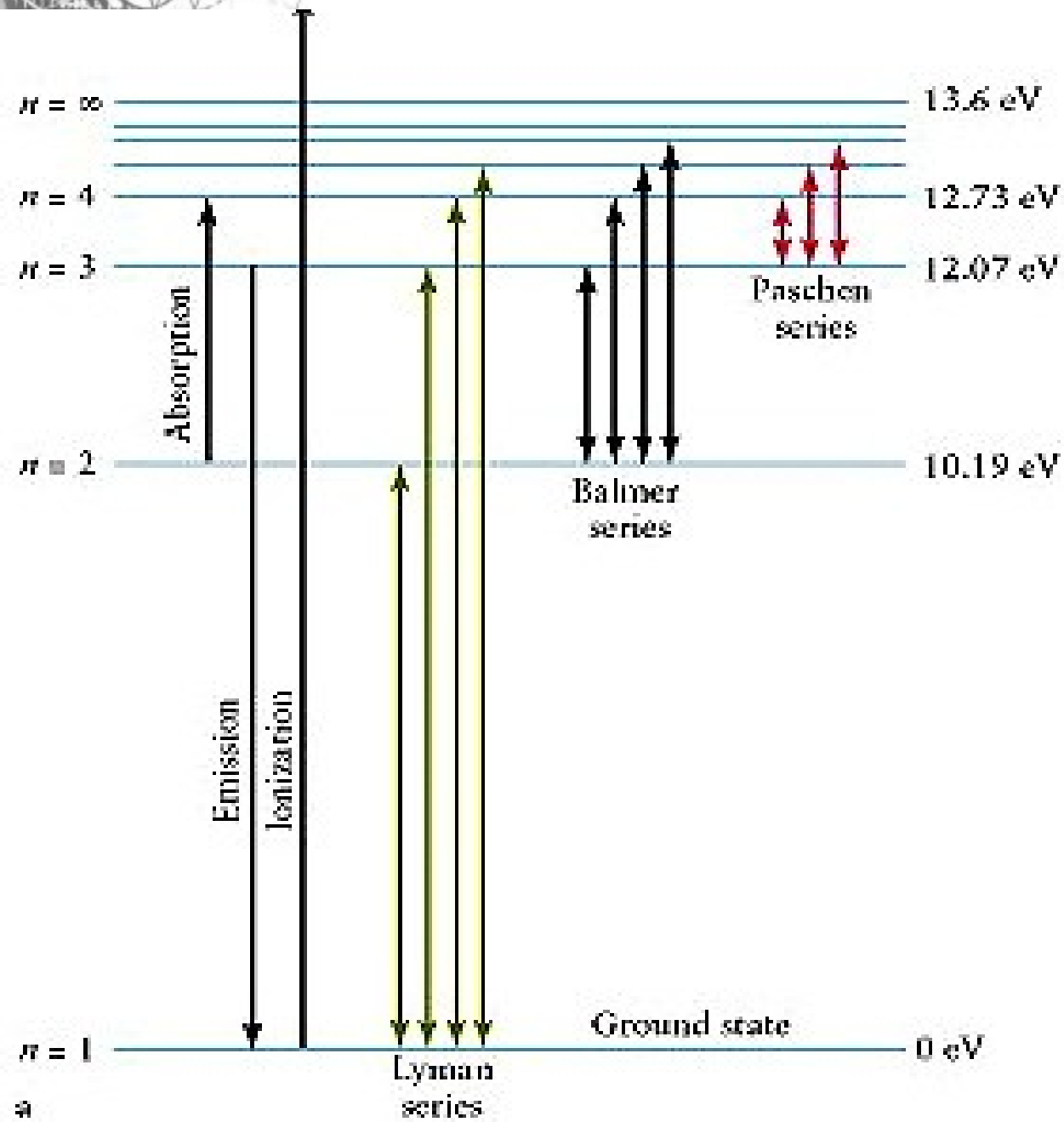
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Outline

- ***Physics of IGM***
 - Previous measurements of thermal state at $z \sim 2-3$
 - What are wavelets?
 - How we applied wavelets
 - Results
 - Comparison with recent work
 - Future work
- 

Lyman alpha series



$$\frac{1}{\lambda} = R \left(\frac{1}{1^2} - \frac{1}{n^2} \right)$$

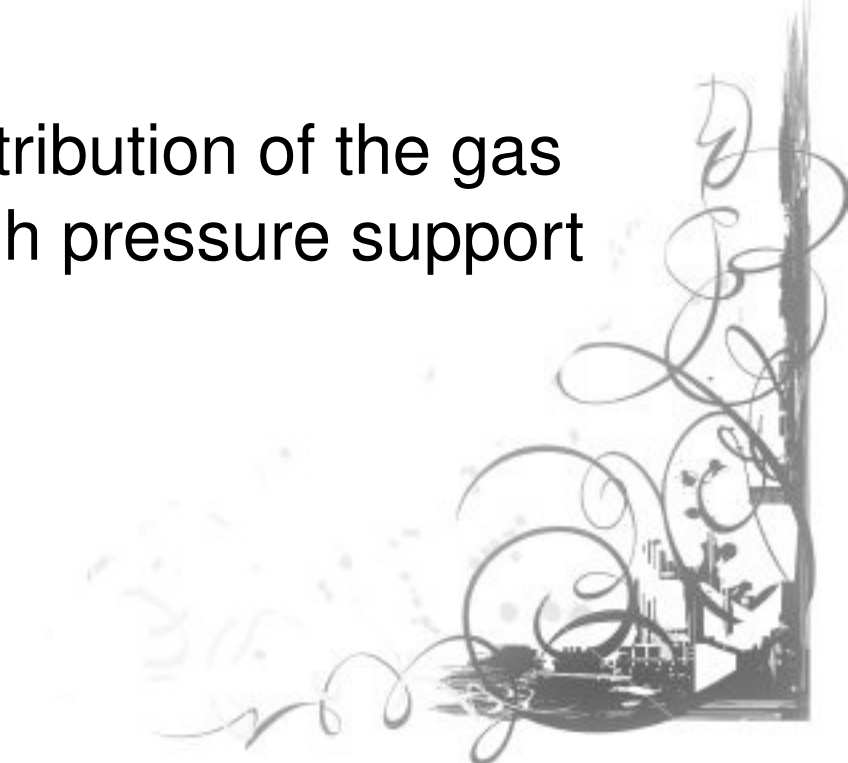
For Lyman α $n = 2$

$$Ly_{\alpha} \simeq 1215 \text{ \AA}$$





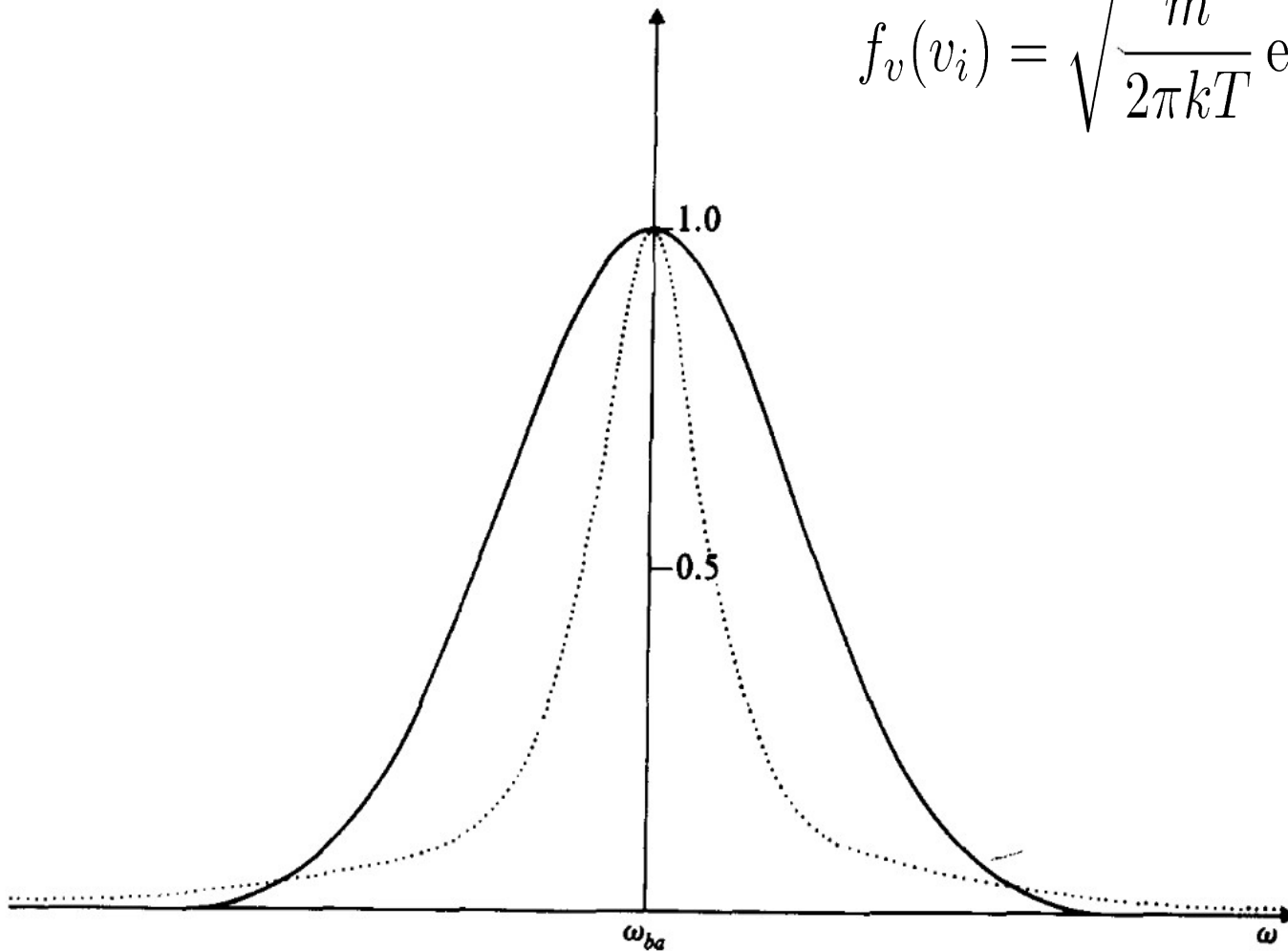
Temperature & IGM structure

- ★ **Thermal broadening:**
smoothing absorption along the line of sight through the thermal motion of the gas
 - ★ **Jeans smoothing:**
smoothing the physical distribution of the gas in three dimensions through pressure support
- 

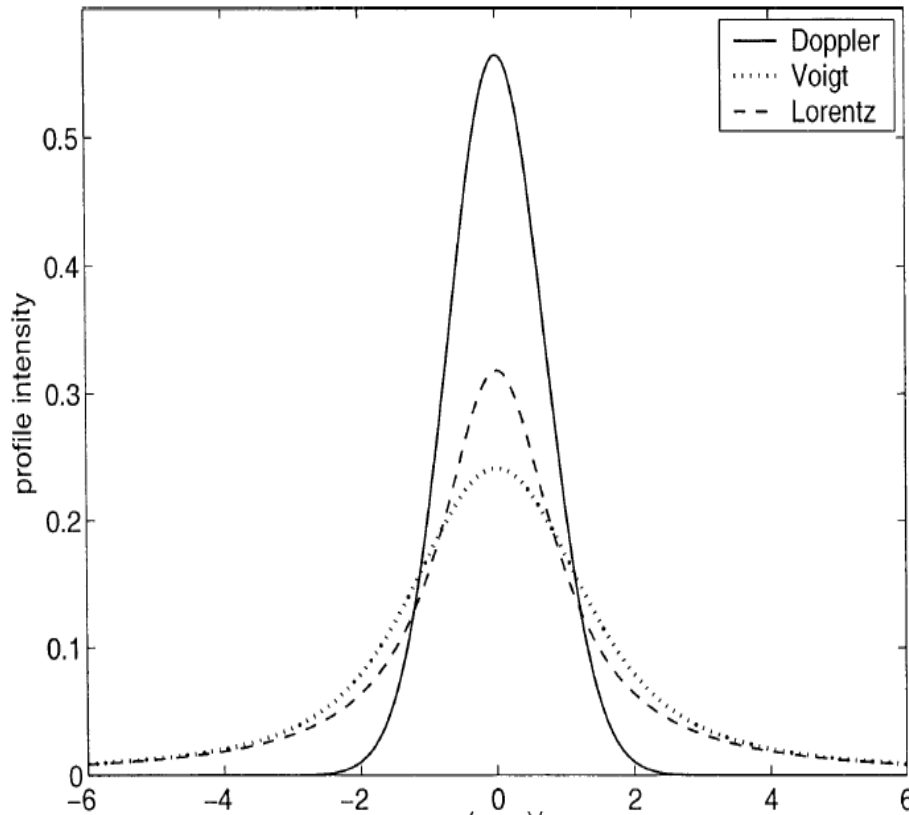
Natural profile and doppler broadening

$$\sigma_{\nu} = \left(\frac{\pi e^2}{m_e c} \right) \left[\frac{1}{4\pi\epsilon_0} \right] f_{lu} \frac{(\Gamma_{ul}/4\pi^2)}{(\nu - \nu_{lu})^2 + (\Gamma_{ul}/4\pi)^2}$$

$$f_{\nu}(v_i) = \sqrt{\frac{m}{2\pi kT}} \exp \left[-\frac{mv_i^2}{2kT} \right]$$



Voigt profile



$$b = \sqrt{\frac{2k_b T}{m}}$$

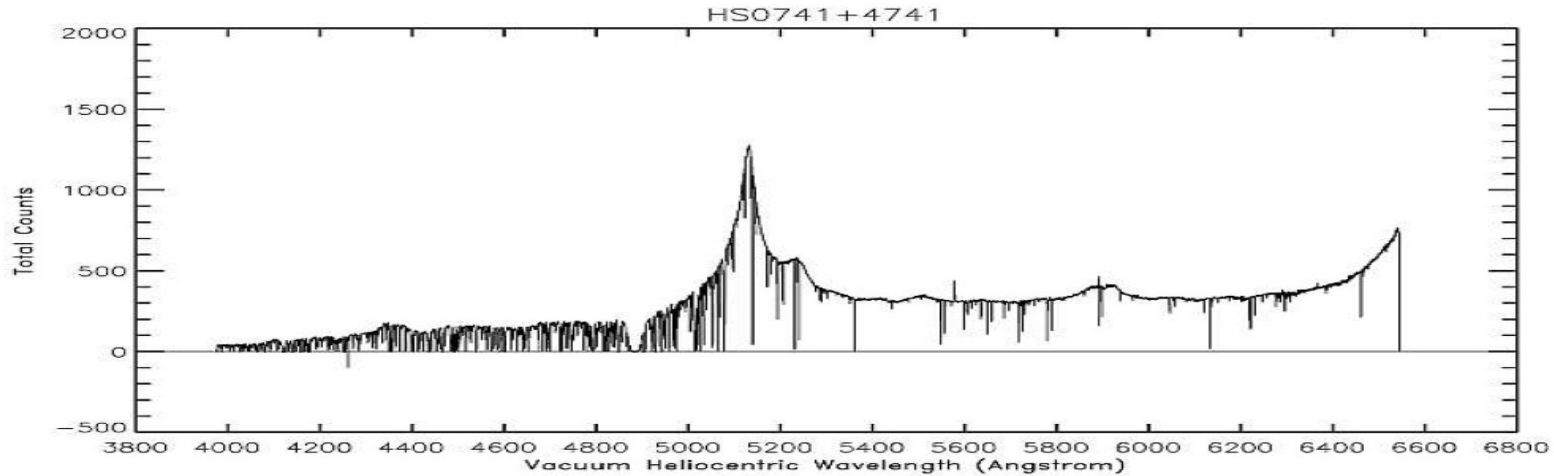
$$a = \frac{\Gamma_{ul}}{4\pi\Delta\nu_D}, \quad \Delta\nu_D = \nu_{lu} \frac{b}{c}$$

$$x = \frac{\nu - \nu_{lu}}{\Delta\nu_D}$$

$$\sigma_\nu = \left(\frac{\pi e^2}{m_e c} \right) \left[\frac{1}{4\pi\epsilon_0} \right] f_{lu} \phi(a, \nu)$$

$$\phi(a, \nu) \approx H(a, x) = \frac{a}{\pi} \int dy \frac{e^{-y^2}}{(x-y)^2 + a^2}$$

Gunn-Peterson effect



$$\lambda_{lu} < \lambda < \lambda_{lu} \frac{a(t)}{a(t_0)} \quad t_0 \text{ emission time}$$

$$\tau_\nu = \int_{s_0}^s ds' n(s', t') \sigma_{\nu'} =$$

$$= 1.2 \cdot 10^4 \frac{(1+z)^3}{[\Omega_m(1+z)^3 + \Omega_K(1+z)^2 + \Omega_\nu]^{1/2}} \left(\frac{f_{lu} \lambda}{506.0 \text{ \AA}} \right) \left(\frac{\langle n \rangle}{\langle n_H \rangle} \right)$$

For an homogeneous medium

Discrete absorption features

$$\tau_\nu = \sum_i \tau_\nu(i)$$

$$\tau_\nu(i) = \int_{s_i - \Delta s/2}^{s_i + \Delta s/2} ds' n(s', t_i) \sigma_{\nu'} \quad \nu' = \nu \frac{a(t)}{a(t_i)}$$

$$\tau_\nu = \pi^{1/2} \tau_0 \langle \phi(a, x) \rangle$$

$$\tau_0 = \frac{\pi^{1/2} e^2}{m_e c} \left[\frac{1}{4\pi\epsilon_0} \right] \frac{N}{b} \lambda_{lu} f_{lu} \quad \text{Optical depth line centre}$$

Expressing absorption features like discrete spatial structure is an approximation

IGM is an evolving spatial continuum

Discrete absorption features

TABLE I Summary of absorption line system properties

Absorber class	Line parameters			Physical characteristics		
	N_{HI} (cm^{-2})	b^a (km s^{-1})	n^b (m^{-3})	T^b (K)	Size (kpc)	$[M/H]^c$
Ly α forest	$\lesssim 10^{17}$	15–60	0.01 – 1000	5000 – 50000	15–1000(?)	-3.5 – -2
LLS	$10^{17} - 10^{19}$	~ 15	$\sim 10^3 - 10^4$	~ 30000	–	-3 – -2
Super LLS	$10^{19} - 2 \times 10^{20}$	~ 15	$\sim 10^4$	~ 10000	–	-1 – +0.6
DLA	$> 2 \times 10^{20}$	~ 15	$\sim 10^7; \sim 10^4$	$\sim 100; \sim 10000$	$\sim 10 - 20(?)$	-1.5 – -0.8

^aApproximate ranges. Not well determined for most Lyman Limit Systems and super Lyman Limit Systems.

^bValues not well constrained by direct observations.

^cApproximate metallicity range, expressed as a logarithmic fraction of solar: $[M/H] = \log_{10}(M/H) - \log_{10}(M/H)_{\odot}$.

Ionization – Ultra Violet Background (UVB)

Steady state ionization equilibrium equations

$$1 - Y_{HI} = Y_{HI} I_{HI}$$

$$Y_{HeII} = Y_{HeI} I_{HeI}$$

$$1 - Y_{HeI} - Y_{HeII} = Y_{HeII} I_{HeII}$$

where

$$I_{HI} = \frac{\Gamma_{HI}}{n_e \alpha_{HI}(T)}$$

α_{HI} Recombination rate of hydrogen

$$\Gamma_{HI} = \int_{\nu_L}^{\infty} d\nu 4\pi \frac{J(\nu)}{h\nu} \sigma_{HI}(\nu)$$

Haardt et Madau, 1996

Equation of state for the IGM

The true equation of state of the gas is the ideal equation of state

The “equation of state” of the IGM is determined by equilibrium between:

- Photoheating of hydrogen and helium
- Cooling due to the adiabatic expansion of the Universe
- Recombination cooling

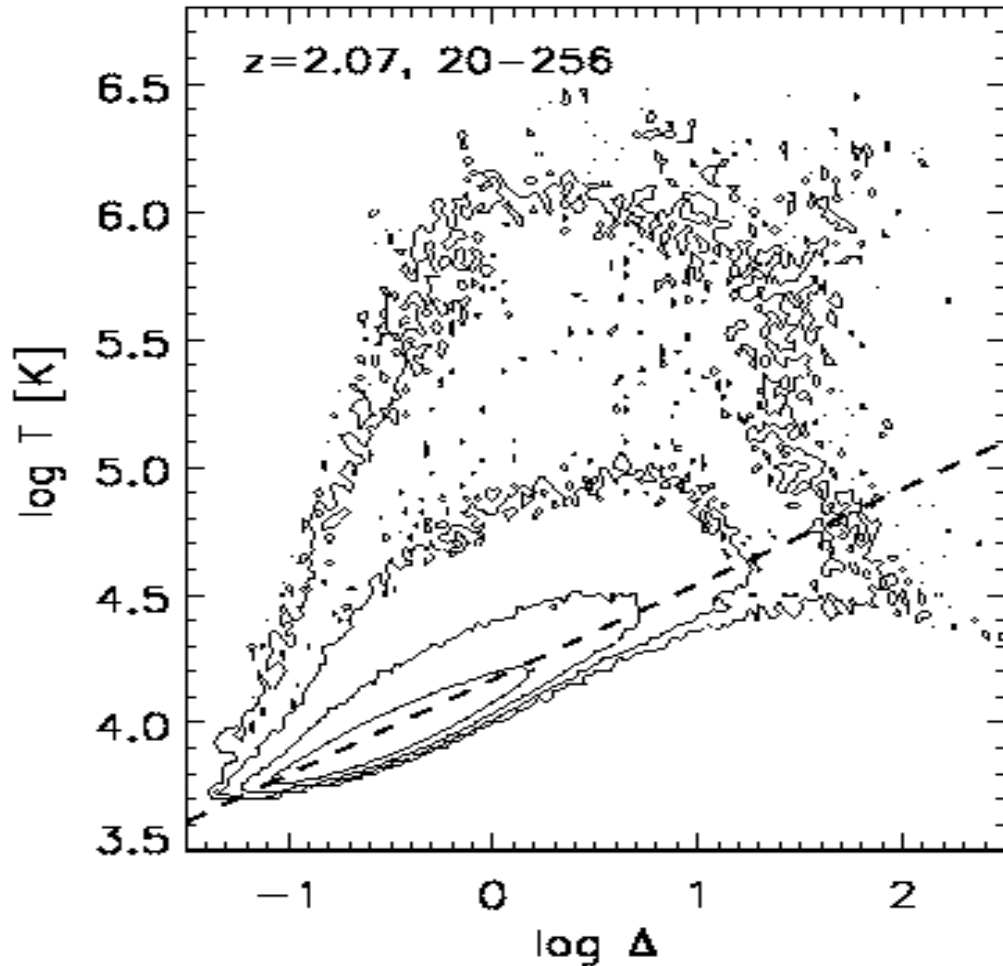
$$\frac{dT}{dt} = -2HT + \frac{2T}{3(1+\delta)} \frac{d\delta}{dt} - \frac{T}{\sum_i \tilde{X}_i} \frac{d\sum_i \tilde{X}_i}{dt} + \frac{2}{3k_B n_b} \frac{dQ}{dt}$$

Expansion of Universe

Change in number of species

Effect of surrounding radiation field

Equation of state for the IGM



$$T = T_0 \Delta^{\gamma-1}$$

$$T_0 \approx 10^4 K$$

$$\gamma \lesssim 1.62$$


$$\Delta = \frac{\rho}{\langle \rho \rangle} < 10$$

Bolton et al, 2008

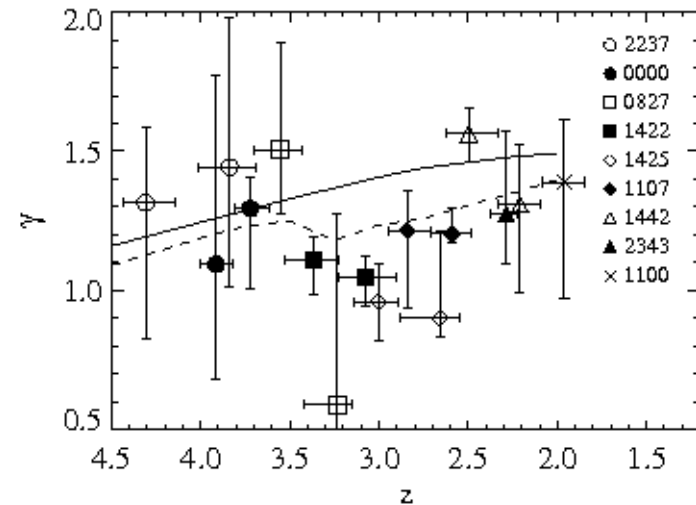
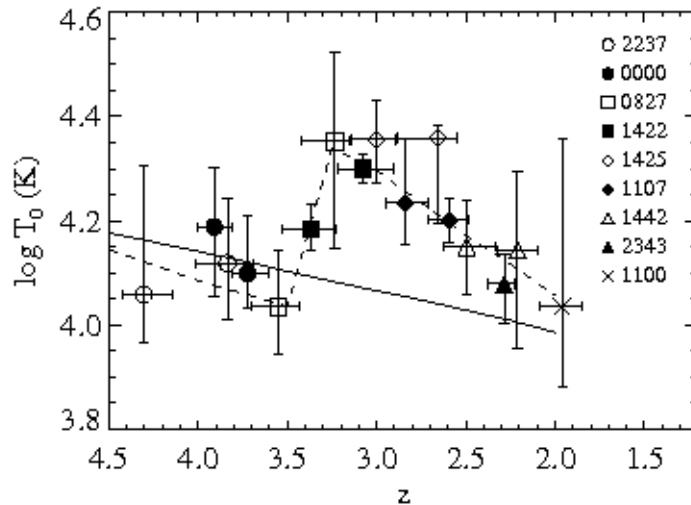
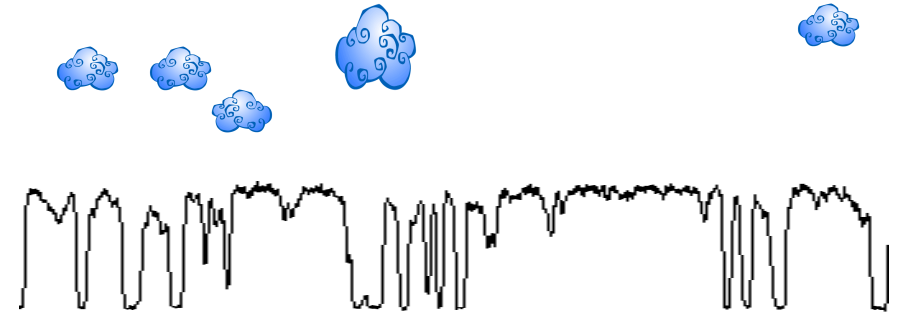
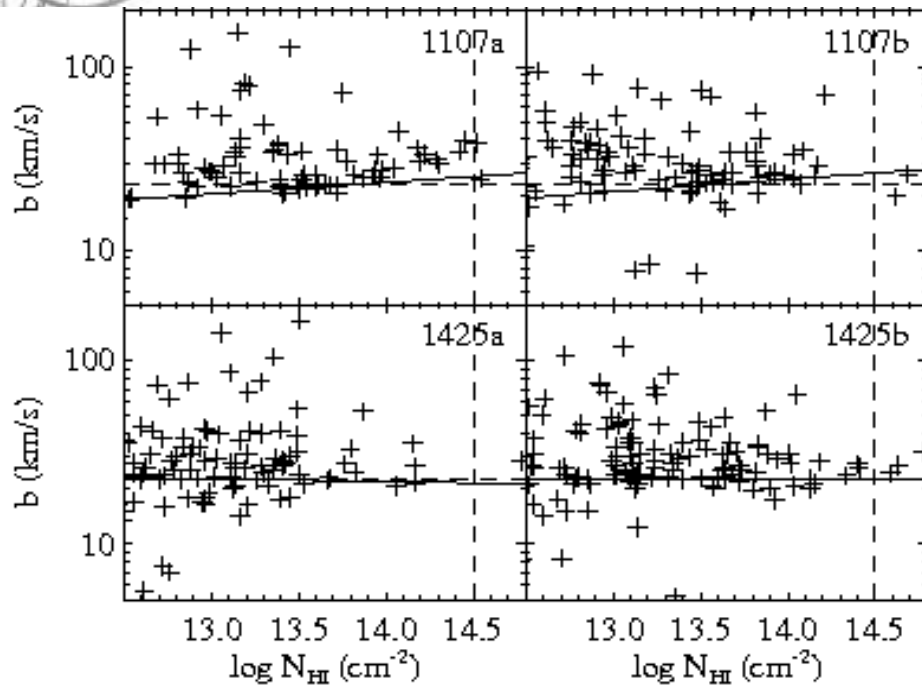
Hui et Gnedin, 1997



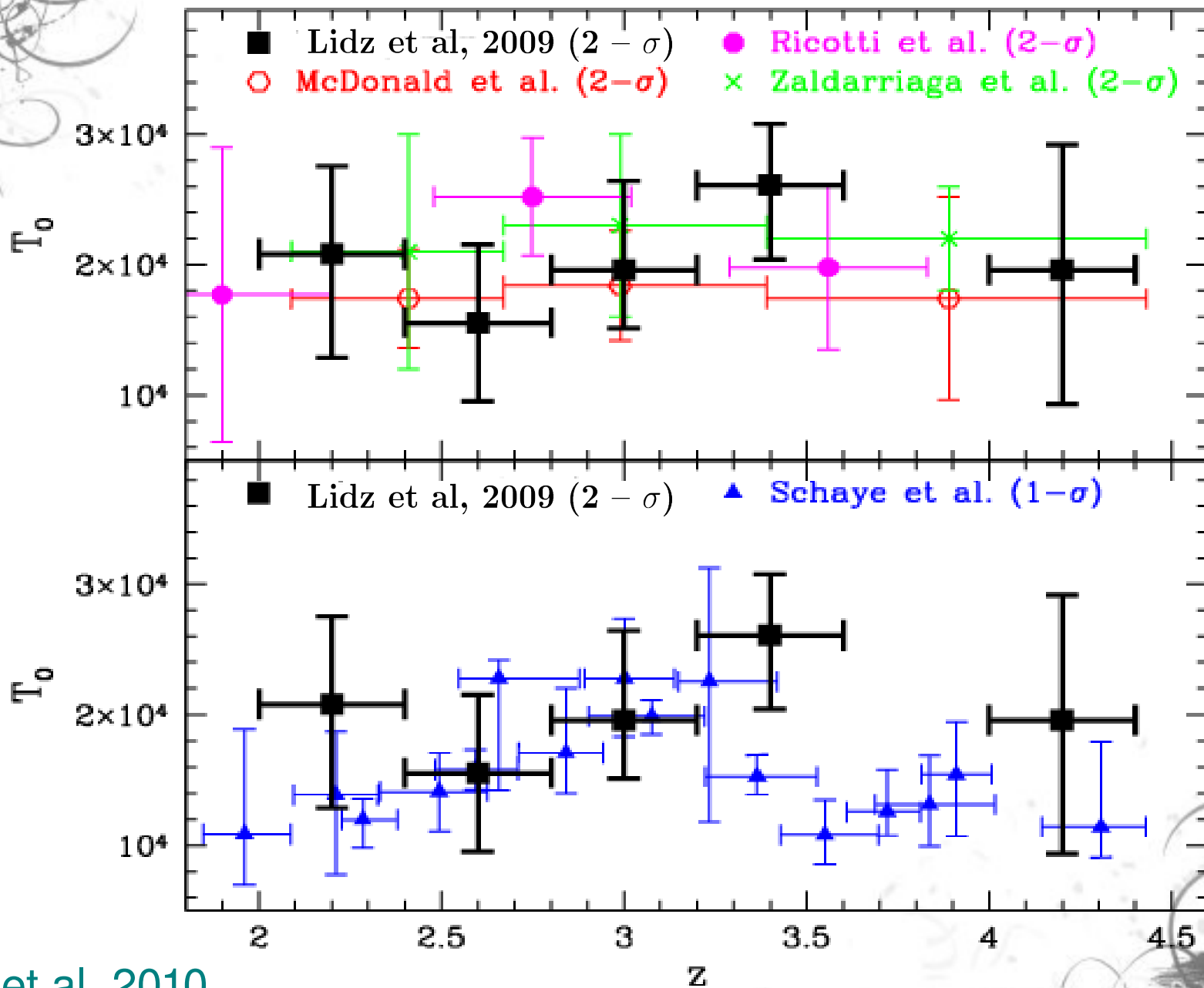
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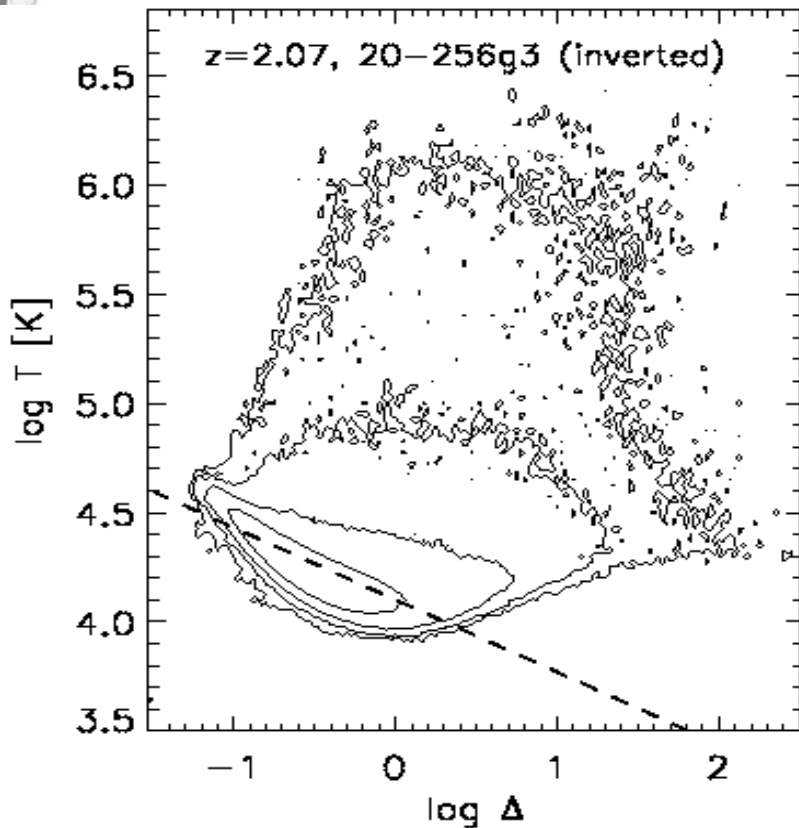
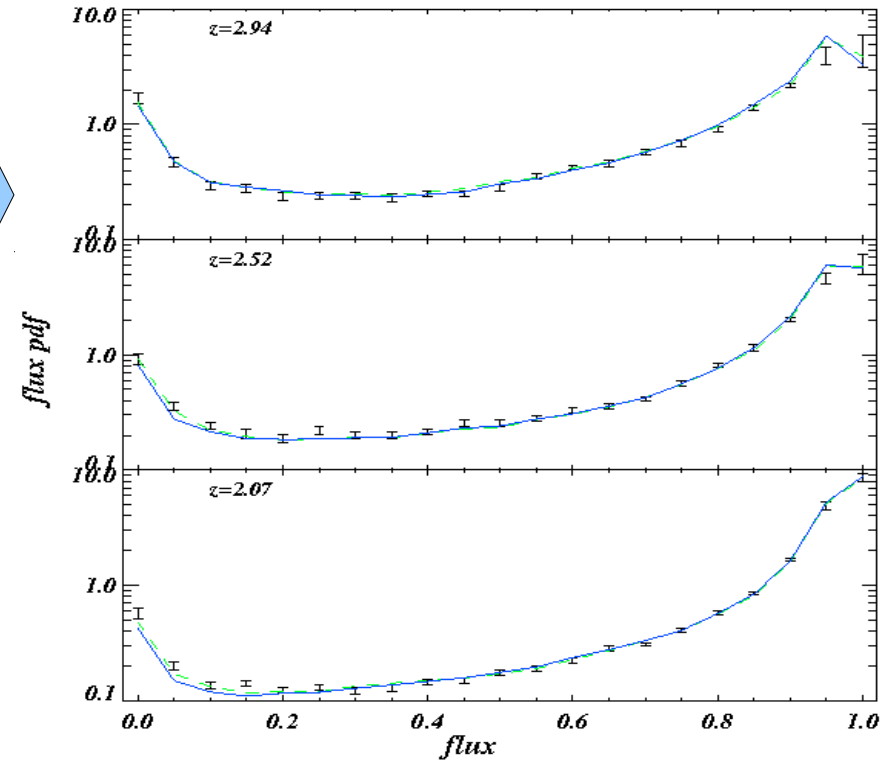
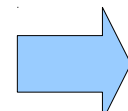
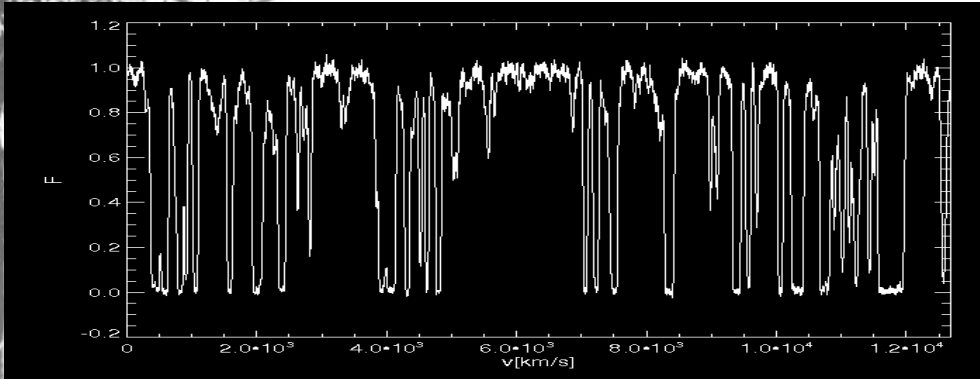
Thermal state of IGM -- Schaye et al (2000)



Thermal state of IGM



Thermal state of IGM – Flux PDF



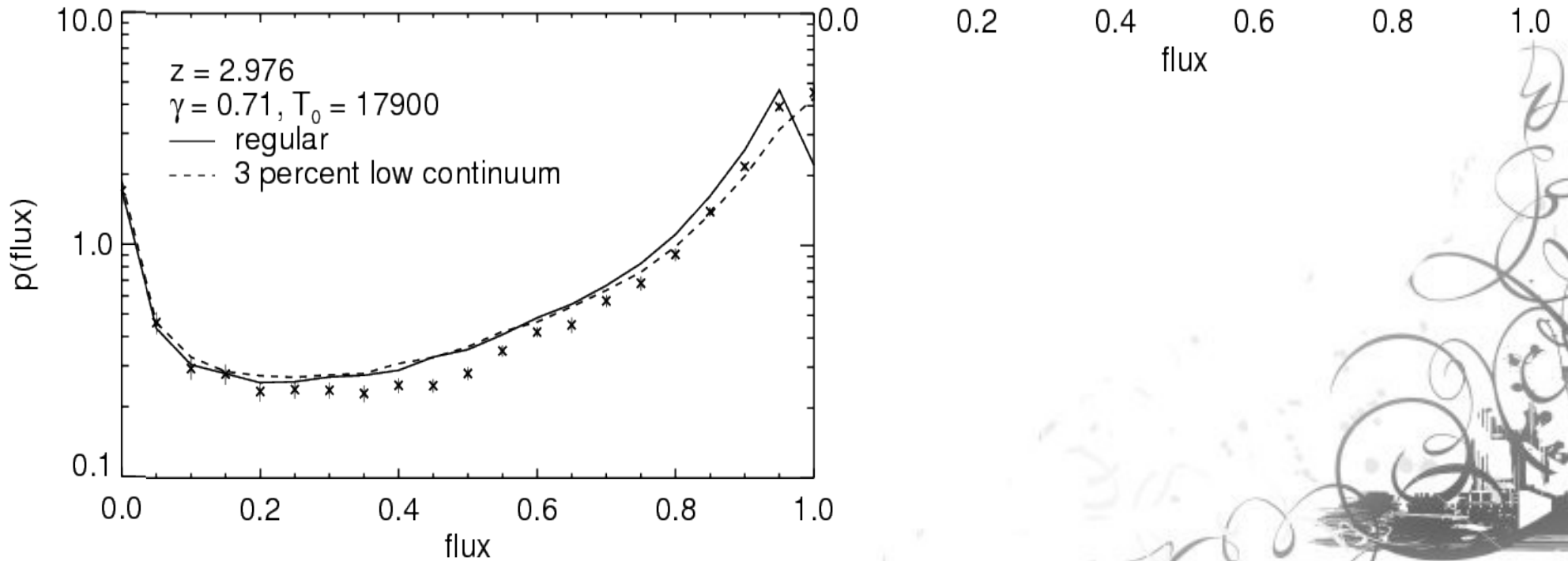
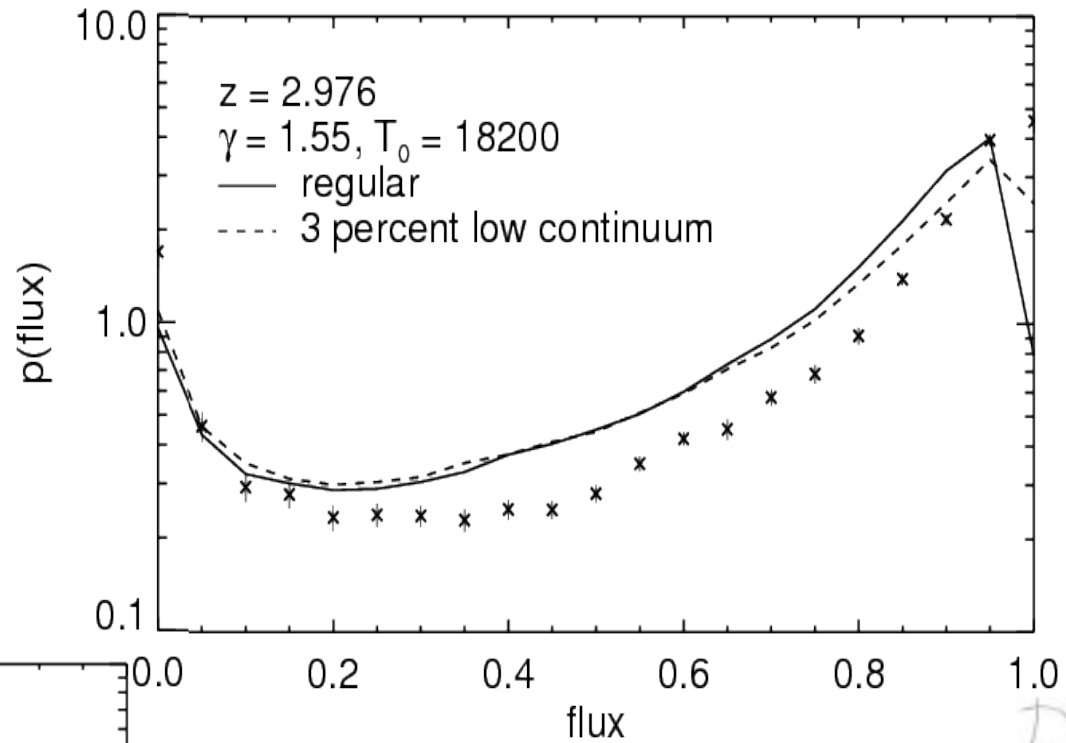
Viel et al, 2009

Bolton et al, 2008

Inverted equation of state

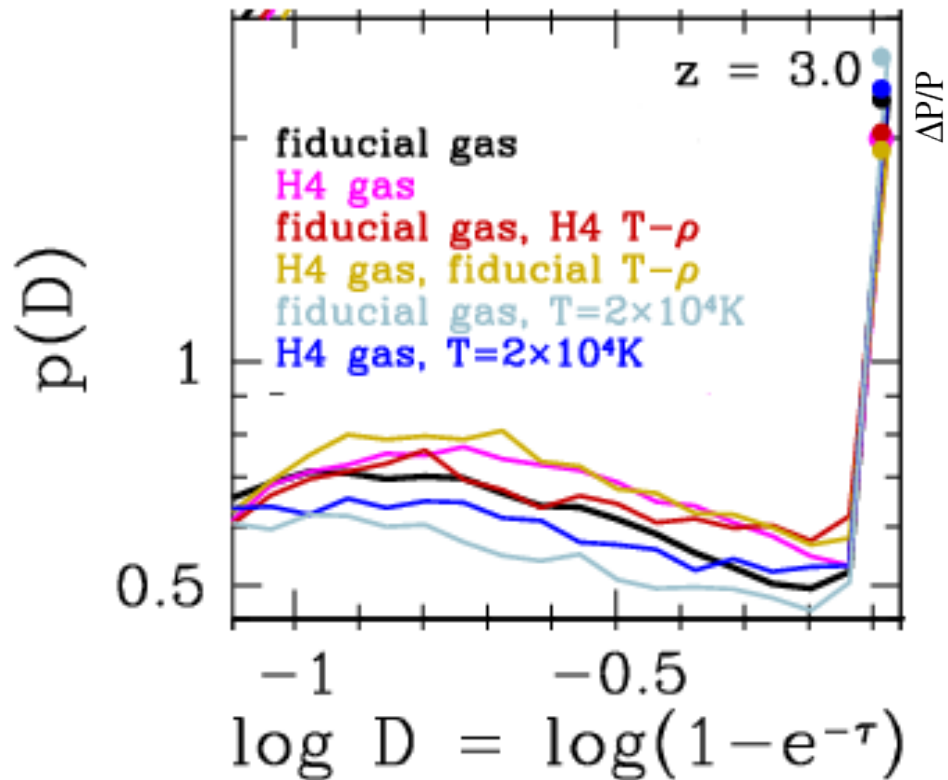
Furlanetto & Oh, 2008

Thermal state of IGM – Flux PDF

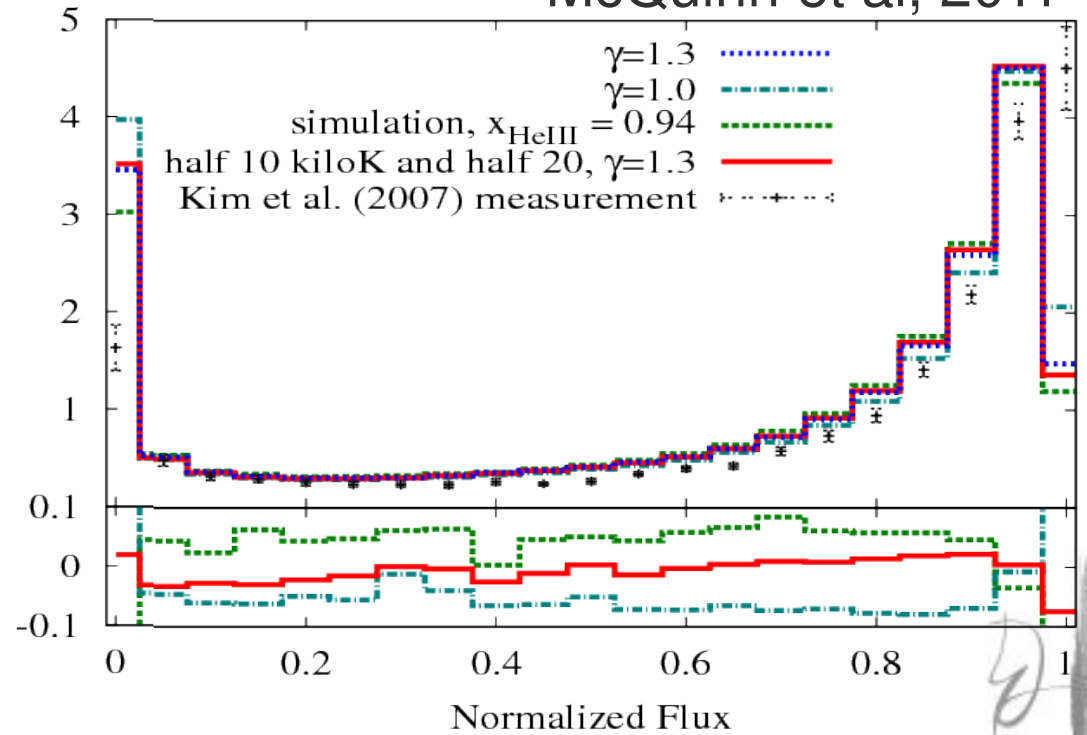


Thermal state of IGM – Flux PDF

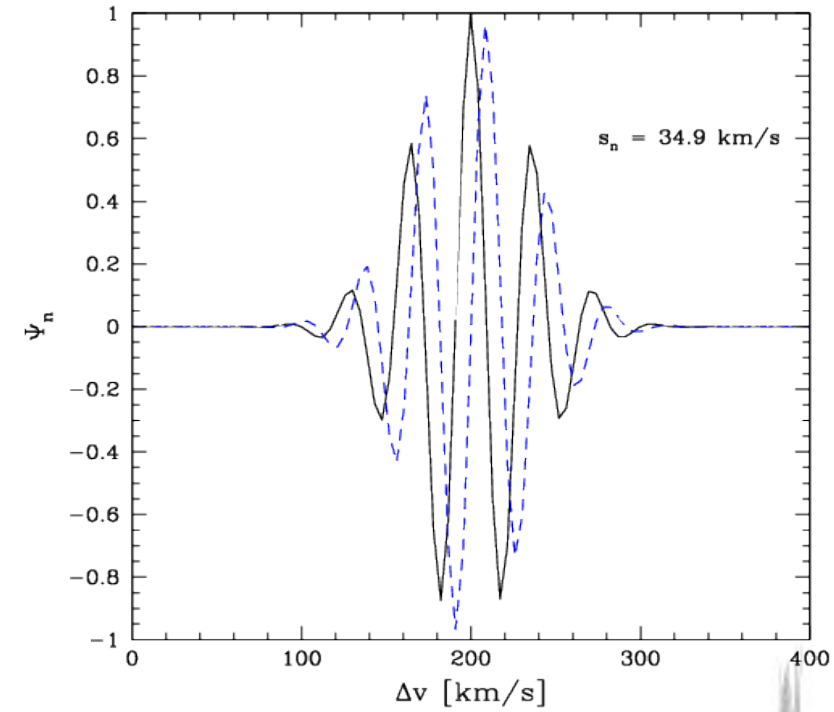
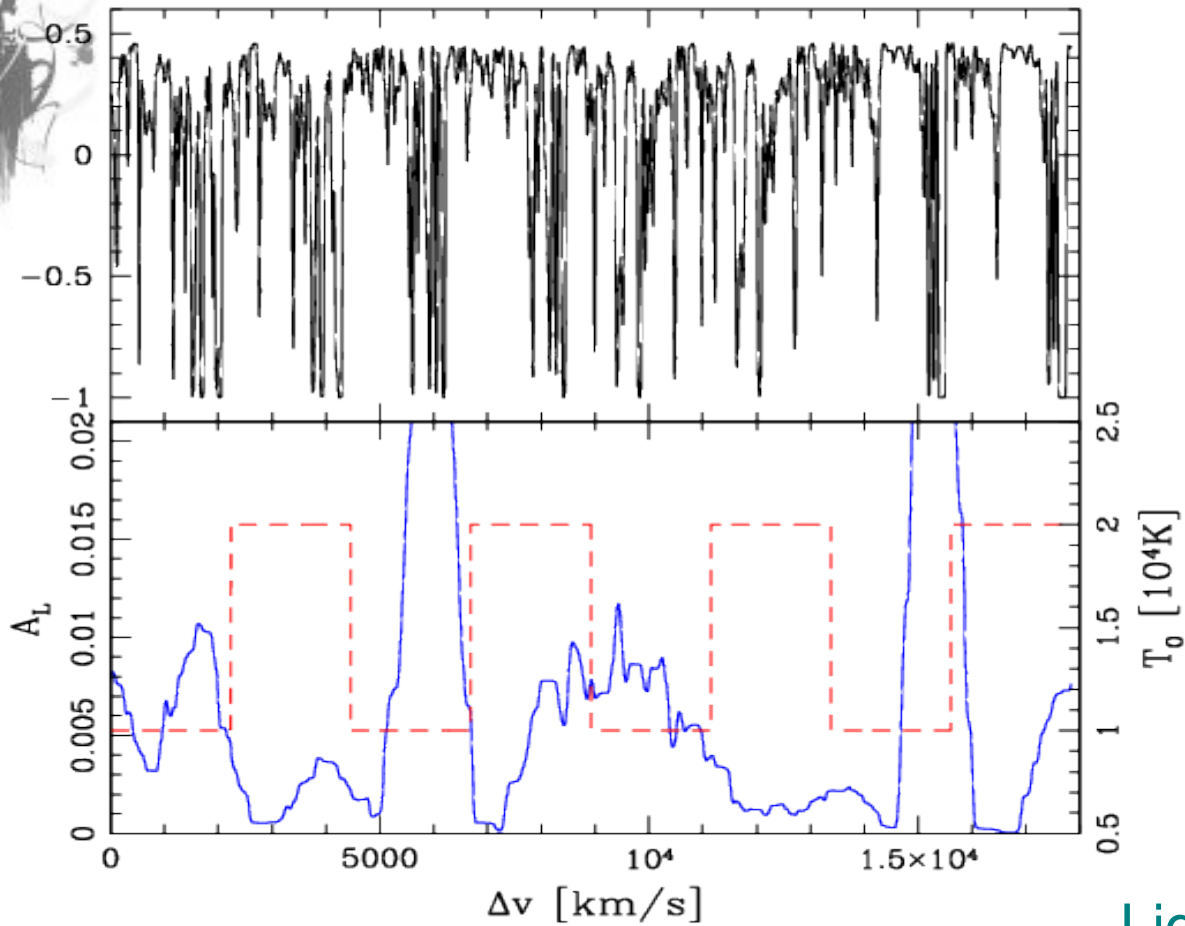
Peeples et al, 2010



McQuinn et al, 2011



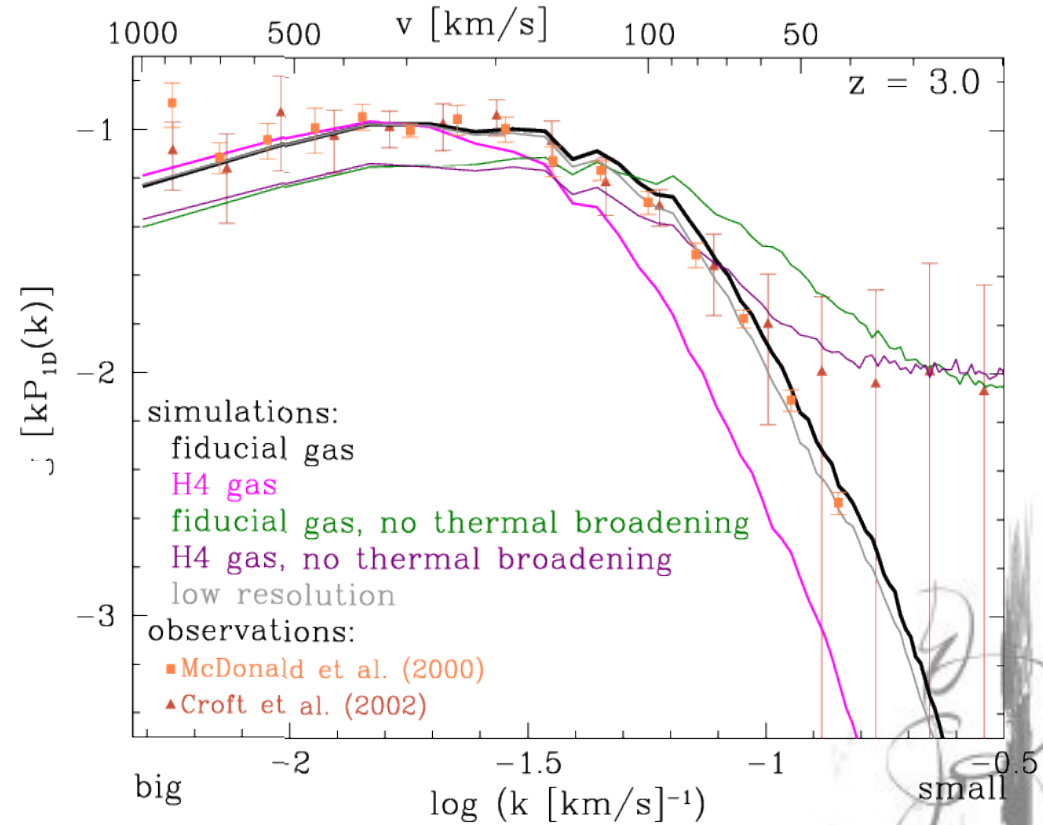
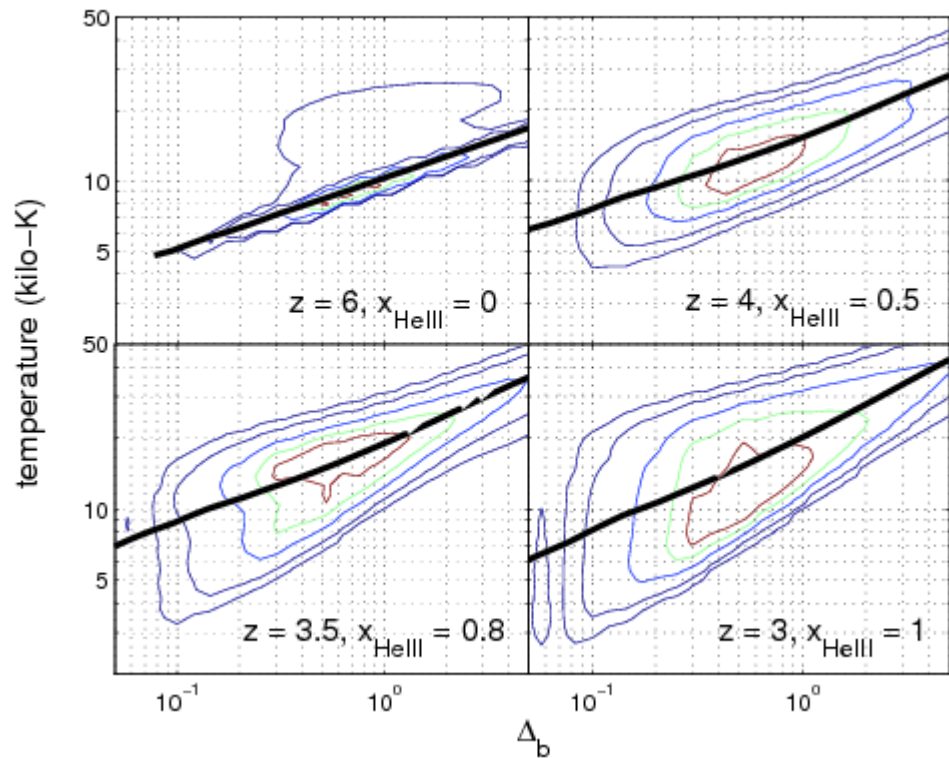
Thermal state of IGM – Wavelet filtering



Lidz et al, 2010

Thermal state of IGM – Wavelet filtering


McQuinn et al, 2009



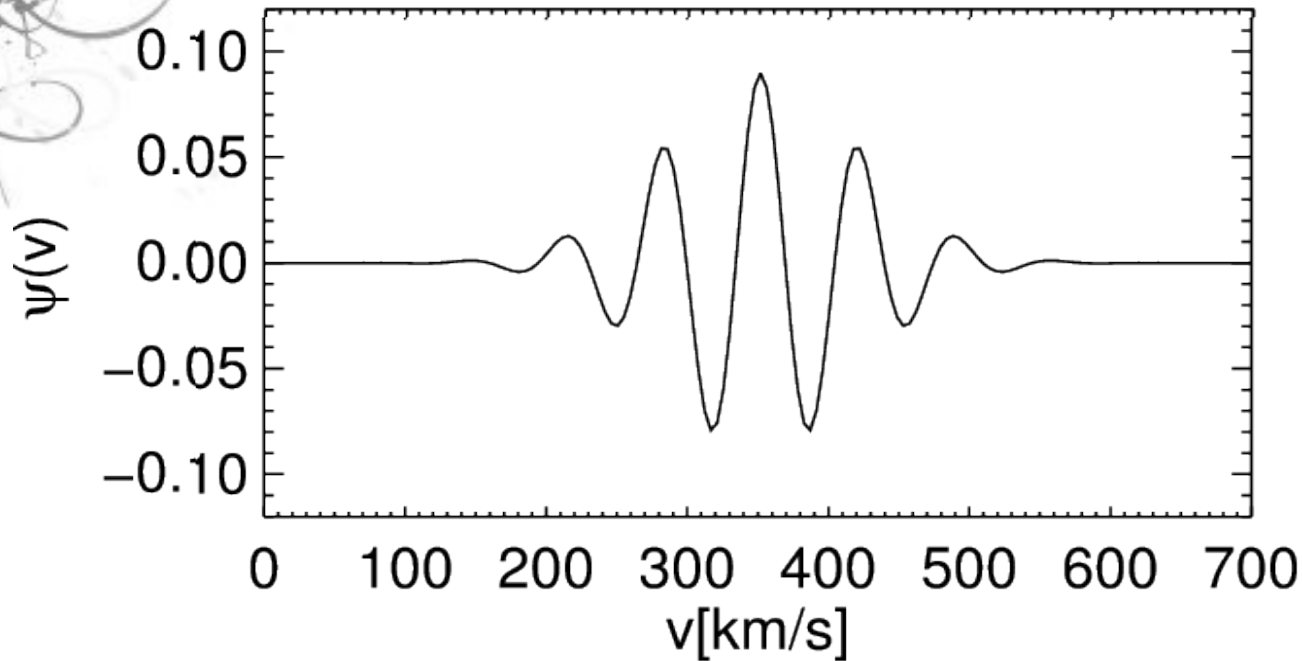
Peeples et al, 2010



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Wavelets

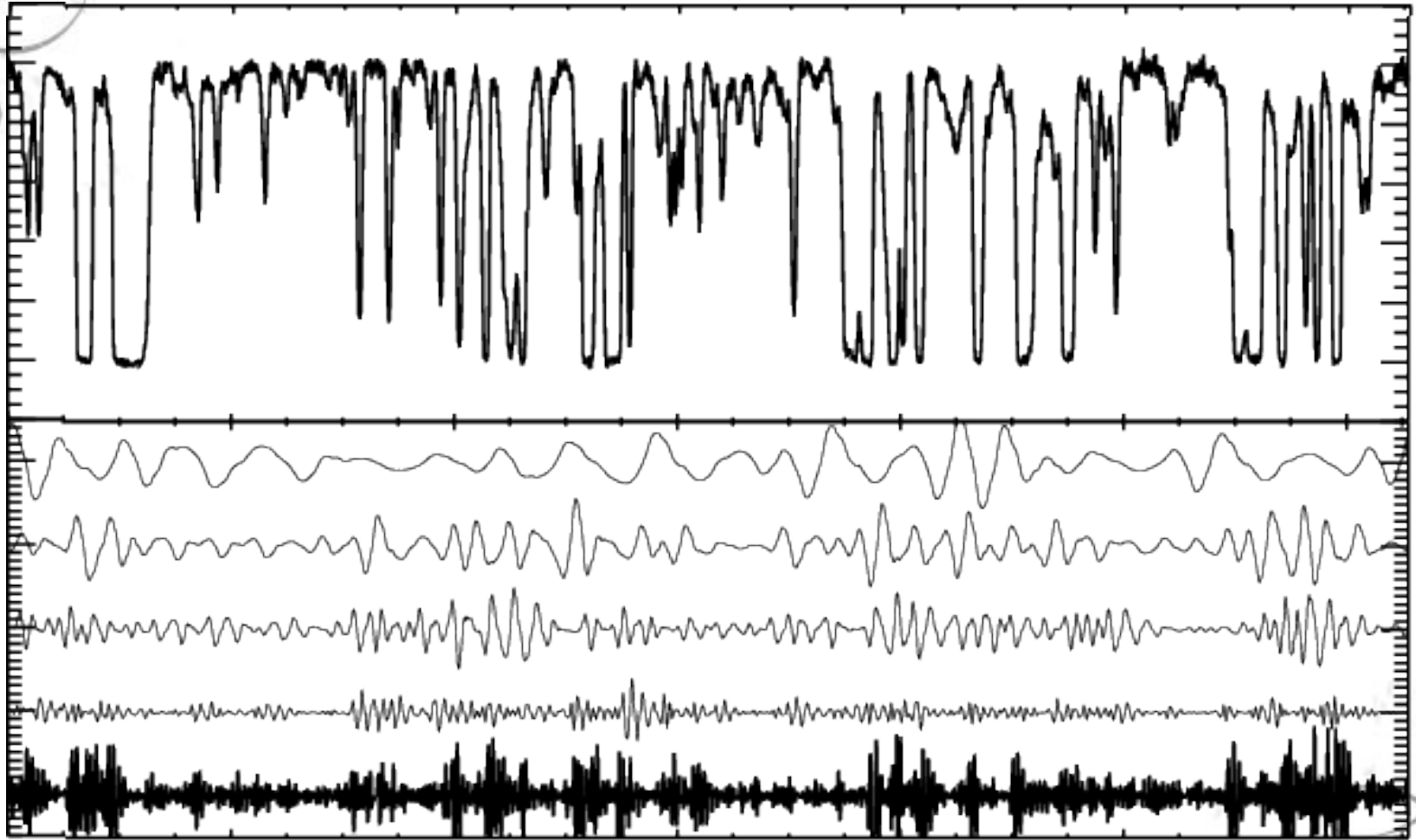


$$\psi_k(v) = \mathcal{A} \exp(-ikv/2\pi) \exp(-v^2/2s^2)$$

$$s = \frac{2\pi}{k}$$

Theuns et Zaroubi (2002)
Zaldarriaga (2002)


Wavelets



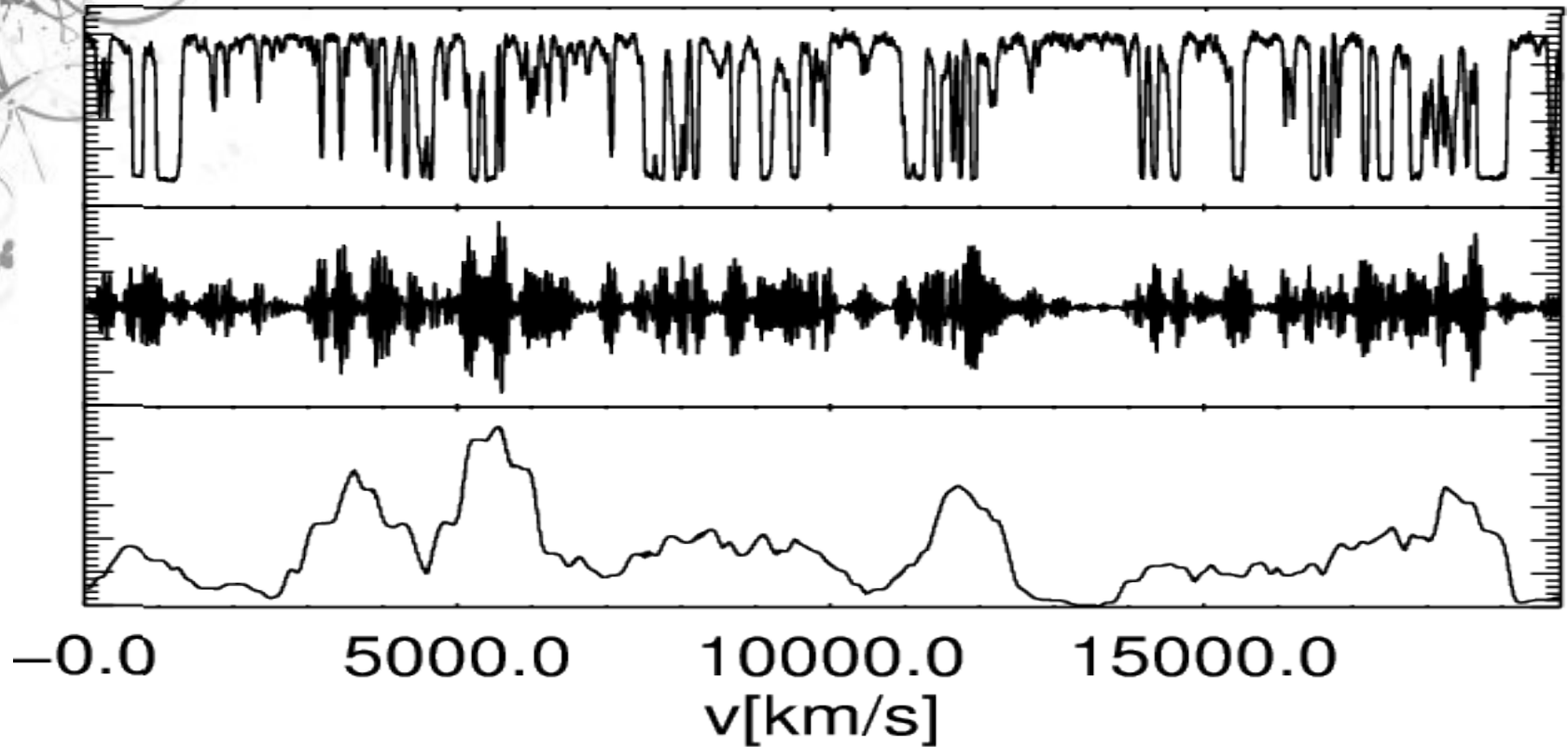
v (km/s)



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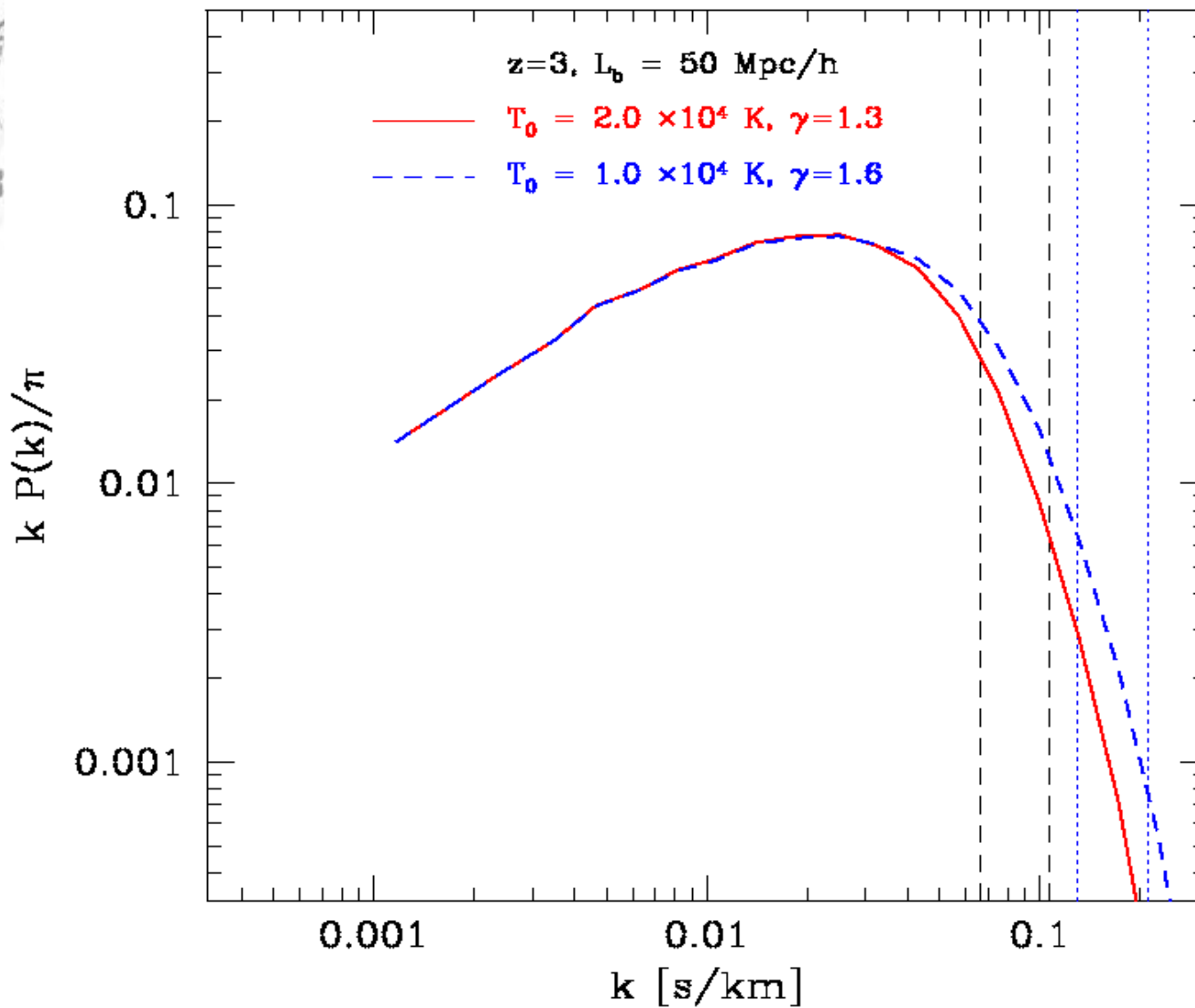
Wavelet amplitude of a spectrum



$$a(x) = \int dx' \psi(x - x') f(x')$$

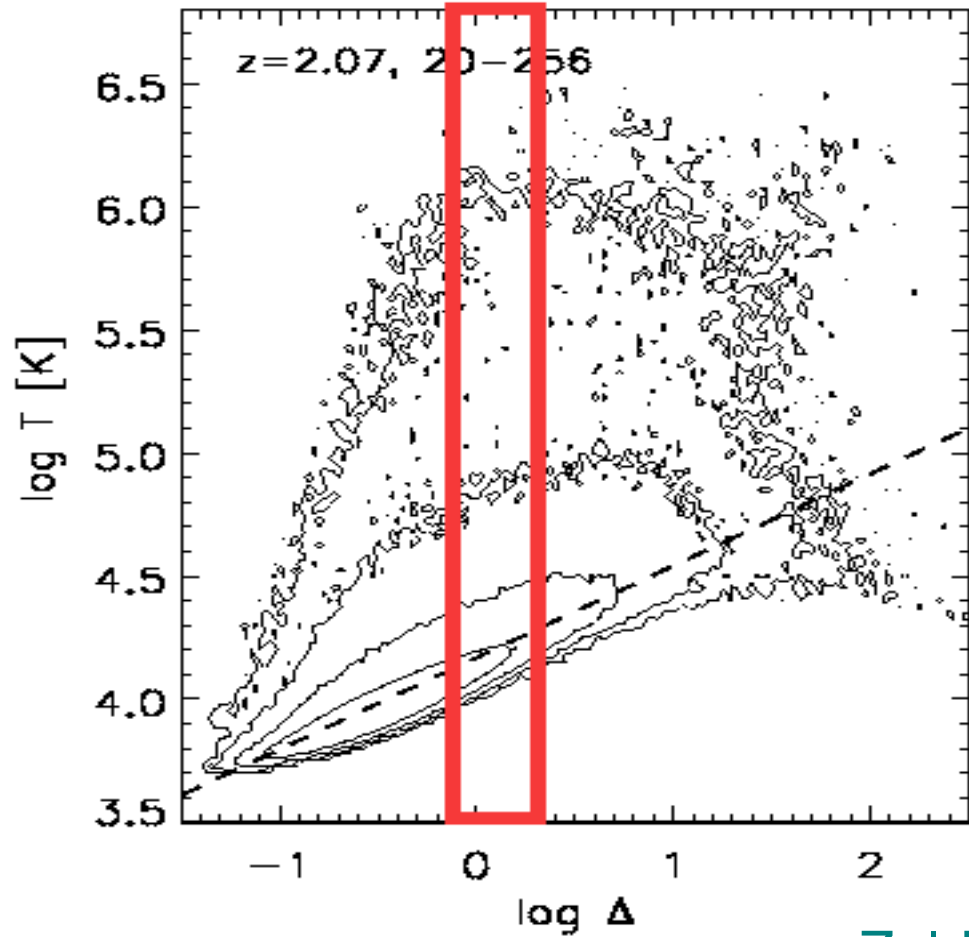
$$A_L(x') = \int_{-\infty}^{+\infty} dx' \Theta(|x - x'|, \frac{L}{2}) |a(x')|^2$$

Wavelet and power spectra



Lidz et al, 2010

Gas densities probed by wavelets



$$0.9 < \Delta < 1.8$$

for $z \sim 3$

Zaldarriaga et al, 2001

Linking theory with observations

Observed spectra

- 18 spectra from UVES of VLT (Kim et al, 2007)
- Metal cleaned
- Continuum fitted
- Normalized
- High S/ N ~ 50

Hydrodynamical Numerical simulations

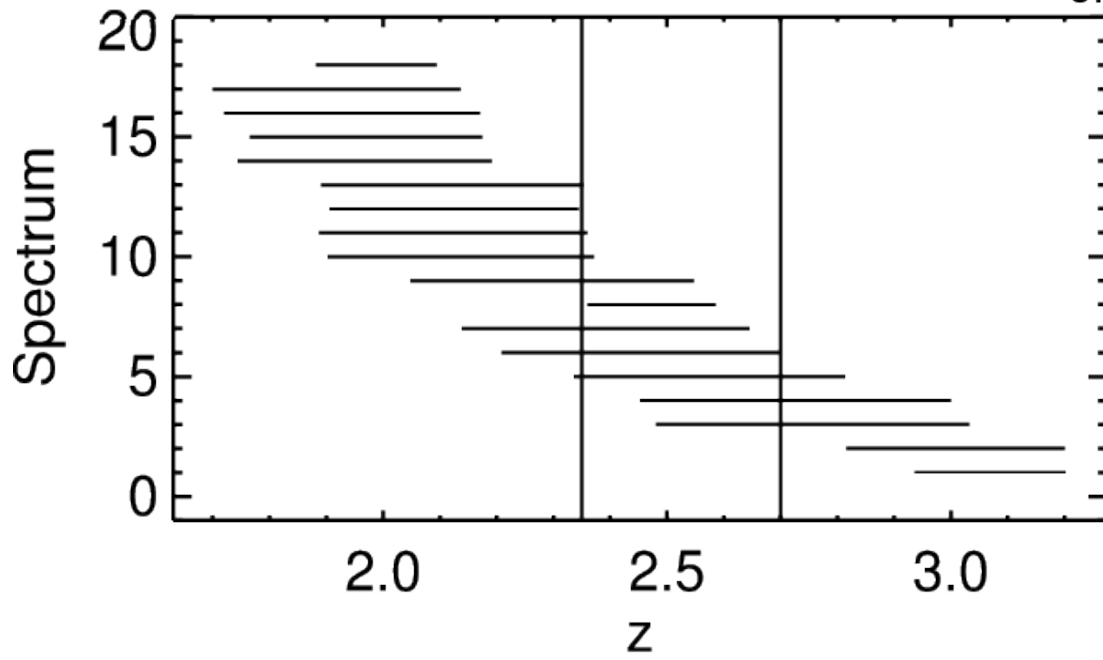
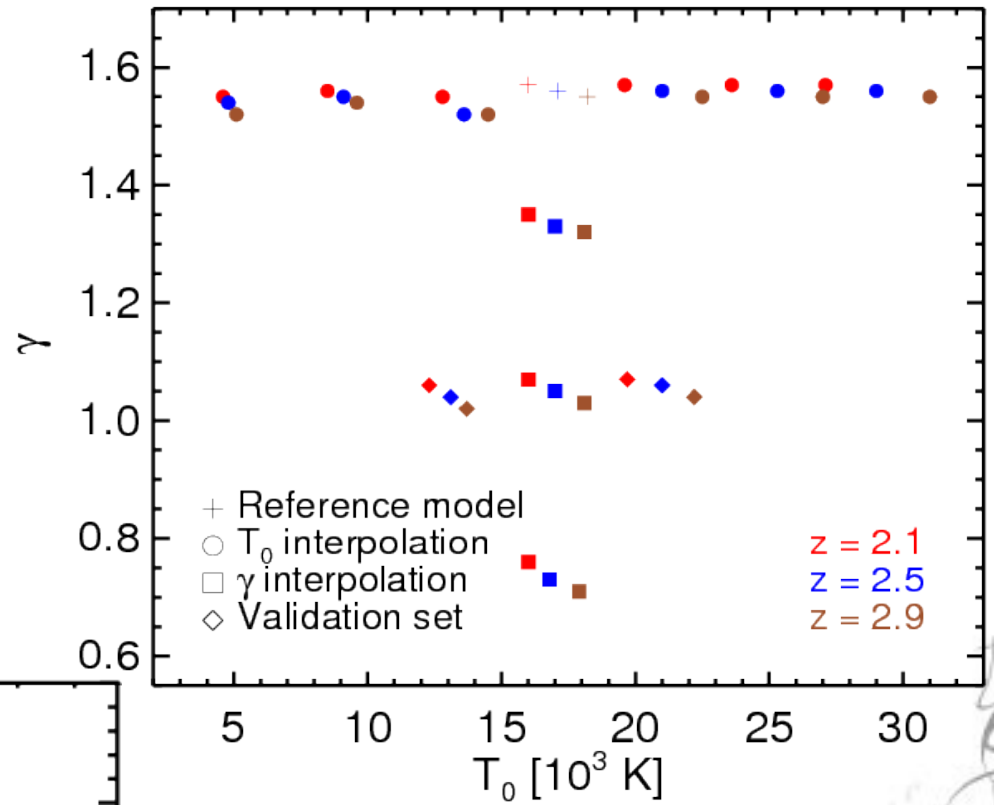
- High resolution numerical simulations (gas + DM) – Gadget 3 (Springel, 2005)
- 256-512³ particles
- 10Mpc boxsize
- Uniform ultraviolet background (Haardt et Madau, 2001)

♦ Interpolation among cosmological and astrophysical parameters

$T_0, \gamma, \tau_{\text{eff}}, H_0, \Omega_m, n_s, \sigma_8$

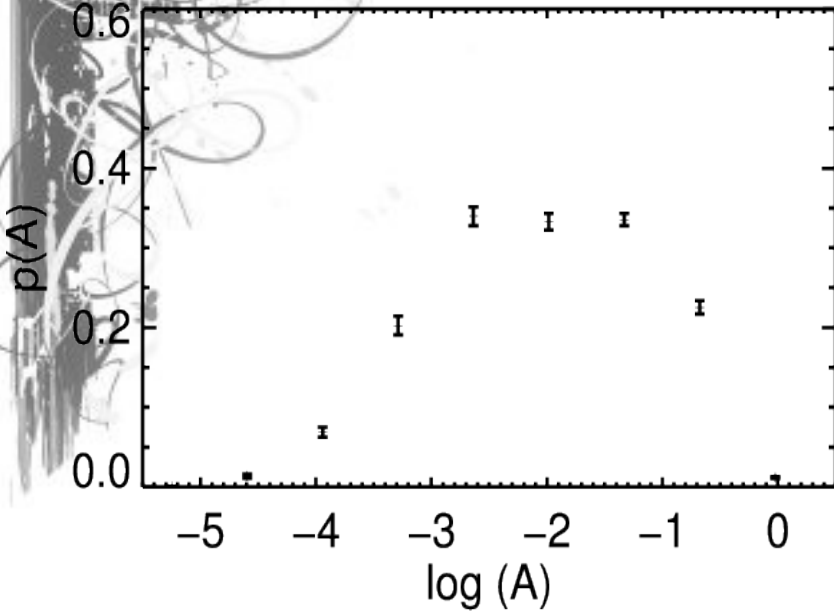
♦ Exploration of likelihood function by Multinest (Feroz et Hobson, 2008)

Observed & Simulated Spectra

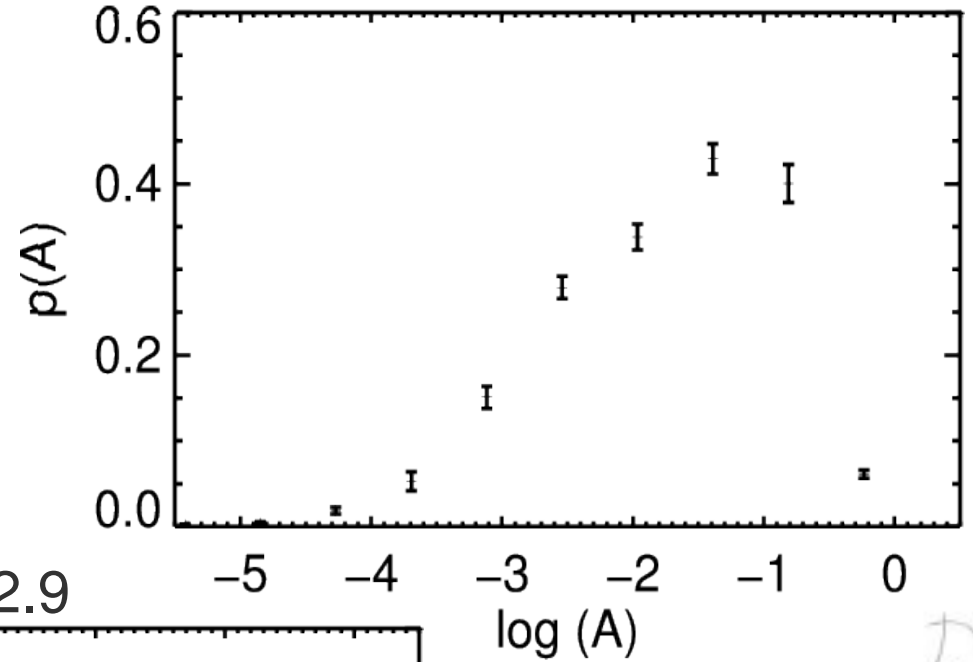


Wavelet amplitude PDF

$z=2.2$

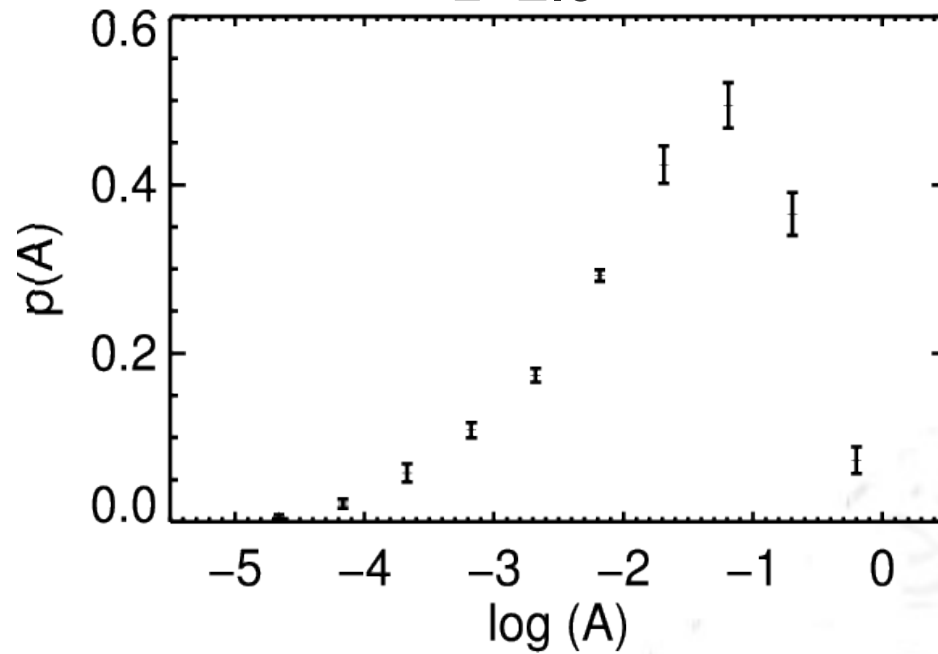


$z=2.5$



$z=2.9$

$r = 70 \text{ km/s}$



Interpolation scheme

Likelihood analysis

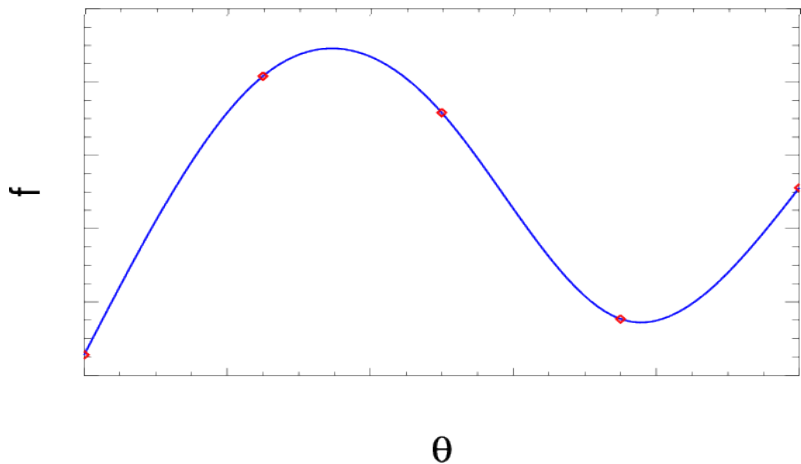
$$\ln L(\theta) \propto (p(A, \theta) - \tilde{p}(A))^T \cdot C^{-1} \cdot (p(A, \theta) - \tilde{p}(A))$$

$$\theta = \{T_0, \gamma, \tau_{\text{eff}}, H_0, \Omega_m, n_s, \sigma_8\}$$

Continuous in θ

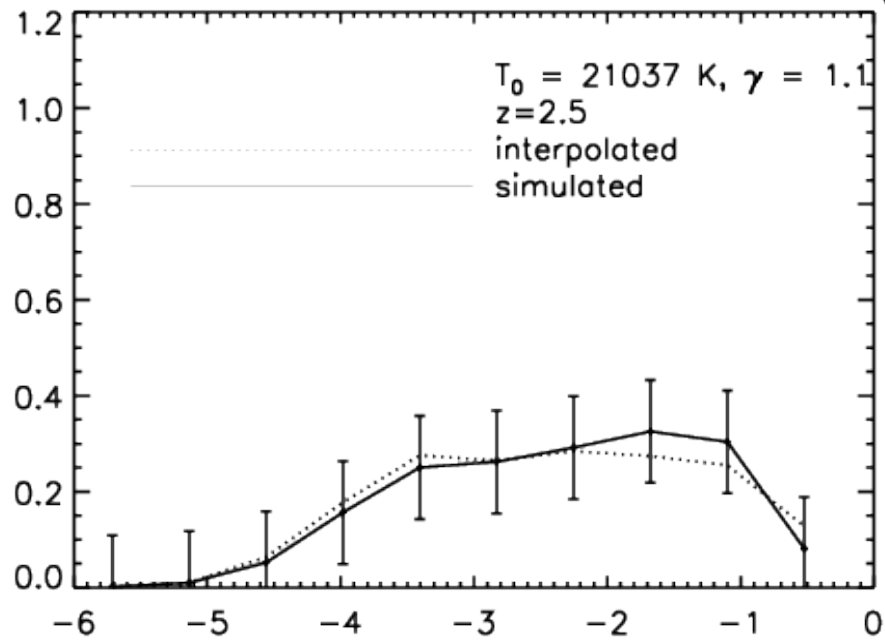
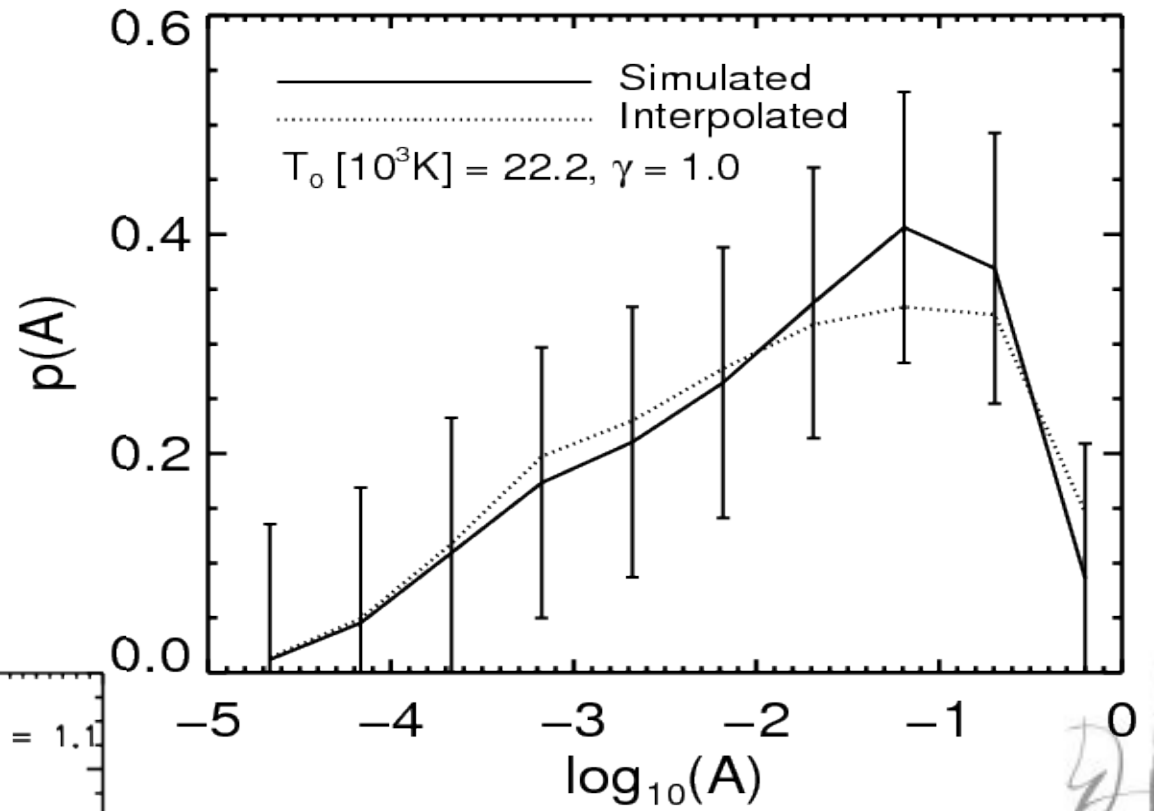
interpolation scheme “taylor expansion” as in Viel et al, 2009

$$p(A_i, \theta) = p(A_i, \theta^*) + f_{\theta_0}(\theta_0 - \theta^*_0) + \dots + f_{\theta_n}(\theta_n - \theta^*_n)$$

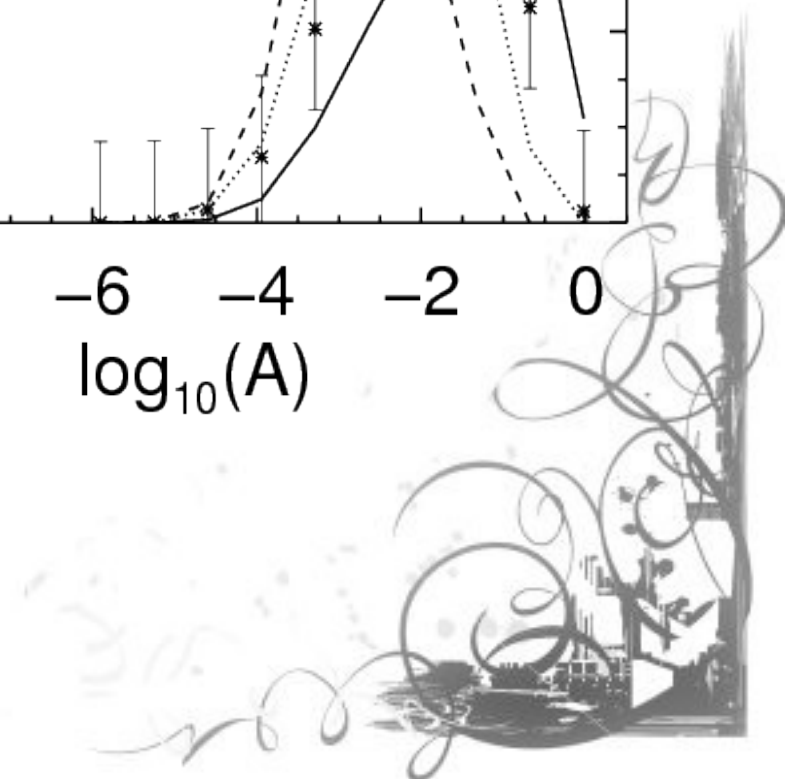
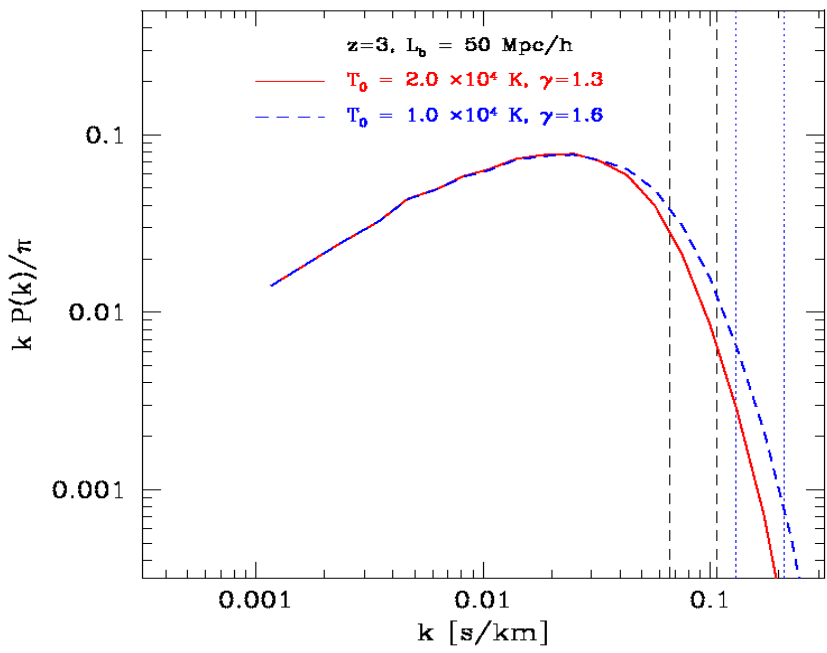
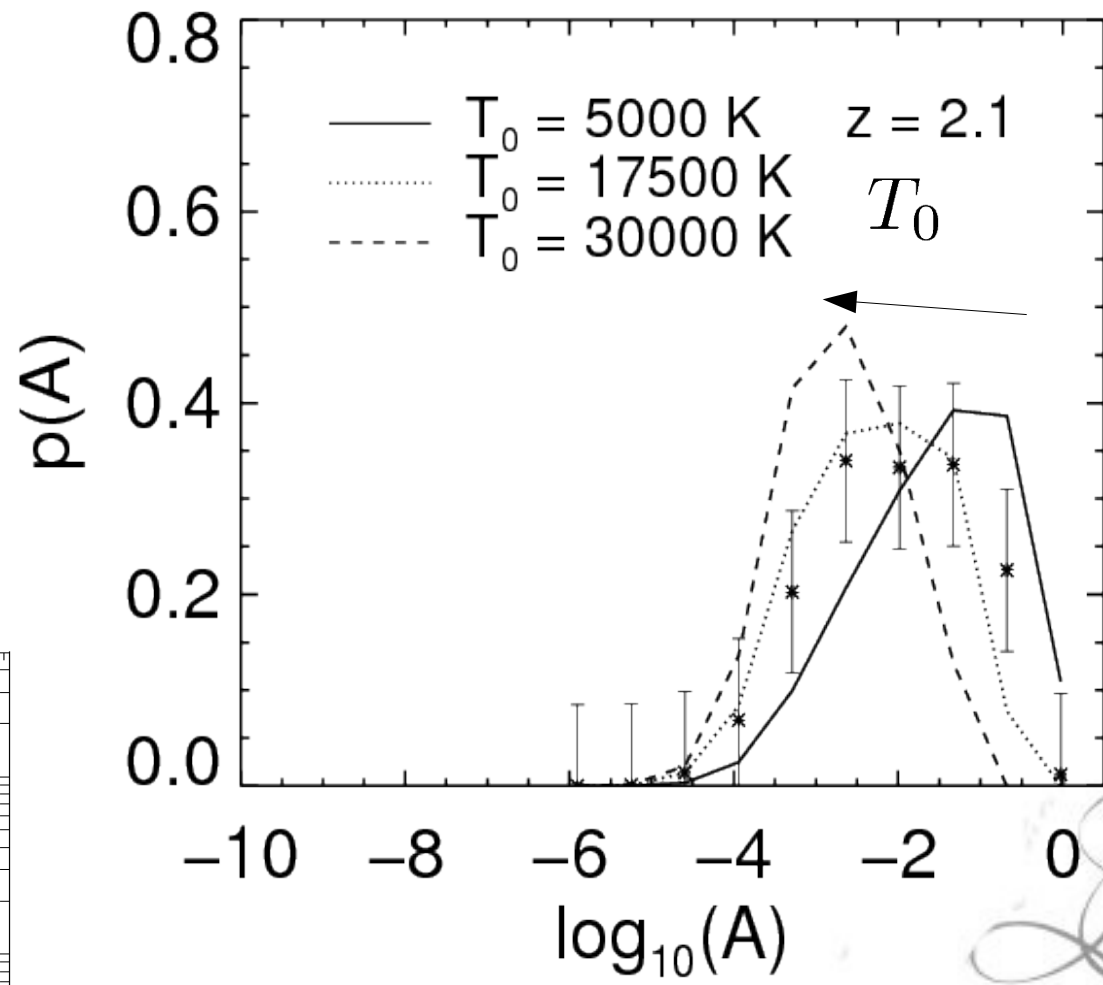
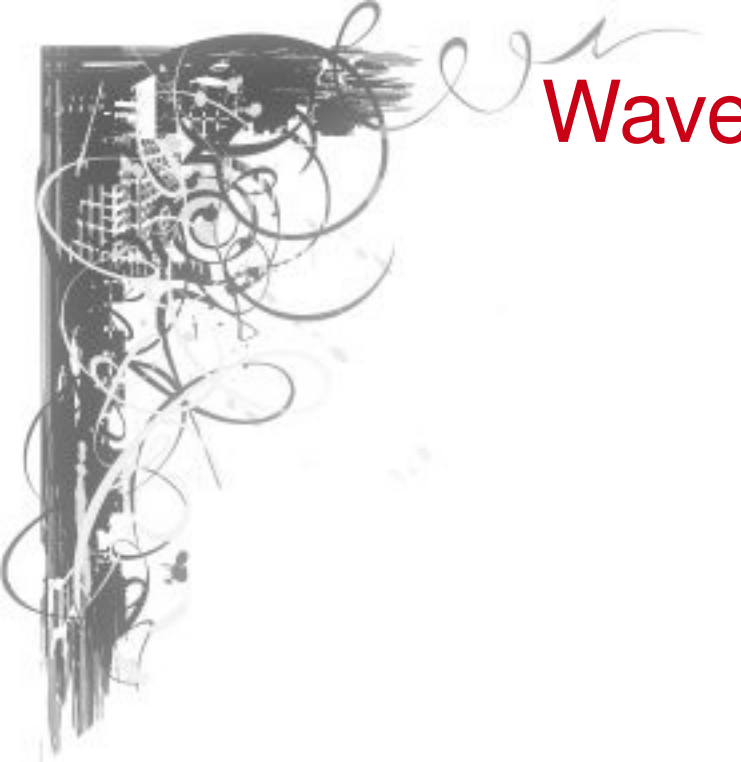


Cubic spline interpolation

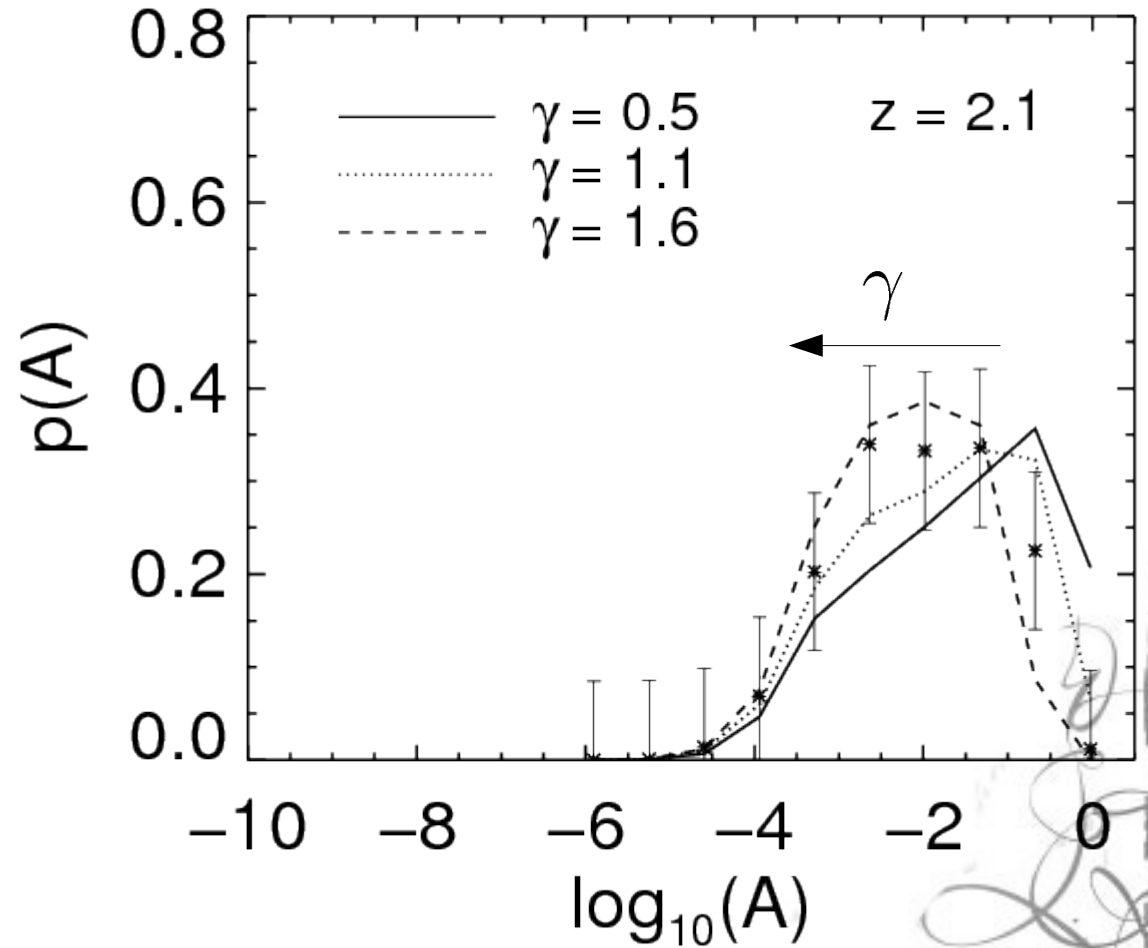
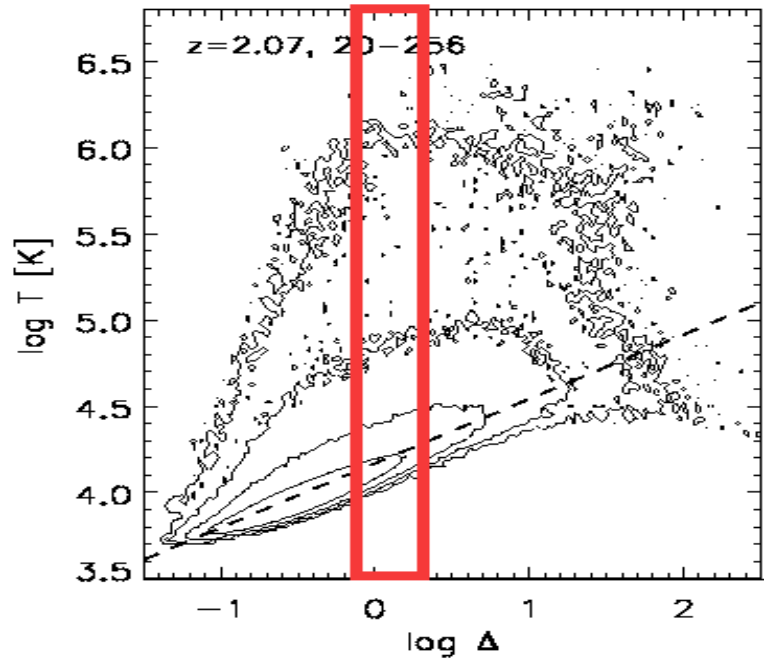
Interpolation scheme



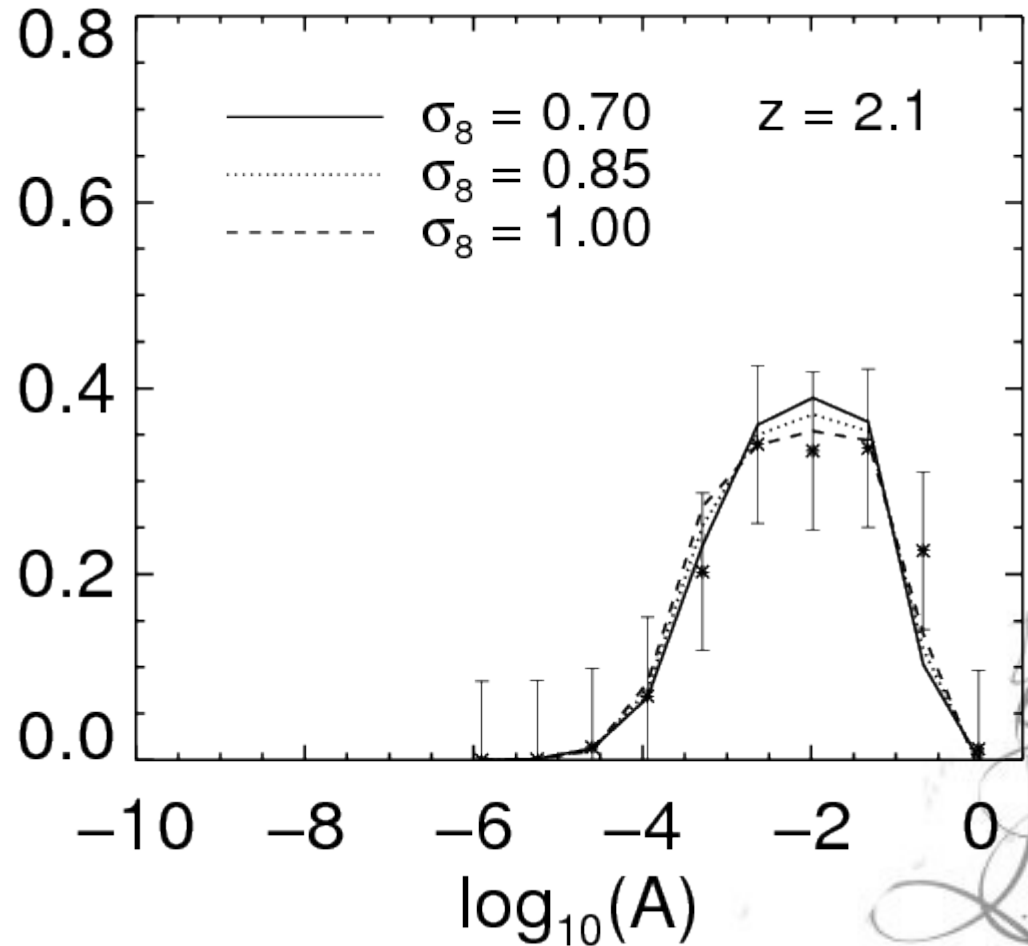
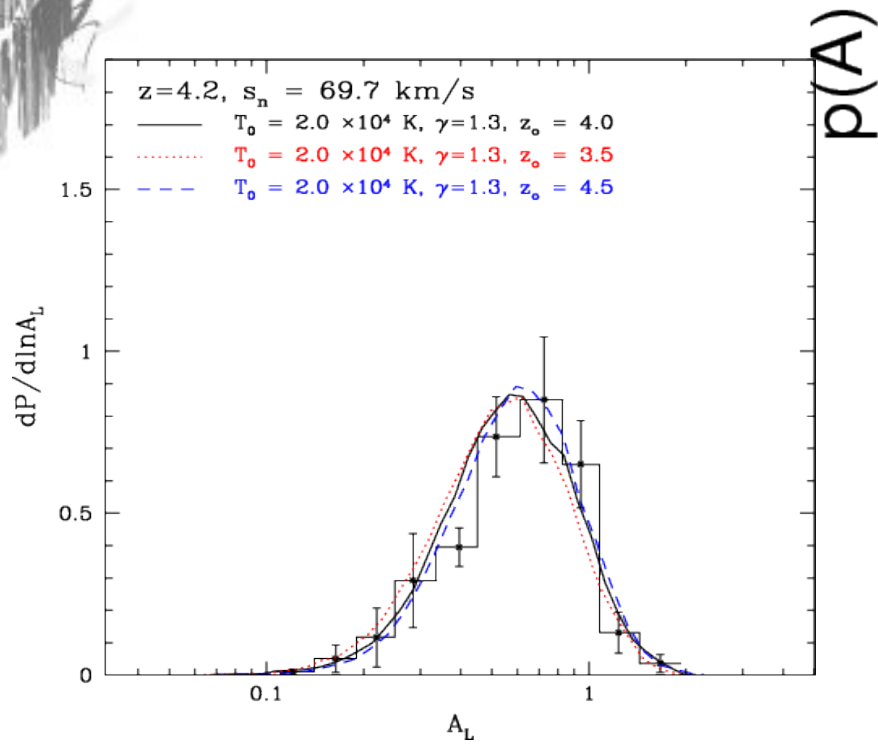
Wavelets as a thermometer



Wavelets as a thermometer




Wavelets & cosmological parameters



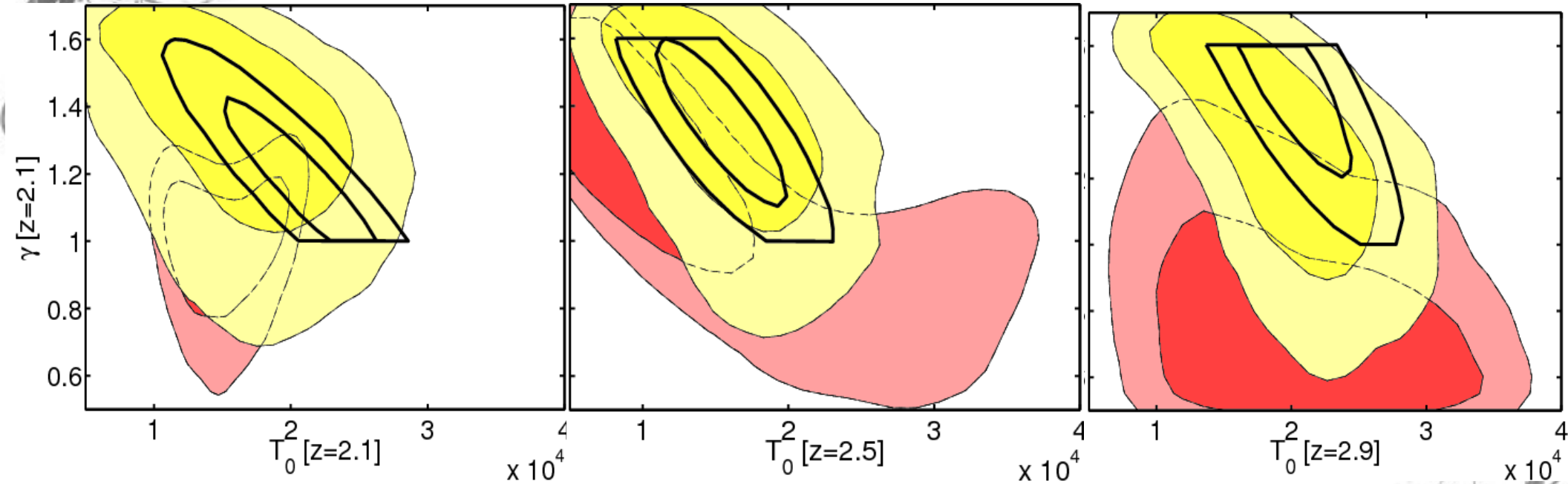
Lower redshift > higher density fluctuations
Higher redshift > lower density fluctuations
Lidz et al, 2010






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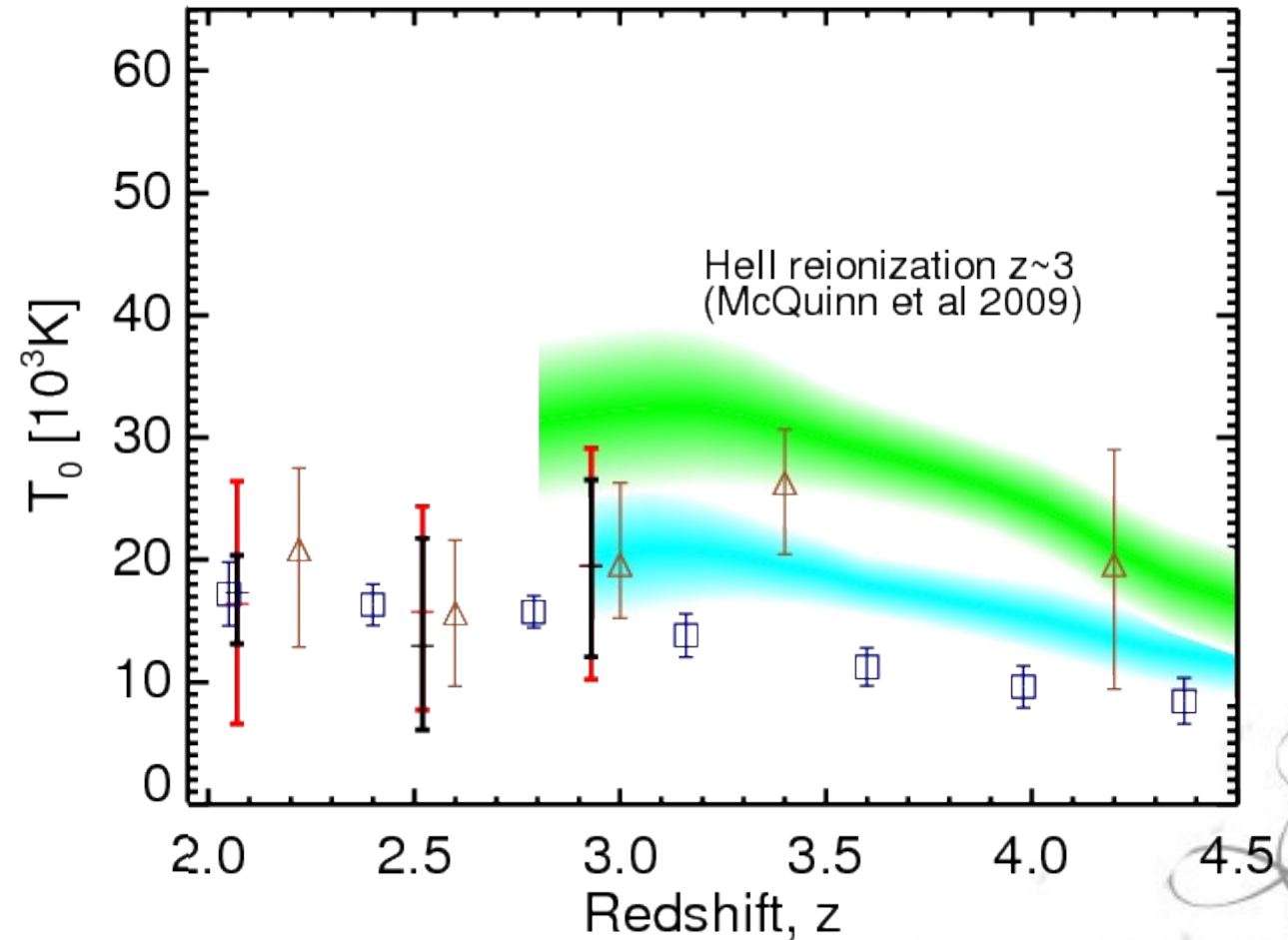
Constraints on IGM thermal state



-  Wavelet filtering
-  Flux PDF (Viel et al, 2009)
-  Lidz et al, 2010

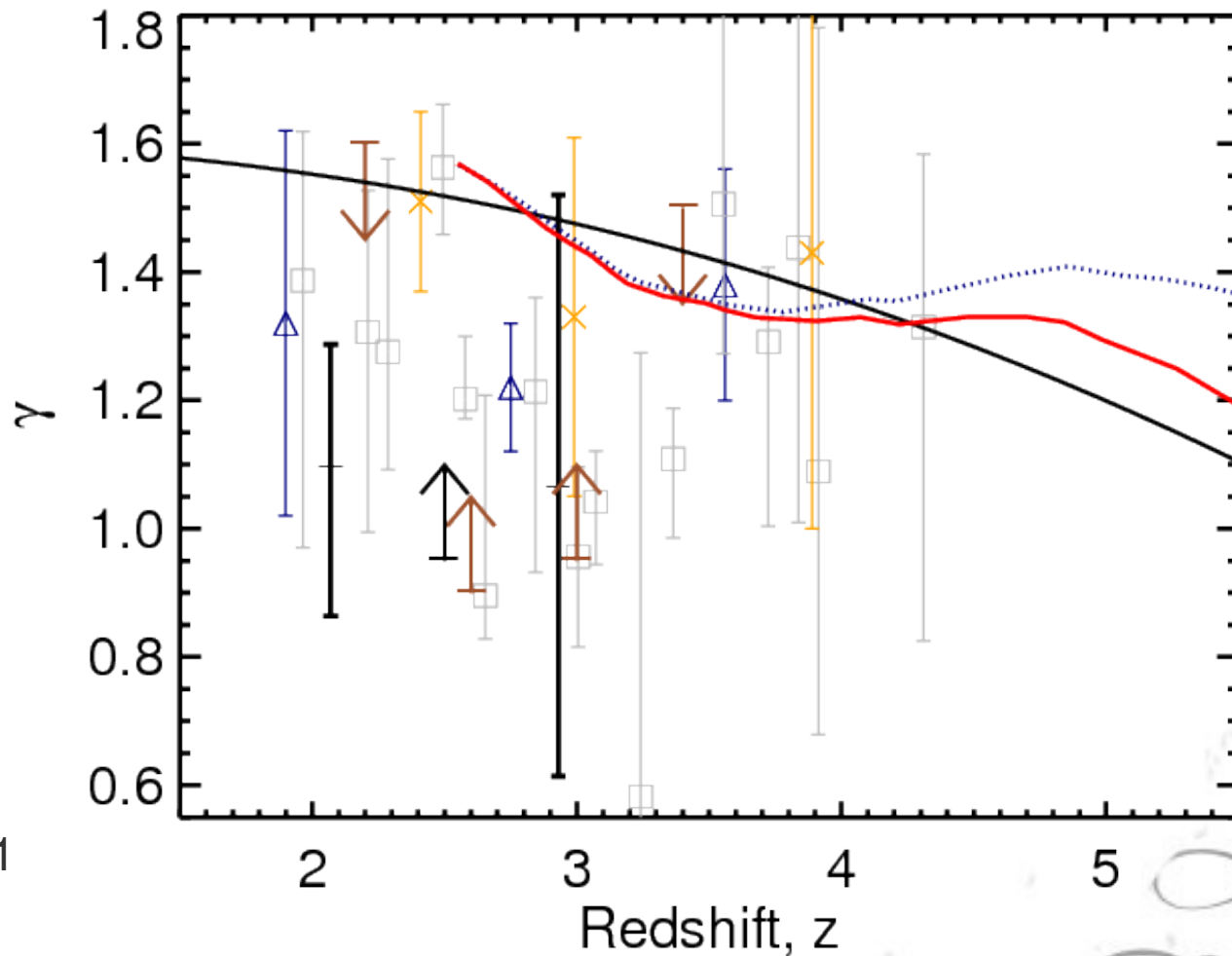


Results: wavelet filtering & joint analysis



- \triangle Lidz et al, 2010
- \oplus Wavelet filtering
- \oplus Wavelet + flux
- \square Becker et al, 2011

Results: wavelet filtering & joint analysis



Ricotti et al, 2000



Lidz et al, 2010



McDonald et al, 2001



Wavelet + flux



Schaye et al, 2000



Hell reionization @ $z=6$



McQuinn et al, 2009 - L1




McQuinn et al, 2009 - L1b

Results: wavelet filtering & joint analysis

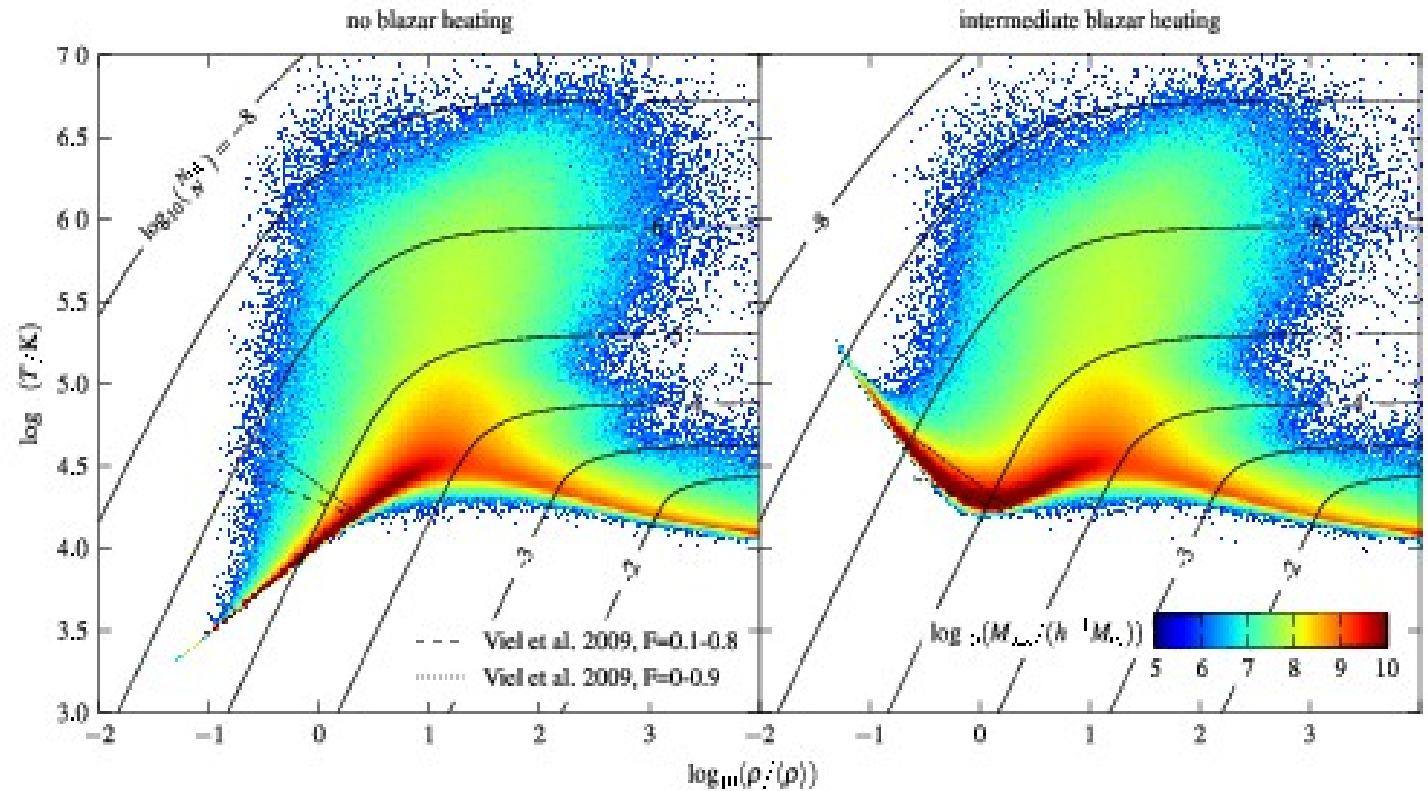
		Wavelet PDF	Flux PDF	Joint analysis
$\langle z \rangle = 2.1$	$T_0 [10^3 \text{ K}]$	16 ± 5	15 ± 3	17 ± 2
	γ	> 0.86	0.99 ± 0.14	1.11 ± 0.11
	τ_{eff}	(0.14 ± 0.04)	0.133 ± 0.004	0.130 ± 0.004
$\langle z \rangle = 2.5$	$T_0 [10^3 \text{ K}]$	16 ± 4	14 ± 9	13 ± 4
	γ	> 0.92	> 0.69	> 0.95
	τ_{eff}	(0.22 ± 0.05)	0.212 ± 0.011	0.200 ± 0.009
$\langle z \rangle = 2.9$	$T_0 [10^3 \text{ K}]$	20 ± 5	21 ± 7	19 ± 4
	γ	> 0.80	< 1.24	1.1 ± 0.2
	τ_{eff}	(0.36 ± 0.09)	0.290 ± 0.019	0.27 ± 0.02



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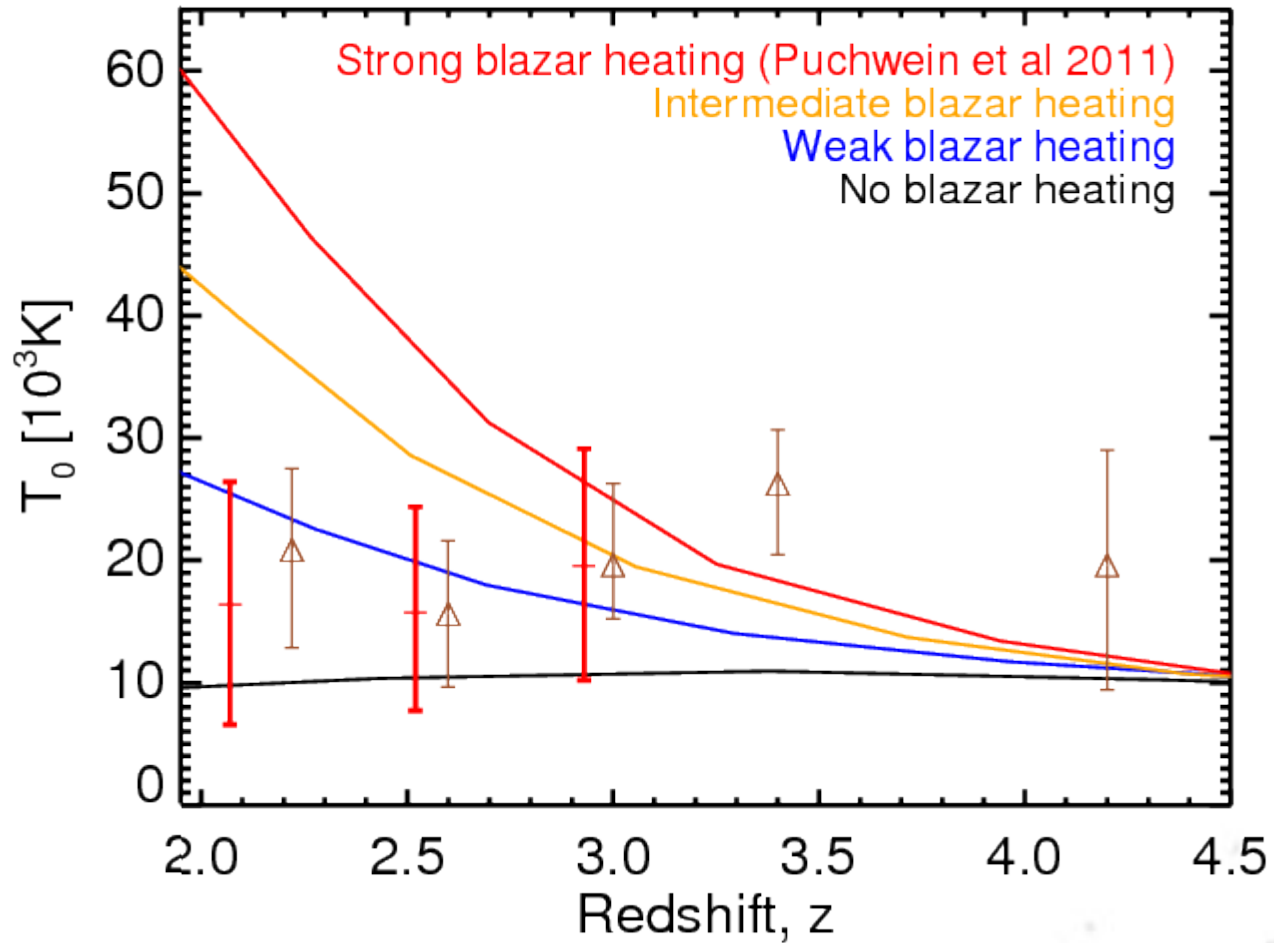
Blazar heating



Puchwein et al, 2012

- TeV emission from Blazars
- Universe at high redshift opaque to TeV emission
- IGM as a calorimeter for Blazar emission
- Changed Temperature Density plane distribution

Blazar heating




\triangle Lidz et al, 2010

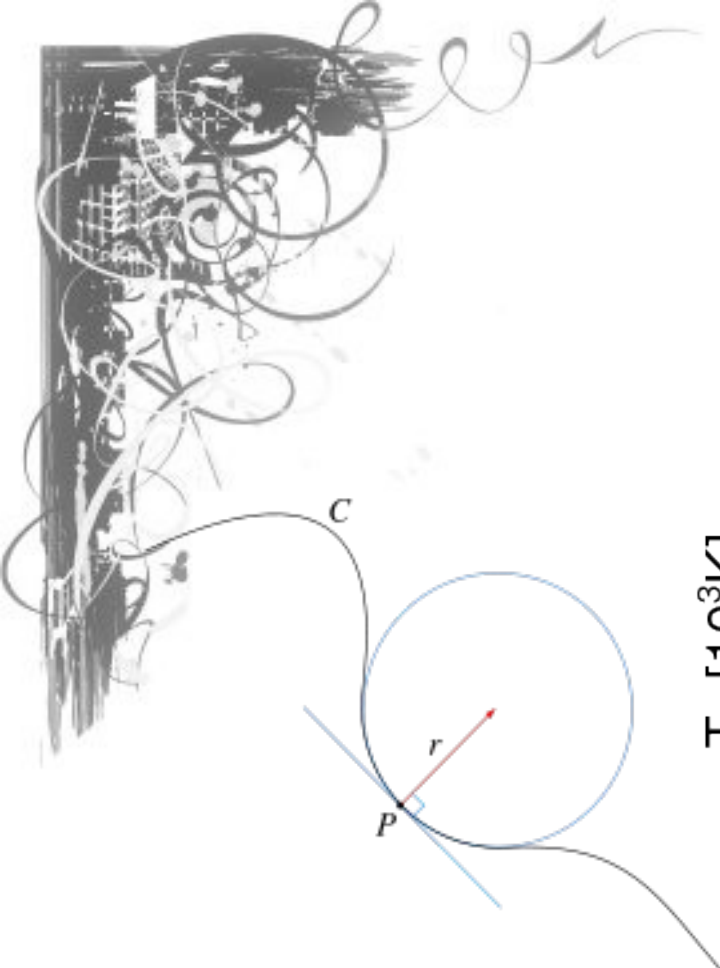
\oplus Our work



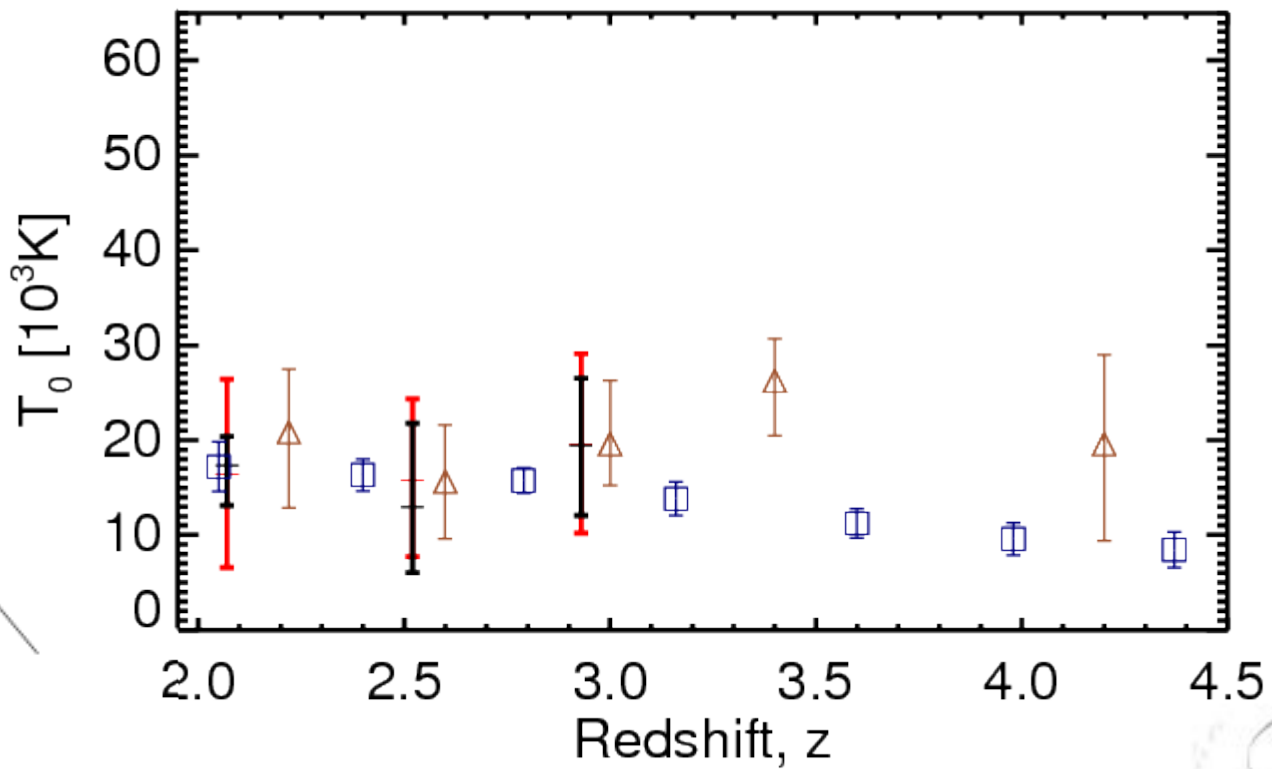
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Curvature



$$\frac{y''}{(1 + y'^2)^{3/2}}$$

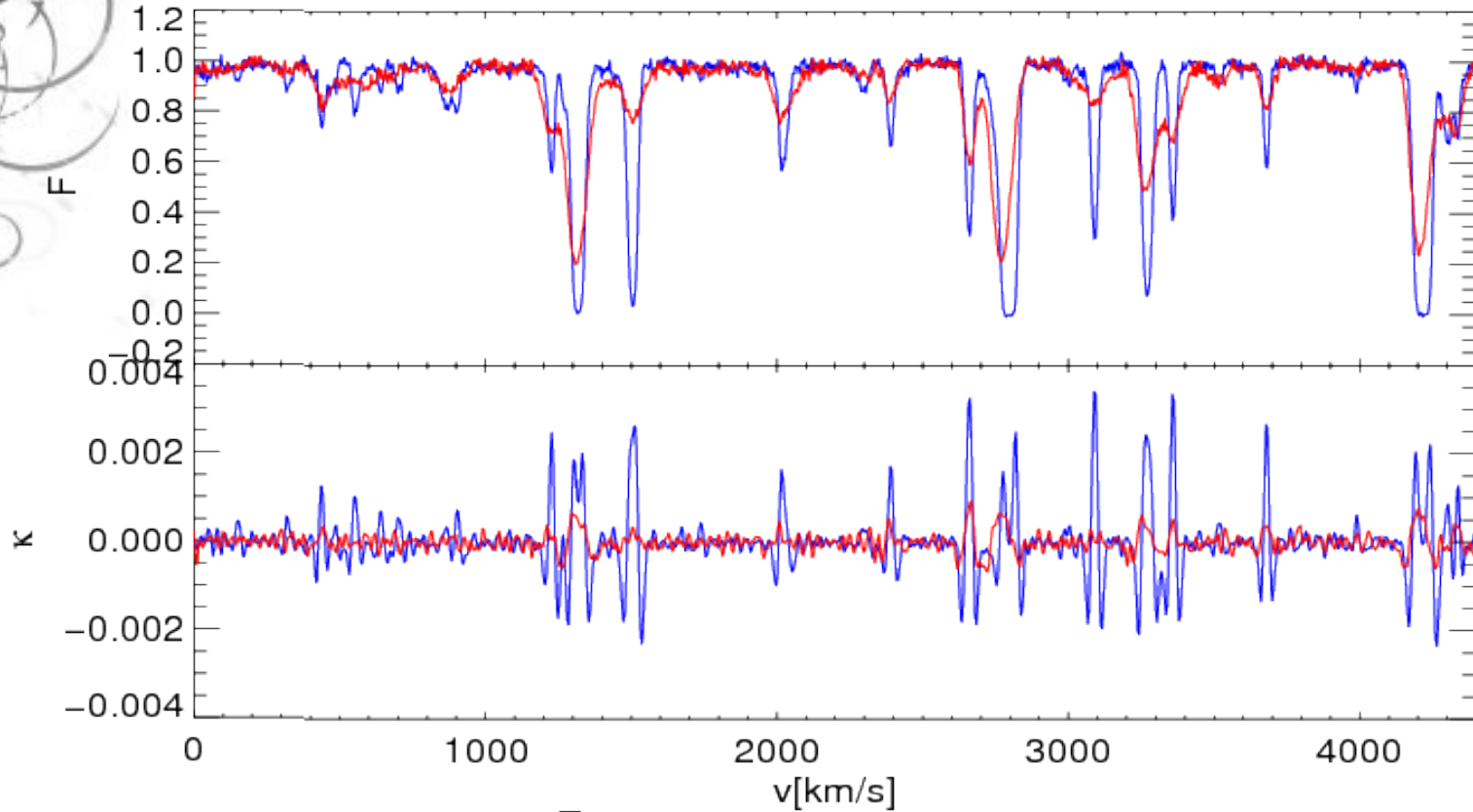


△ Lidz et al, 2010

⊕ Our work

□ Becker et al, 2011

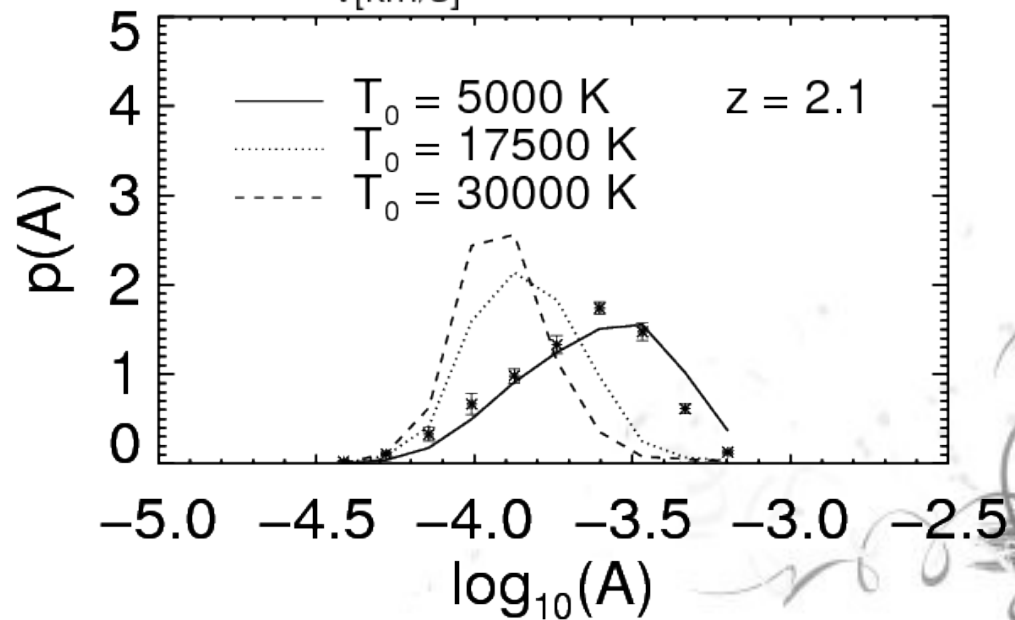
Curvature



$$\gamma = 1.5$$

$$T_0 = 30000 K$$

$$T_0 = 5000 K$$



Conclusions

- Wavelet filtering analysis of the thermal state of the IGM: agreement with results from Lidz et al, 2010
- Varied the relevant cosmological parameters, mild dependence from σ_8 in the lowest redshift bin
- Joint analysis with flux PDF
- Thermal history consistent with previous observations, compatible with additional source of heating at $z < 4$
- Result from joint analysis consistent with $\gamma \sim 1.1 - 1.3$
inverted temperature-density relation still possible ($\gamma < 1$)